

Let T be a linear transformation $T : V \longrightarrow V$

- (1) Suppose T is invertible. Show that $(\bar{T})^{-1} = \bar{T}^{-1}$.
- (2) Suppose T is W -invariant for some subspace W . Show that T^t is W^0 -invariant.

Let S be a linear transformation $S : V \longrightarrow W$

- (1) Show that if S is injective then S^t is surjective.
- (2) Show that $\ker T^t = (\operatorname{im} T)^0$.