

# Linear Elasticity Tutorial 2D bar problem clamped at one end while being pulled at the other end (Dirichlet-Neumann-Point boundary conditions case)

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## Abstract

This document details a single tutorial of 'linear elasticity' module of PSD in a more verbose manner.

Similar simulations, as in the previous tutorial is presented in this section. We showcase the 2D bar problem simulation with one end clamped while being pulled at the other end. Contrary to simulation in the previous tutorial, the clamped end just restricts  $x$  movement, i.e.,  $u_x = 0$ . Just like simulation from the previous tutorial the body force is neglected. Just like simulation in the previous tutorial, the non clamped ends pull is approximated with Neumann force  $\int_{\partial\Omega_N^h} (\mathbf{t} \cdot \mathbf{v}^h)$ . To simulate the pull we assume traction vector  $\mathbf{t} = [t_x, t_y] = [10^9, 0]$  acting on the non clamped right end of the bar, i.e., force in  $x$  direction is  $10^9$  units. The same problem from previous tutorials 1 and 2 is used here, a bar 5 m in length and 1 m in width, and is supposed to be made up of a material with density  $\rho = 8 \times 10^3$ , Young's modulus  $E = 200 \times 10^9$ , and Poisson's ratio  $\nu = 0.3$ . Here is how PSD simulation of this case can be performed.

## Step 1: Preprocessing

First step in a PSD simulation is PSD preprocessing, at this step you tell PSD what kind of physics, boundary conditions, approximations, mesh, etc are you expecting to solve.

In the terminal `cd` to the folder `/home/PSD-tutorials/linear-elasticity`. Launch `PSD_PreProcess` from the terminal, to do so run the following command.

```
1 PSD_PreProcess -problem linear-elasticity -dimension 2 -dirichletconditions 1 -tractionconditions 1 \
2 -dirichletpointconditions 1 -postprocess u
```

Additional flag `-dirichletpointconditions 1` now appears, this notifies to PSD that there is one Dirichlet point boundary condition. Edit the `ControlParameters.edp` to communicate the desired point boundary conditions, set the variables `Pbc0Ux 0.` and `Pbc0Uy 0.` to specify  $u_x = 0, u_y = 0$ , and variable `PbcCord = [[ 0. , 0. ]]` to specify the point coordinates  $(x, y) = (0, 0)$ . Via the flags we specified that `-dirichletconditions 1`, i.e., there is one Dirichlet border. To provide the Dirichlet condition ( $u_x = 0$ ) set the variables `Dbc0On 2` and `Dbc0Ux 0.` in `ControlParameters.edp`. PSD understands that 4 is the mesh border label on which Dirichlet is applied and ( $u_x = 0$ ) is the condition to be applied.

## Step 2: Solving

Let us now use 6 cores to solve this problem. To do so enter the following command:

```
1 PSD_Solve -np 6 Main.edp -mesh ../Meshes/2D/bar.msh -v 0
```

Notice, that this is the exact same command used in solving the previous bar problems from other sections, with only difference that we now use `-np 6`.

Note that for this simple problem, the bar mesh (`bar.msh`) has been provided in `../Meshes/2D/` folder, this mesh is a triangular mesh produced with Gmsh. Moreover detailing meshing procedure is not the propose of PSD tutorials. A user has the choice of performing their own meshing step and providing them to PSD in `.msh`<sup>1</sup> or `.mesh` format, we recommend using Salome or Gmsh meshers for creating your own geometry and meshing them.

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<sup>1</sup>Please use version 2

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### Step 3: Postprocessing

Launch ParaView and have a look at the `.pvd` file in the `PSD/Solver/VTUs_DATE_TIME` folder.



Figure 1: 2D bar results. Partitioned mesh (left) and 100X warped displacement field (right).

Note now in fig. 1 there are six subdomains in the partitioned mesh. As expected, we see that the right and the left end of the bar which is being pulled now contract in  $y$  direction, and the bar elongates in  $x$  direction.