Lesson 8: Quadratic Equations Mix

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Read all the problems before starting to solve any!

Problem 1.

s Prove that if b is any real number and $a \neq 0$, then the quadratic equation $ax^2 + bx - a = 0$ has two distinct real roots.

Problem 2.

 $f(x) = x^2 + px + q$ is an even function. Find (with proof) the value of p.

Problem 3.

Points A, B, C lie on a circle of radius r, and AC = r. Find $\angle ABC$. Hint: Is there only one solution?

Problem 4.

- a) Find p and q, if 10 and -15 are the roots of the quadratic equation $x^2 + px + q$.
- b) Sum of squares of roots of a quadratic equation $x^2 + px 3$ is equal to 10. Find p.

Problem 5.

- a) What is the minimum value of the function $f(x) = x^2 + 10x 13$?
- **b)** What is its maximum value?

Problem 6.

Let O be the center of a circle and A be a point outside of it. Let AM and AN be tangents to the circle, and let B be the intersection of line AO with the circle furthest from A. Given that $AN \parallel BM$, find $\angle OAM$ and prove that AMBN is a rhombus.