# **Linear Elasticity Tutorial 2:**

To showcase the usage of Linear elasticity, we shall discuss here an example of a 2D bar, which bends under its own load. The bar  $5\times 1~\text{m}^2$  in area is made up of material with  $~\rho=8\times 10^3$ ,  $E=200\times 10^9$ , and  $\nu=0.3$ . Contrary to tutorial 1, now both ends of the bar are clamped.

### **Step 1: Preprocessing**

First step in a PSD simulation is PSD preprocessing, at this step you tell PSD what kind of physics, boundary conditions, approximations, mesh, etc are you expecting to solve.

In the terminal cd to the folder \home\PSD-tutorials\linear-elasticity . Launch PSD\_PreProcess from the terminal, to do so run the following command.

```
PSD_PreProcess -problem linear-elasticity -dimension 2 -bodyforceconditions 1 \backslash -dirichlet
conditions 2 -postprocess u
```

After the PSD\_PreProcess runs successfully you should see many .edp files in your current folder.

What do the arguments mean? -problem linear-elasticity means that we are solving linear elasticity problem, -dimension 2 means it is a 2D simulation, -bodyforceconditions 1 with body force; -dirichletconditions 2 says we have two Dirichlet border; and -postprocess u means we would like to have ParaView post processing files.

Since basic nature of both the problems (the one from tutorial 1 and 2) is same the almost the same command for preprocessing used in previous tutorial 1 is used here. The only difference,is that an additional Dirichlet condition needs to be supplied, notified to PSD by dirichletconditions 2. To provide Dirichlet conditions of the left clamped end ( $u_x = u_y = 0$ ) in ControlParameters.edp set Dbc00n 2, Dbc0Ux 0., and Dbc0Uy 0. Similarly, for the right end set variables Dbc10n 4, Dbc1Ux 0., and Dbc1Uy 0. Each one of these is a clamped border respectively labeled as 2 (Dbc00n 2) and 4 (Dbc10n 4) in the mesh .../Meshes/2D/bar.msh.

Just like the previous tutorial the input properties  $E, \nu$  should be mentioned in <code>ControlParameters.edp</code>, use <code>E = 200.e9</code>, and <code>nu = 0.3</code>; . The volumetric body force condition is mentioned in the same file via variable <code>Fbc0Fy -78480.0</code>, i.e (  $\rho*g=8.e3*(-9.81)=-78480.0$ ). One can also provide the mesh to be used in <code>ControlParameters.edp</code>, via <code>ThName = "../Meshes/2D/bar.msh"</code> (note that mesh can also be provided in the next step) .In addition variable <code>Fbc00n 1</code> has to be provided in order to indicate the volume (region) for which the body force is acting, here <code>1</code> is the integer volume tag of the mesh.

## Step 2: Solving

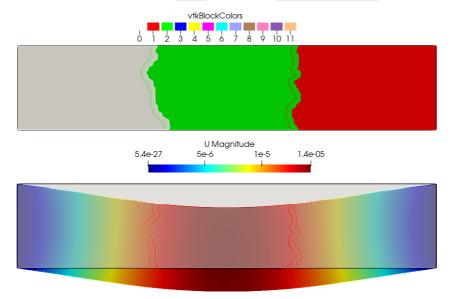
As PSD is a parallel solver, let us use 3 parallel processes to solve this 2D bar case. To do so enter the following command:

```
PSD_Solve -np 3 Main.edp -mesh ./../Meshes/2D/bar.msh -v 0
```

Here -np 3 denote the argument used to enter the number of parallel processes (MPI processes) used while solving. -mesh ./../Meshes/2D/bar.msh is used to provide the mesh file to the solver.
-v 0 denotes the verbosity level on screen. PSD\_Solve is a wrapper around FreeFem++ or FreeFem++-mpi. Note that if your problem is large use more cores. PSD has been tested upto 13,000 parallel processes and problem sizes with billions of unknowns, surely you will now need that many for the 2D bar problem.

### **Step 3: Postprocessing**

PSD allows postprocessing of results in ParaView. After the step 2 mentioned above finishes. Launch ParaView and have a look at the pvd file in the VTUs\_DATE\_TIME folder.



You are all done with your 2D linear-elasticty simulation.

# What else should you try to become an advanced user

- Try running the 3D problem. Keep in mind to rerun the PSD\_PreProcess with -dimension 3 flag and using the approprite mesh via -mesh flag with -PSD\_Solve . It goes without saying you will need to adjust the direchlet border lables in ControlParameters.edp.
- Since gravity is the main force involved in the problem, try redoing the test with diffrent graviational constant. Imagine, you wish to know how the test would compare if performed on Moon and Jupiter. The only thing that will change now is the gravitational pull, for Moon g=1.32 and for Jupiter g=24.79. To perform the moon test simply change <code>Fbc0Fy-10560.0</code> in <code>ControlParameters.edp</code> and redo step 2 and step 3. Similarly, for the Jupiter test <code>Fbc0Fy-198320.0</code> in <code>ControlParameters.edp</code> and redo step 2 and step 3.
- Optionally try using -withmaterialtensor flag with PSD\_PreProcess, and run the simulation. You are encouraged to have a look at ControlParameters.edp and VariationalFormulations.edp file produced with -withmaterialtensor flag and without this flag.
- Add -sequential flag to PSD\_PreProcess for sequential solver, but remember to use PSD\_Solve\_Seq instead of PSD\_Solve and no -np flag.

```
PSD_PreProcess -problem linear-elasticity -dimension 2 -sequential \
-bodyforceconditions 1 -dirichletconditions 2 -postprocess u
```

```
PSD_Solve_Seq Main.edp -mesh ./../Meshes/2D/bar.msh -v 0
```

- You are encouraged to time your the PSD solver and see if you have considerable gains when using more processes in parallel PSD or when comparing a a sequential solver with a parallel one. To time the solver use -timelog flag during PSD\_PreProcess.
- You are encouraged to use more complex meshes for this same problem, but do not forget to update the ControlParameters.edp file.