# Lesson 8: Quadratic Equations Mix

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Read all the problems before starting to solve any!

#### Problem 1.

s Prove that if b is any real number and  $a \neq 0$ , then the quadratic equation  $ax^2 + bx - a = 0$  has two distinct real roots.

#### Problem 2.

 $f(x) = x^2 + px + q$  is an even function. Find (with proof) the value of p.

#### Problem 3.

Points A, B, C lie on a circle of radius r, and AC = r. Find  $\angle ABC$ . Hint: Is there only one solution?

#### Problem 4.

- a) Find p and q, if 10 and -15 are the roots of the quadratic equation  $x^2 + px + q$ .
- b) Sum of squares of roots of a quadratic equation  $x^2 + px 3$  is equal to 10. Find p.

## Problem 5.

- a) What is the minimum value of the function  $f(x) = x^2 + 10x 13$ ?
- **b)** What is its maximum value?

#### Problem 6.

Let O be the center of a circle and A be a point outside of it. Let AM and AN be tangents to the circle, and let B be the intersection of line AO with the circle furthest from A. Given that  $AN \parallel BM$ , find  $\angle OAM$  and prove that AMBN is a rhombus.