

# Linear Elasticity Tutorials

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## Abstract

This document details some tutorials of ‘linear elasticity’ module of PSD. These tutorials are not verbose, but does instead give a kick start to users/developers for using PSD’s ‘linear elasticity’ module.

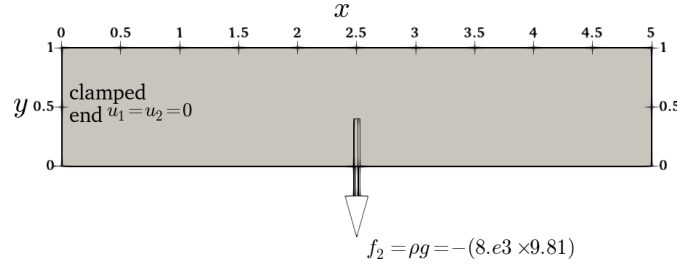


Figure 1: The 2D clamped bar problem.

## Parallel 2D linear-elasticity

The problem of interest is a single Dirichlet condition (clamped end 2D bar) and body force source term (see, figure~1). Additionally postprocessing is demanded for displacement  $u$ .

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u
```

We solve the problem using four MPI processes, with the given mesh file [bar.msh](#).

```
1 PSD_Solve -np 4 Main.edp -mesh ../Meshes/2D/bar.msh -v 0
```

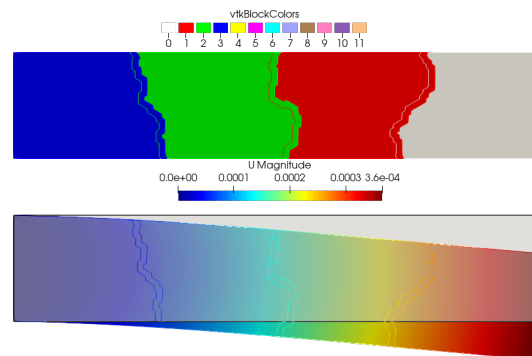


Figure 2: The 2D clamped bar problem: partitioned mesh and displacement field visualization in ParaView.

Using ParaView for postprocessing the results that are provided in the [VTUs...](#) folder, results such as those shown in figure~2 can be extracted.

## Parallel 3D linear-elasticity

The problem of interest is a single Dirichlet condition (clamped end 3D bar) and body force source term. Additionally postprocessing is demanded for displacement  $u$ .

```
1 PSD_PreProcess -problem linear_elasticity -dimension 3 -bodyforceconditions 1 \
2 -dirichletconditions 1 -postprocess u
```

We solve the problem using four MPI processes, with the given mesh file [bar.msh](#).

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/3D/bar.msh -v 0
```

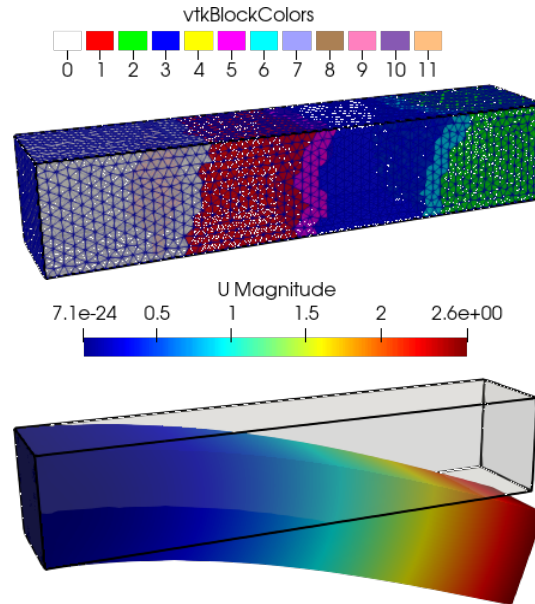


Figure 3: The 3D clamped bar problem: partitioned mesh and displacement field visualization in ParaView.

Using ParaView for postprocessing the results that are provided in the [VTUs...](#) folder, results such as those shown in figure~3 can be extracted.

## Sequential problems

To the same problems above Add `-sequential` flag to [PSD\\_PreProcess](#) for sequential solver, but remember to use [PSD\\_Solve\\_Seq](#) instead of [PSD\\_Solve](#). So the work flow for the 2D problem would be:

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \
2 -dirichletconditions 1 -postprocess u -sequential
```

We solve the problem using the given mesh file [bar.msh](#).

```
1 PSD_Solve_Seq Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```

Similarly try out the 3D problem as well.

## Comparing CPU time

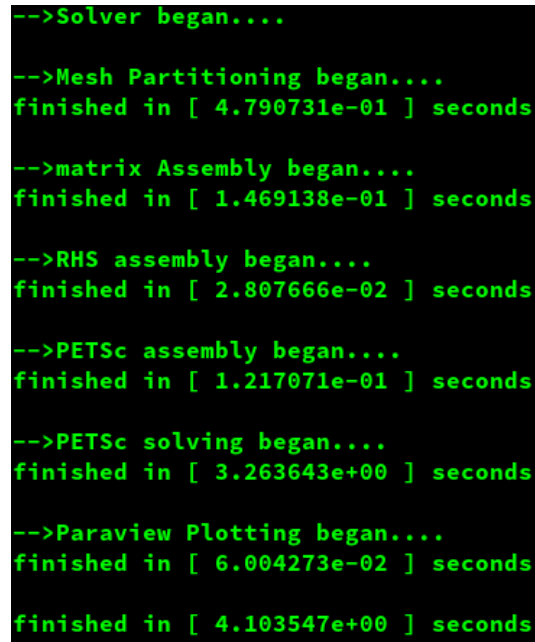
PSD provides mean to time log your solver via `-timelog` flag. What this will do when you run your solver, on the terminal you will have information printed on what is the amount of time taken by each step of your solver. Warning, this will make your solver slower, as this action involves ‘MPI\_Barrier’ routines for correctly timing operation.

An example work flow of 2D solver with timelogging:

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog
```

We solve the problem using four MPI processes, with the given mesh file [bar.msh](#).

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```



```
-->Solver began....  
  
-->Mesh Partitioning began....  
finished in [ 4.790731e-01 ] seconds  
  
-->matrix Assembly began....  
finished in [ 1.469138e-01 ] seconds  
  
-->RHS assembly began....  
finished in [ 2.807666e-02 ] seconds  
  
-->PETSc assembly began....  
finished in [ 1.217071e-01 ] seconds  
  
-->PETSc solving began....  
finished in [ 3.263643e+00 ] seconds  
  
-->Paraview Plotting began....  
finished in [ 6.004273e-02 ] seconds  
  
finished in [ 4.103547e+00 ] seconds
```

Figure 4: Time logging output produced for parallel run on 4 processes.

The figure~4 shows the time logging output produced for parallel run on 4 processes using `-timelog` flag. Take note of timings produced for different operations of the solver.

## Exercise 1

There is a solver run level flag for mesh refinement <sup>1</sup>. This flag is called `-split [int]` which splits the triangles (resp. tetrahedrons) of your mesh into four smaller triangles (resp. tetrahedrons). As such `-split 2` will produce a mesh with 4 times the elements of the input mesh. Similarly, `-split n` where  $n$  is a positive integer produces  $2^n$  times more elements than the input mesh. You are encouraged to use this `-split` flag to produce refined meshes and check, mesh convergence of a problem, computational time, etc. Use of parallel computing is recommended. You could try it out with `PSD_Solve` or `PSD_Solve_Seq`, for example:

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0 -split 2
```

for splitting each triangle of the mesh [bar.msh](#) into 4.

## Exercise 2

There is a preprocess level flag `-debug`, which as the name suggests should be used for debug proposes by developers. However, this flag will activate OpenGL live visualization of the problems displacement field. You are encouraged to try it out

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<sup>1</sup>Mesh refinement is performed after partitioning.

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog -debug
```

Then to run the problem we need traditional `-wg` flag

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0 -wg
```

## Exercise 3

One interesting way of solving a linear Elasticity problem is to solve it via a pseudo nonlinear model. There is a preprocess level flag `-model pseudo_nonlinear`, which introduces pseudo nonlinearity into the finite element variational formulation of linear elasticity. You are encouraged to use this flag and see how the solver performs.

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog -model pseudo_nonlinear
```

Then to run the problem we need additional `-wg` flag

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```

To understand what the flag does, try to find out the difference between the files created by `PSD_PreProcess` when used with and without `-model pseudo_nonlinear` flag. Especially, compare `LinearFormBuilderAndSolver.edp` and `VariationalFormulations.edp` files produced by `PSD_PreProcess` step. You will see Newton–Raphsons iterations are performed for solving the linear problem. However, the nonlinear iterations loop converges very rapidly (in 1 iteration) due to linear nature of the problem. **Note:** This flag is exclusive for parallel solver.

## Exercise 4

There is a preprocess level flag `-withmaterialtensor`, which introduces the full material tensor into the finite element variational formulation. You are encouraged to use this flag and see how the solver performs.

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog -withmaterialtensor
```

Then to run the problem we need additional `-wg` flag

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```

To understand what the flag does, try to find out the difference between the files created by `PSD_PreProcess` when used with and without `-withmaterialtensor` flag. Especially, compare `FemParameters.edp`, `MeshAndFeSpace` and `VariationalFormulations.edp` files produced by `PSD_PreProcess` step.

## Exercise 5

PSD has also been interfaced with MFront material library, this library (MFront) provides users with multiple linear/non-linear mechanical laws (behaviours) and one can profit from this opensource DSL. There is a preprocess level flag `-useMfront`, which in the case of linear-elasticity will introduces the full material tensor into the finite element variational formulation and this material tensor will be built using MFront library. You are encouraged to use this flag and see how the solver performs.

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog -useMfront
```

Then to run the problem we need additional `-wg` flag

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```

To understand what the flag does, try to find out the difference between the files created by [PSD\\_PreProcess](#) when used with and without `-useMfront` flag. Especially, compare [FemParameters.edp](#), [MeshAndFeSpace](#) and [VariationalFormulations.edp](#) files produced by [PSD\\_PreProcess](#) step.

One can also use the Mfront interface with the pseudo-nonlinear model for solving elasticity. In this case Mfront will be in charge of building the Material tensor (stiffness matrix) and the stress tensor in previous nonlinear iterate. To realise this case:

```
1 PSD_PreProcess -problem linear_elasticity -dimension 2 -bodyforceconditions 1 \  
2 -dirichletconditions 1 -postprocess u -timelog -useMfront -model pseudo_nonlinear
```

Then to run the problem we need additional `-wg` flag

```
1 PSD_Solve -np 4 Main.edp -mesh ../../Meshes/2D/bar.msh -v 0
```

To understand what the flag does, try to find out the difference between the files created by [PSD\\_PreProcess](#) when used with and without `-useMfront` flag. Especially, compare [FemParameters.edp](#), [LinearFormBuilderAndSolver.edp](#), [MeshAndFeSpace](#) and [VariationalFormulations.edp](#) files produced by [PSD\\_PreProcess](#) step.