

Inductive Learning:

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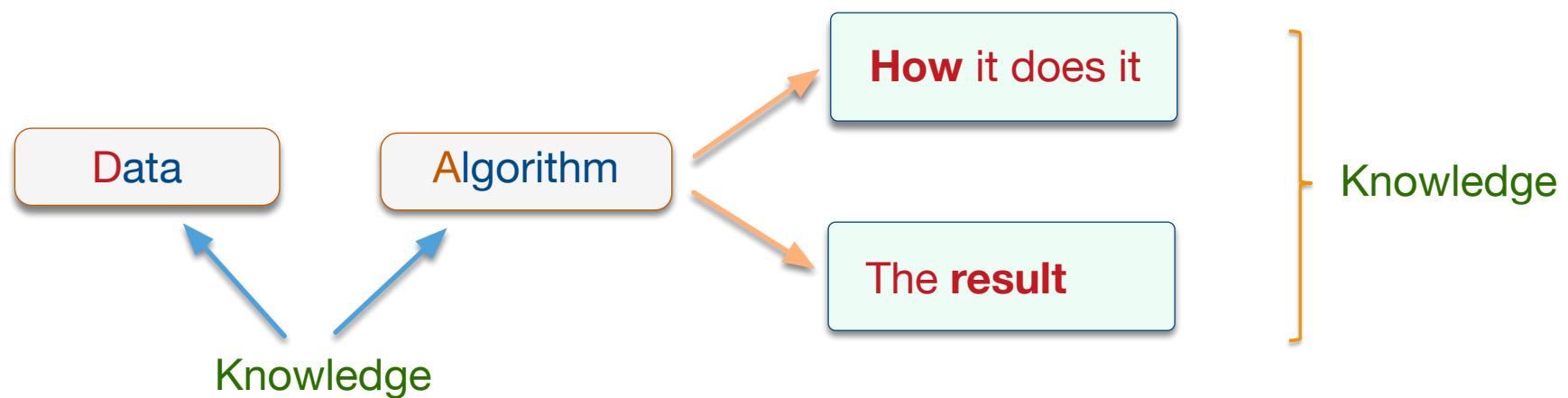
Inductive Learning: a Risky Business

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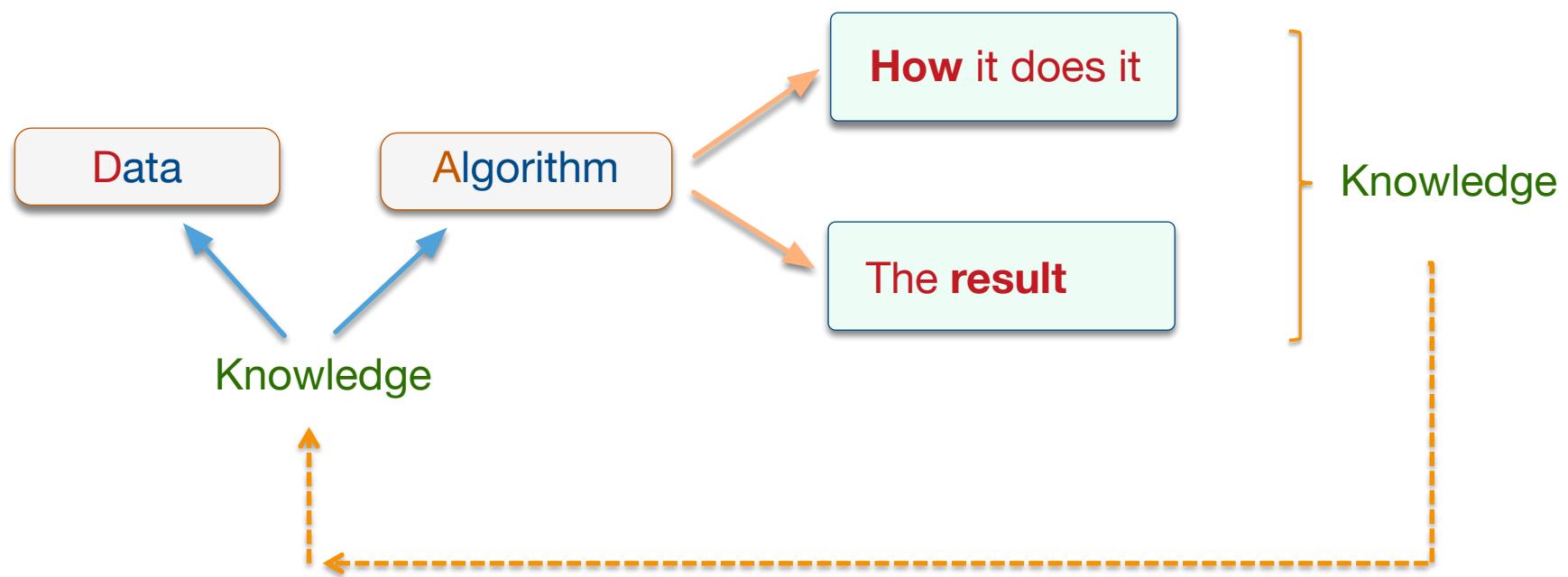
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Inductive learning: what it does



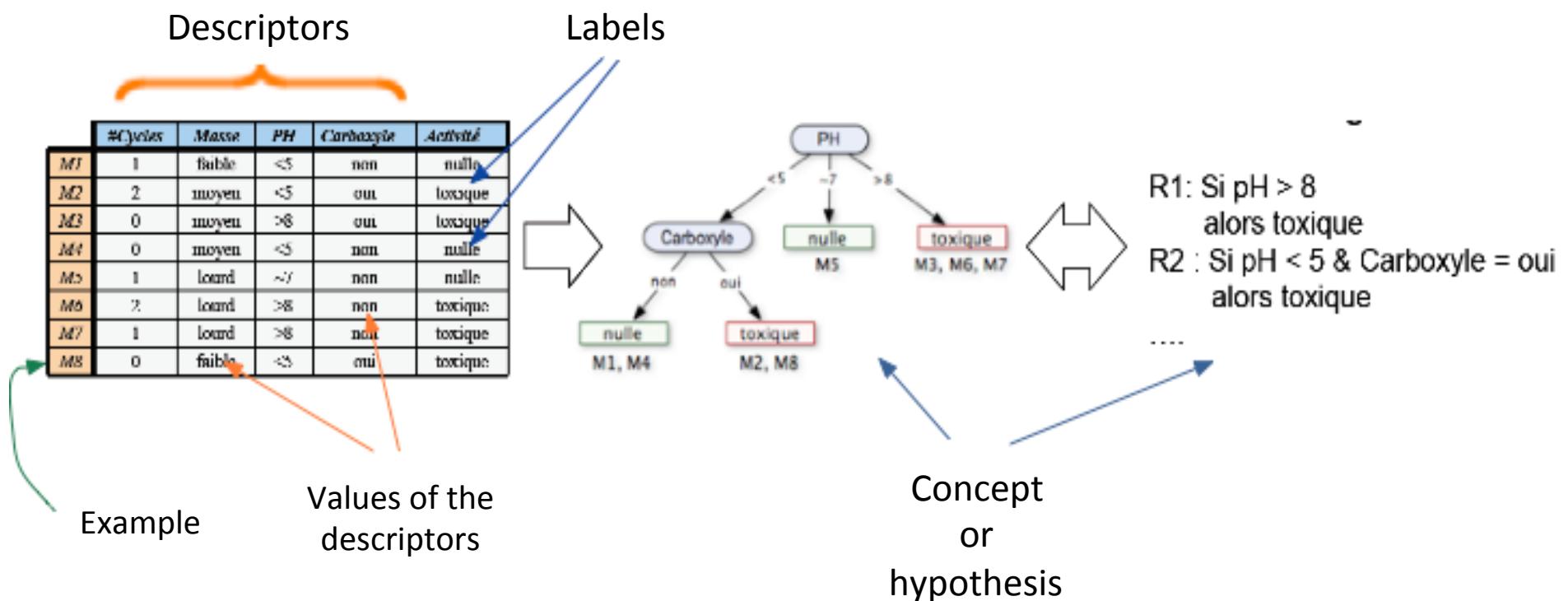
...

Inductive learning: what it does



...

Supervised Induction



What do you expect?

- Better **understand** your data

What do you expect?

- Better understand your data
- Be able to make **prediction**

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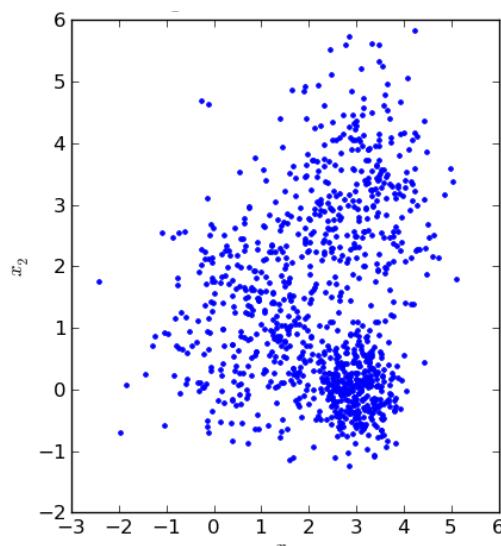
- Better understand your data
- Be able to make prediction
- Be able to make **prescription**

What do you expect?

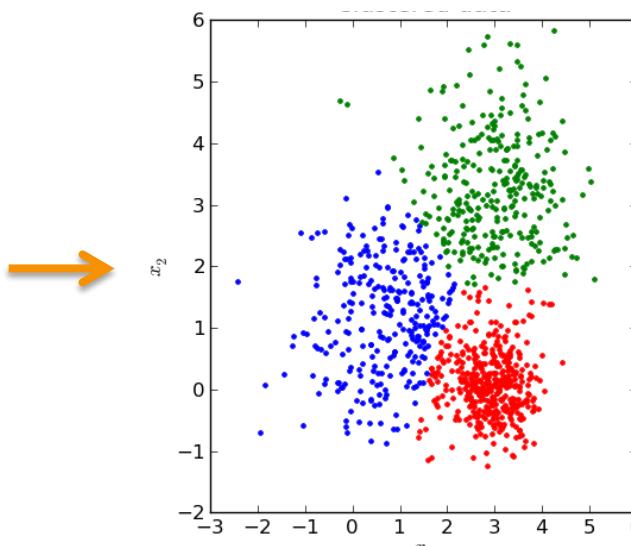
- Better **understand** your data
- Be able to make **prediction**
- Be able to make **prescription**

(1) Understand your data

- Re-express it
 - In a concise way
 - To be interpretable by an expert of the domain



Original data



Clustered data

Three groups of customers with such and such characteristics ...

(2) Make predictions

- Extrapolate your data to find predictive correlations
 - From a training set $S = \{(x_1, y_1), (x_2, y_2), \dots, (x_i, y_i), \dots, (x_m, y_m)\}$

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The diagram shows a mathematical expression for a training set S . Above the set, there is a red curved arrow pointing downwards from the letter f . Below the set, there is another red curved arrow pointing upwards from the letter h .

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The diagram shows a set of training data points S . Above the set, the letter f is written in orange, with a curved orange arrow pointing downwards towards the set. Below the set, the letter h is written in blue, with a curved orange arrow pointing upwards from the set.

New $x \rightarrow y ?$

(2) Make predictions

- **Extrapolate** your data to find predictive correlations
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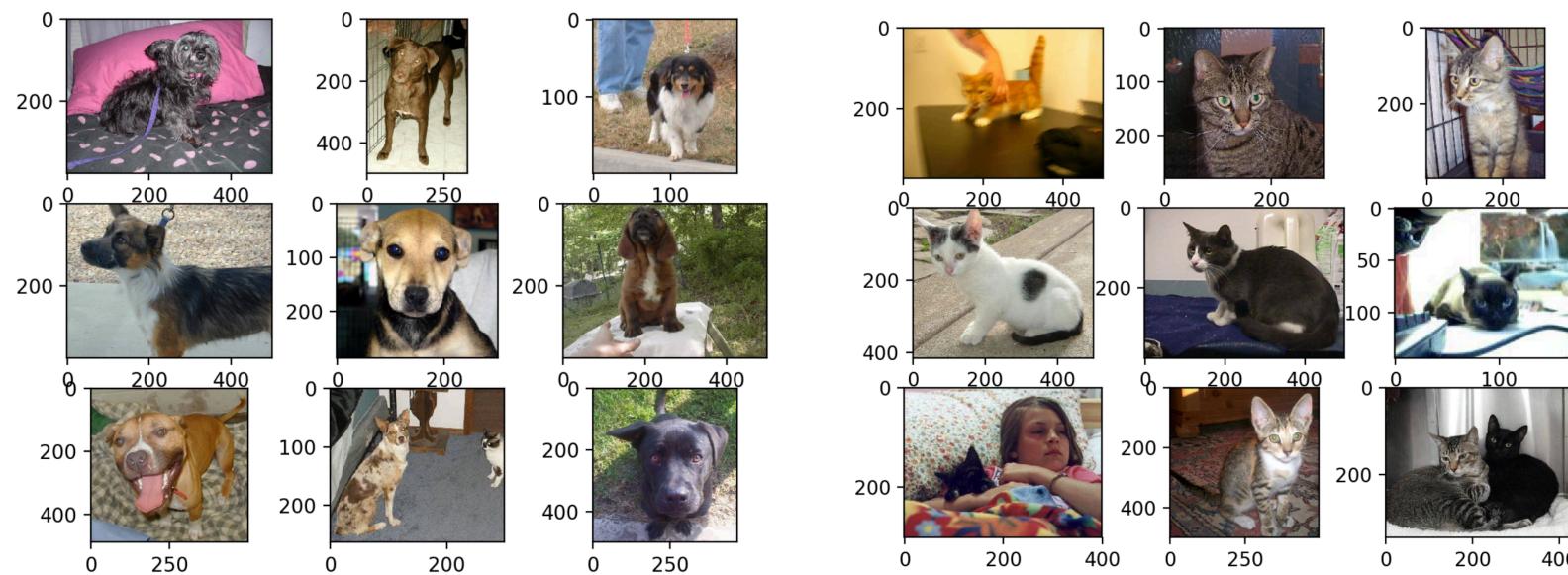
The diagram illustrates the process of learning a hypothesis. A set of training data points S is shown below. Above it, a function f maps the data to a hypothesis h . An orange curved arrow points from the set S up to the label f , and another orange curved arrow points from the label h back down to the set S .

$x - h \rightarrow y$

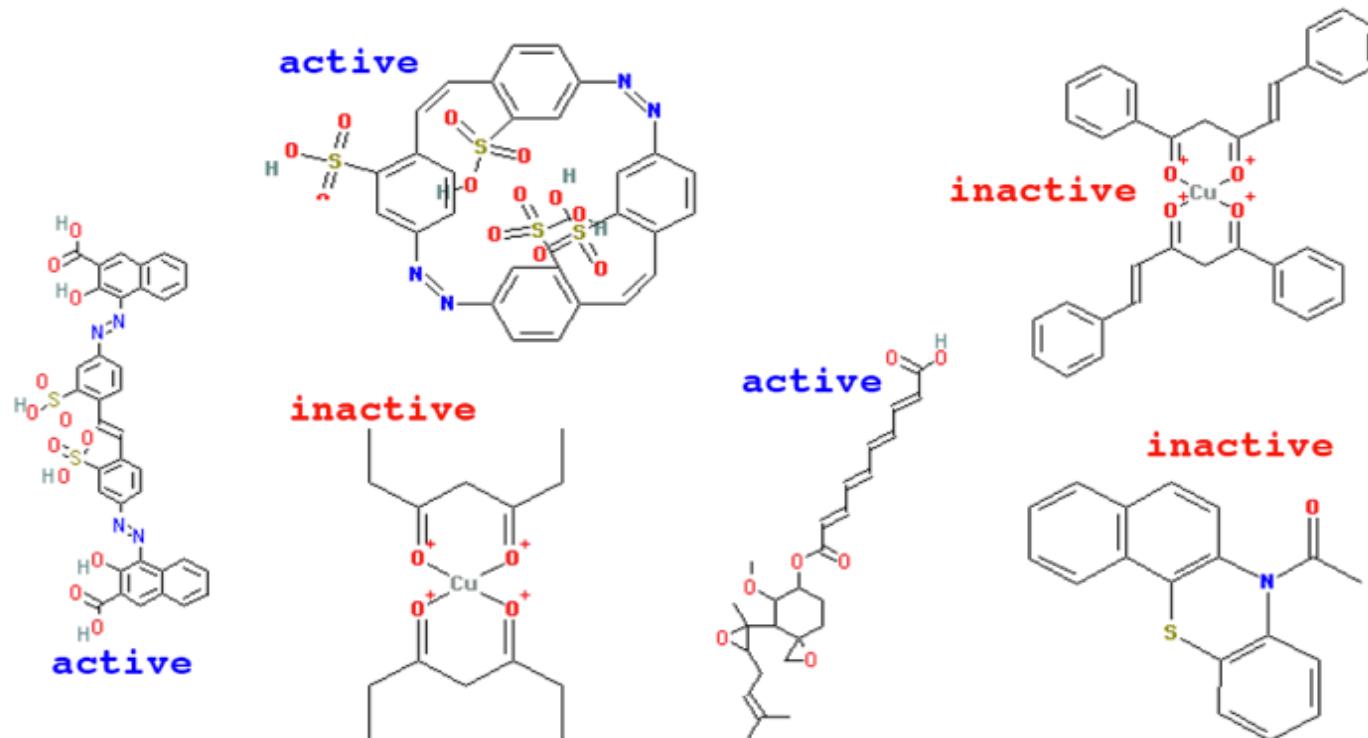
(2) Machine Learning as ...

... Learning a **function** from an **input** space X to an **output** space Y

Cats vs. dogs



Supervised learning



NCI AIDS screen results (from <http://cactus.nci.nih.gov>).

(3) Make prescriptions

- Learning **causal** relationships
 - The barometer **allows the prediction** of tomorrow's weather
 - But tampering with its needle **will not** change the weather

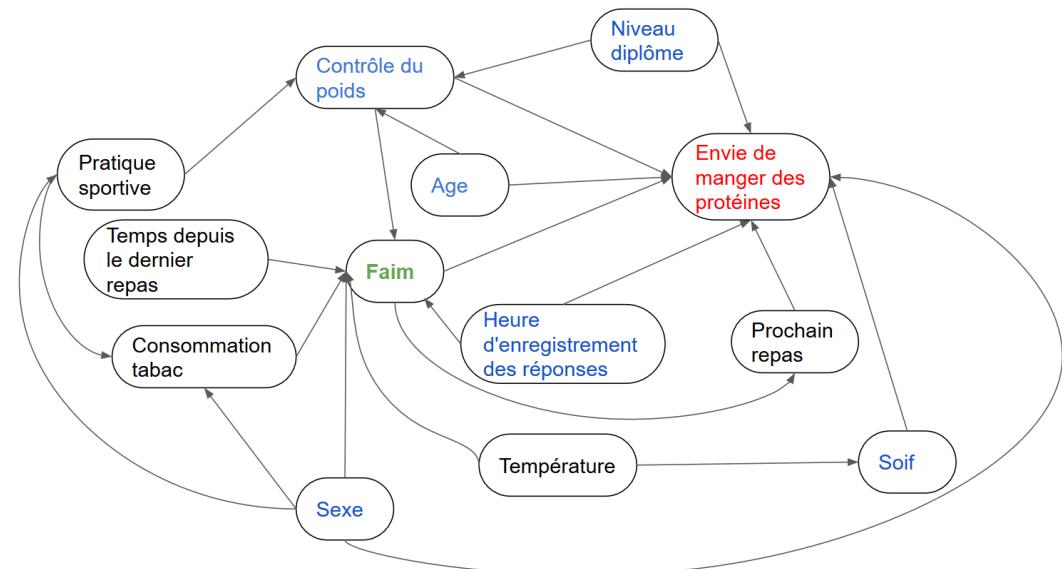
Correlation **is not** causality

Discovering causal relationships
(generally) requires knowing **more than the data**

Looking for causal relationships

- What **causes** appetite for protein dishes?

- Hunger ?
- The hour in the day ?
- Gender ?
- The visual aspect ?
- The olfactory aspect ?
- The high protein content of previous meals ?
- ...



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 - Wants to see things that are not really there
 - Blind to interesting but out of the blue patterns

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Descriptive learning usually takes place in an **exploratory phase**

→ Be very careful

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 - **Interpretability** of the model
 - Explanation/**justification** of the prediction
 - **Fruitfulness** wrt. the domain theory

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Often, we are **not** interested in prediction alone,
but in **understanding** the **prediction** and/or the **predictive model**

How do you evaluate the results?

- **Predictive learning**

- **Predictive performance** (on a test set)
 - E.g. error rate
- But, this is not all there is to it. We want also
 - **Interpretability of the results**
 - **Interpretability of the model and the process**
 - Gaining a **better understanding of the world**
when including the learned decision function in an existing theory

Often, we are **not** interested in prediction alone,
but in **understanding** the **prediction** and/or the **predictive model**

A basic principle

- Machine Learning “just” **reformulates** what has been given as input
- A **conservation theorem**:
 - **No information is “added”**
 - Data + prior knowledge

A basic principle

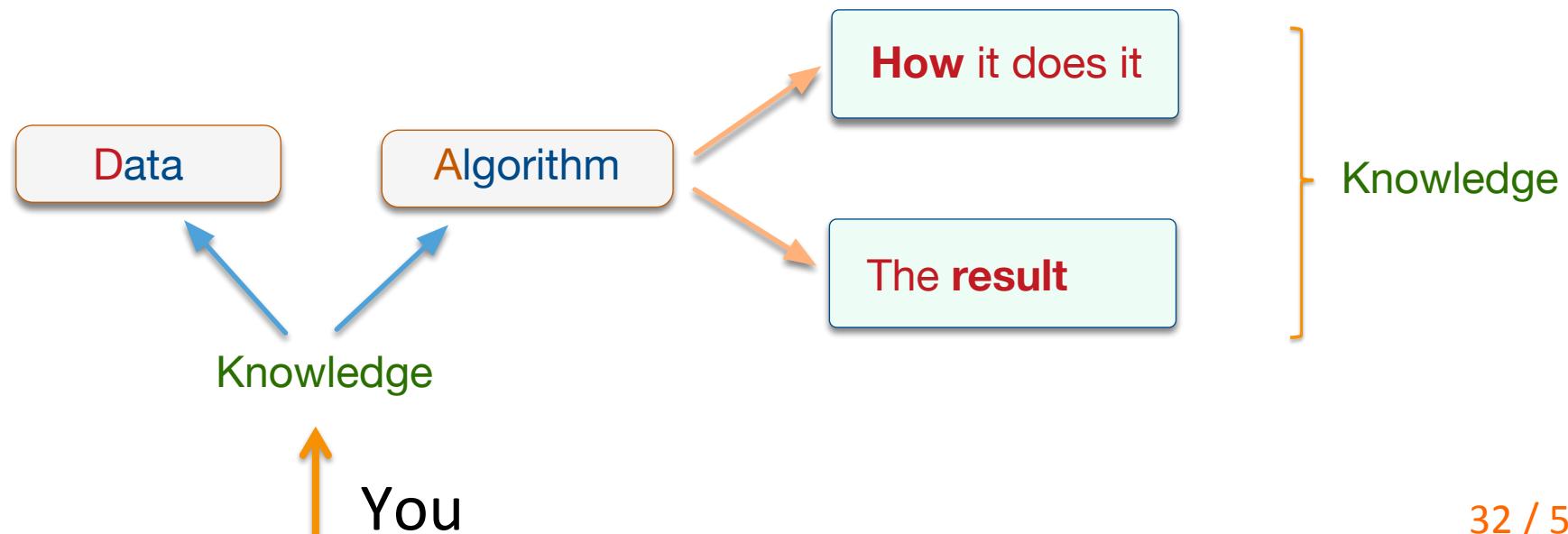
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Little data + lots of prior knowledge
Big data + less prior knowledge

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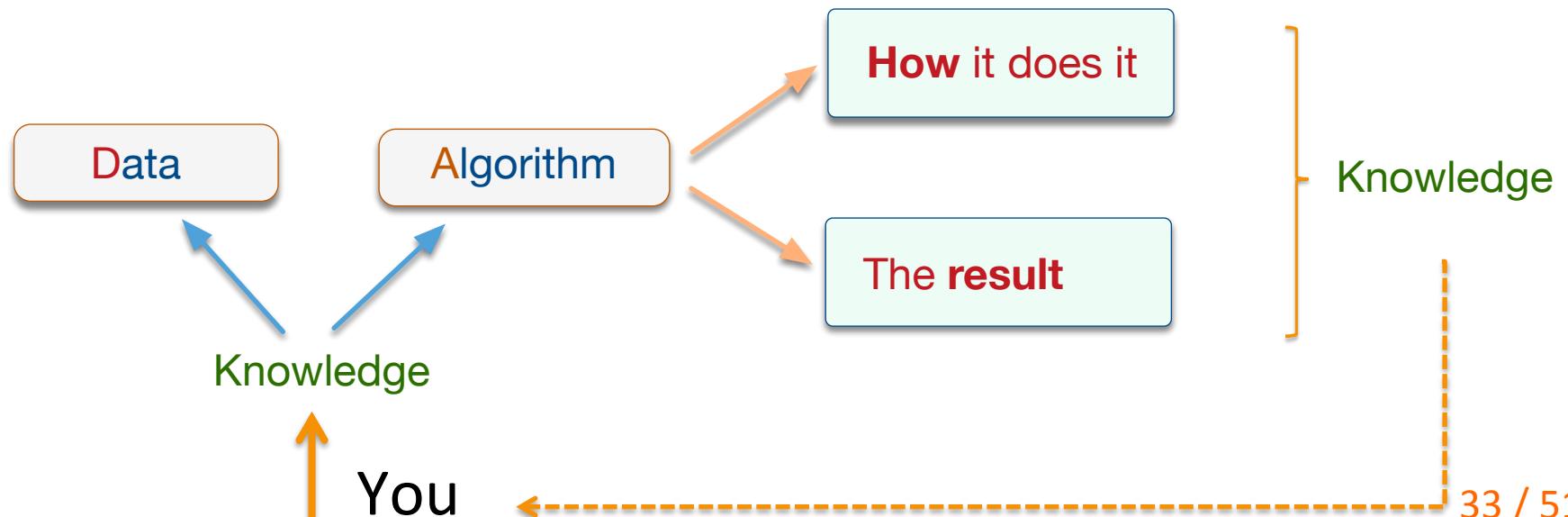
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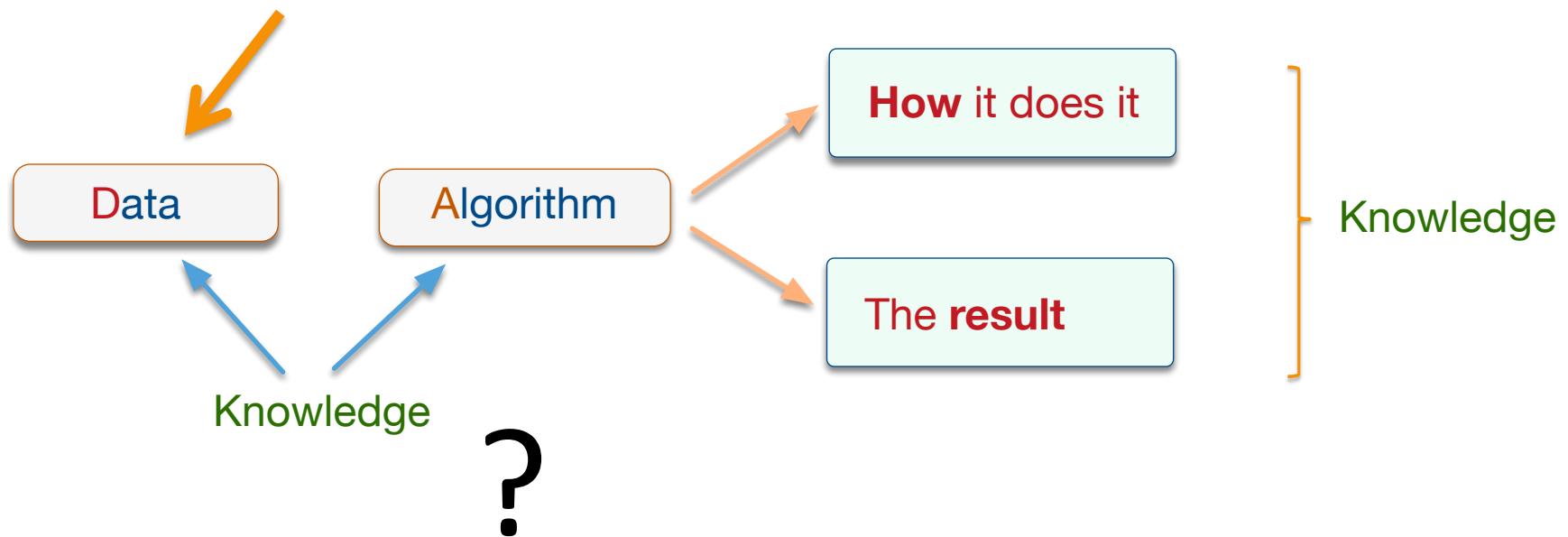
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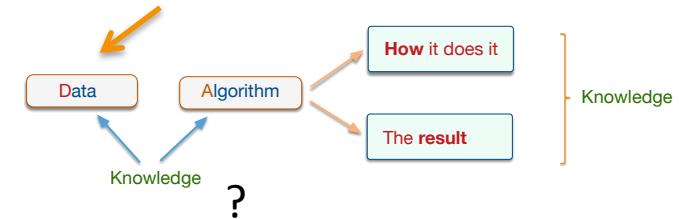
Prior knowledge



...

Knowledge as input to ML

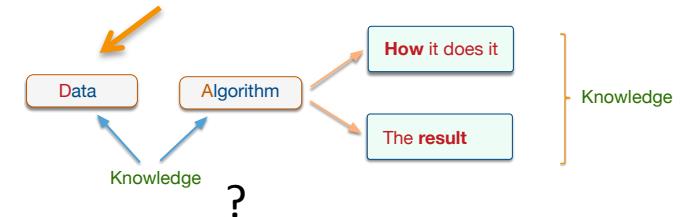
- Knowledge in the data
 - The experimental apparatus
 - Choice of the descriptors (the features)
 - Enrichment using ontologies
 - Normalization of the values
 - Missing values
 - Possibly added data point
 - With invariances in mind
 - ...



Knowledge as input to ML

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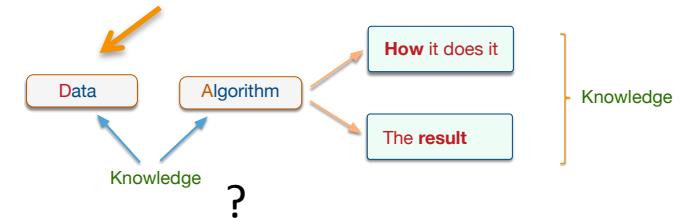
- The experimental apparatus → With its own imperfection and biases
- Choice of the descriptors (the features)
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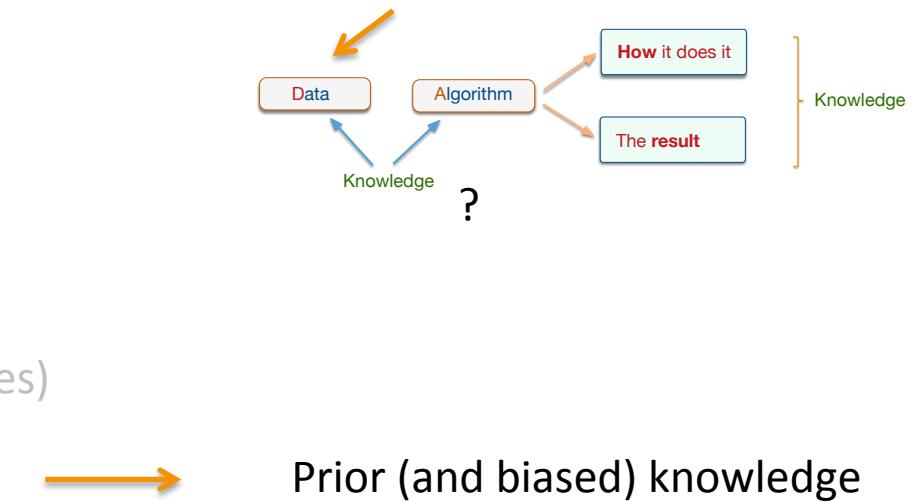
- The experimental apparatus
- Choice of the descriptors (the features) → Necessarily biased
- Enrichment using ontologies
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Knowledge as input to ML

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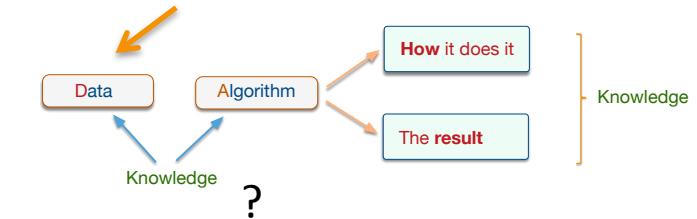


Prior (and biased) knowledge

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→ No perfect normalization

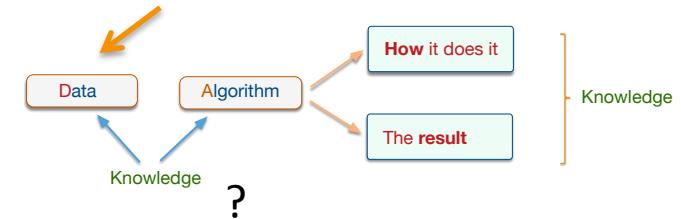
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What choice of imputation method?



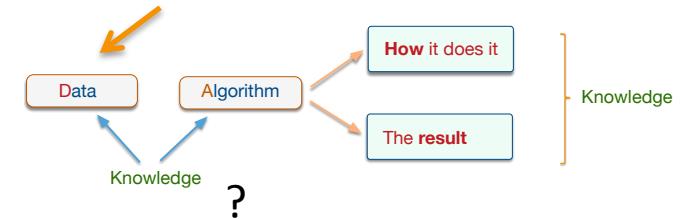
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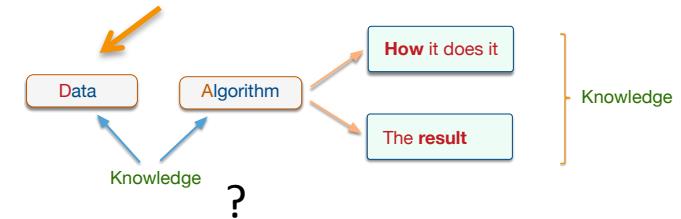


How do you add points?
Choice of invariance (prior assumptions)



Knowledge as input to ML

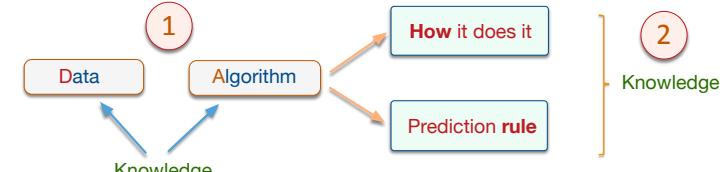
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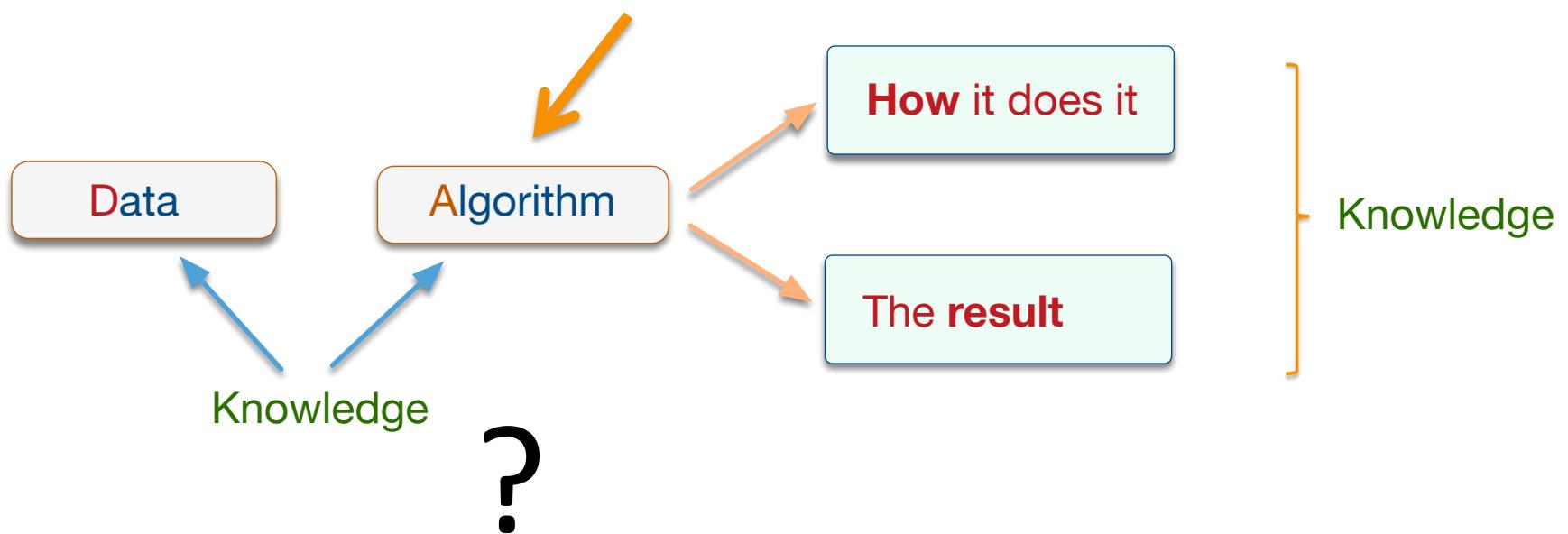
Prior assumptions
everywhere

Knowledge as input to ML

- Knowledge in the data



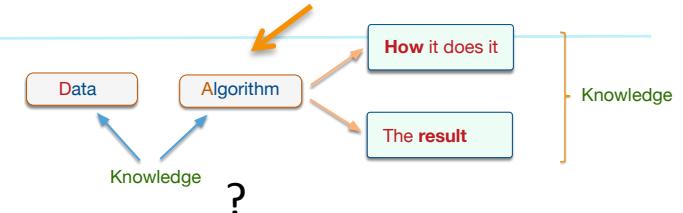
And sometime, there is not even that much
available data!



Knowledge as input to ML

- Knowledge in the learning algorithm

- Constraints on the hypothesis space: representation bias



$$h^* = \underset{h \in \mathcal{H}}{\text{ArgMin}} \left[R_{\text{Emp}}(h) + \lambda \text{reg}(h) \right]$$

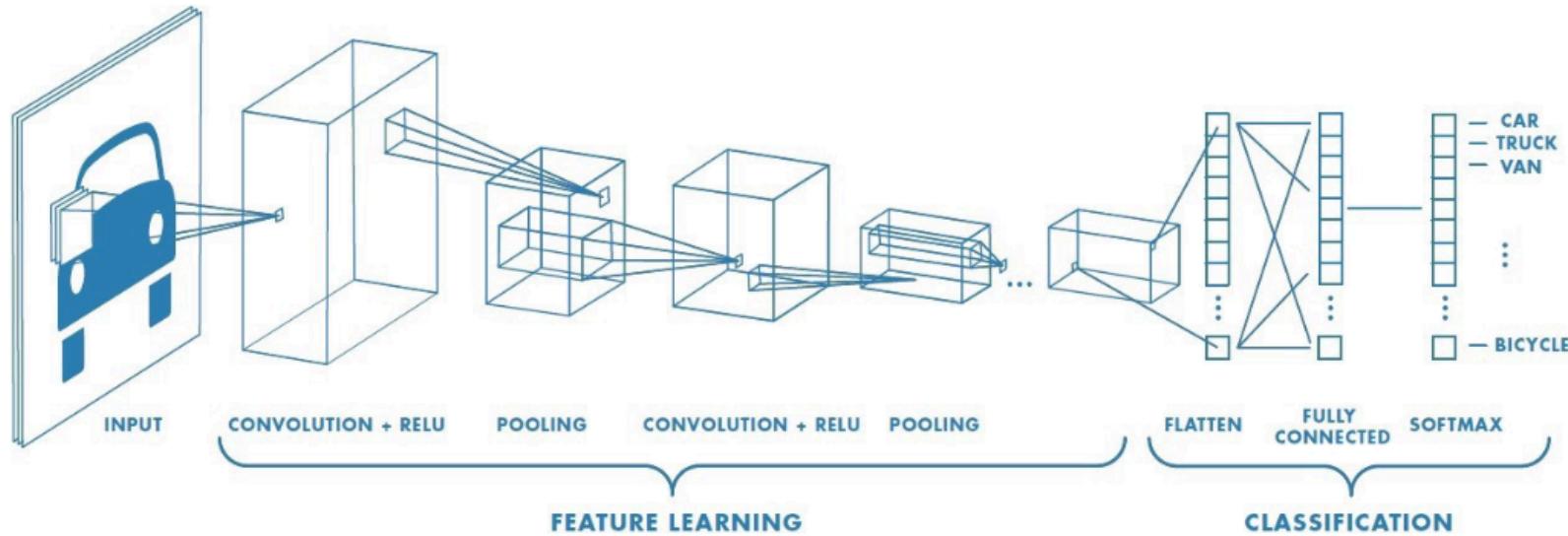
Looking for sparse linear hypotheses

$$h^* = \underset{h \in \mathcal{H}}{\text{ArgMin}} \left[\frac{1}{m} \sum_{i=1}^m \ell(h(\mathbf{x}_i), y_i) + \lambda \|h\|_1 \right]$$

Favors hypotheses with few non null coefficients

Knowledge as input to ML

- Convolutional Neural Networks
 - Knowledge embedded in the architecture of the network

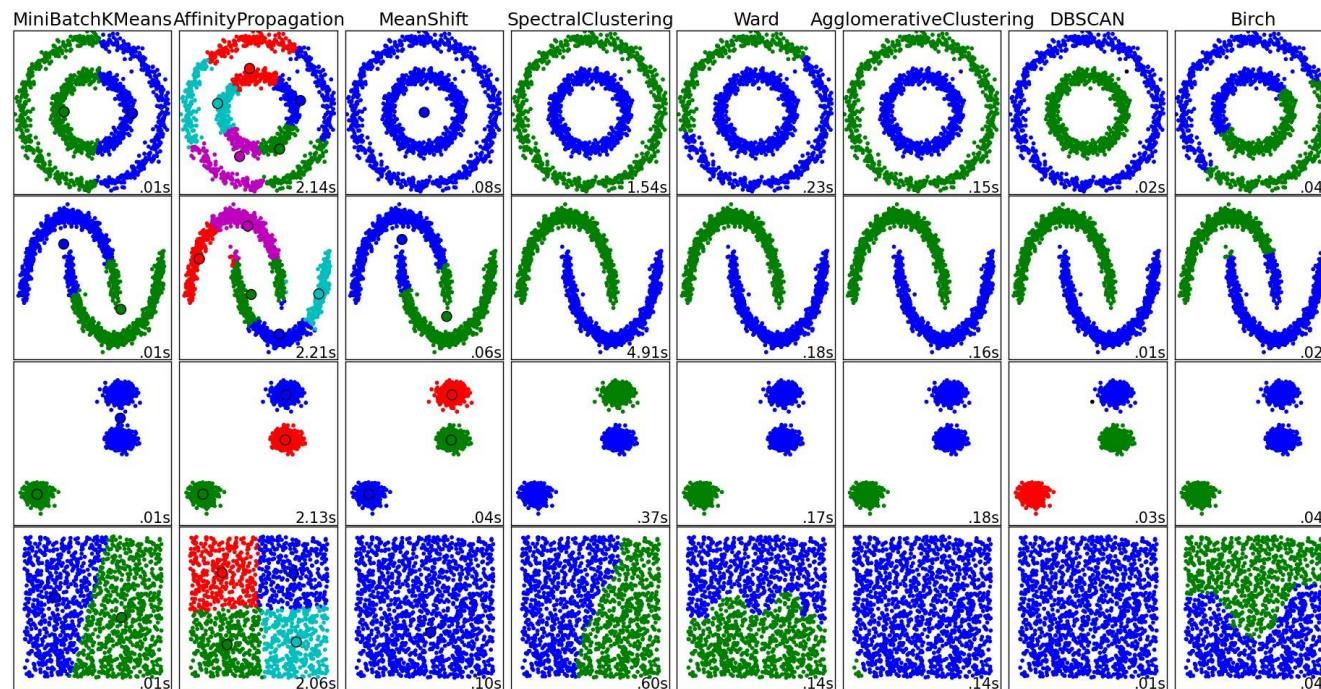


From <https://towardsdatascience.com/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53>

What current Inductive Learning is good at

1. Identifying patterns in data (DESCRIPTIVE learning)

- But no guarantees about the value of their value



What current Inductive Learning is good at

2. Discover **prediction rules** based on statistical correlations (PREDICTIVE learning)

- Geared towards **minimizing prediction errors**
- In **stationary** environments
- **Statistical** correlations: needs lots of data and ...



Is this less of a car
because the context is wrong?

Some current challenges

- Non stationary environments
- Heterogeneous multiple sources
- Interpretability of the results
- Integration in larger reasoning systems (including people)

Induction is a **risky** business

1. You have to **invest a lot**
2. And **be very careful** about the yield

Machine Learning DOES NOT produce absolute truths

Do not give up your **critical sense** at every step!

Induction is a **risky** business

1. You have to **invest a lot**
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But **do not abandon hope**

Machine Learning is a **useful tool** ... in good hands

