Math 312, Extra Credit Problems

These problems are hard and interesting. The solutions should be presents orally before April 14. It might improve your score, but should be used for fun. Only the first solution will be graded.

1. Show that the field of all numbers of the form $a + b\sqrt{2}$ for $a, b \in \mathbb{Q}$ admits a nonstandard ordering (that is, not the one comming from the standard ordering of real numbers).