

# A Tiny Example

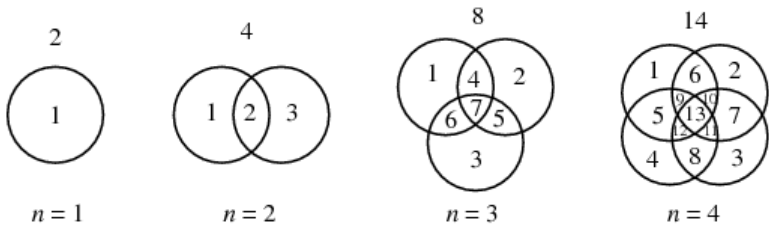
Andrew Mertz and William Slough

June 15, 2005

Suppose we have an (infinite) collection of sets  $\mathcal{F}$ .  
We define a shatter function  $\pi_{\mathcal{F}}(n)$

$$\pi_{\mathcal{F}}(n) = \max\{\# \text{ of atoms in boolean algebra generated by } S \\ | S \subset \mathcal{F} \text{ with } |S| = n\}$$

Example: Let  $\mathcal{F}$  consist of all discs on a plane.



$$\pi_{\mathcal{F}}(1) = 2 \quad \pi_{\mathcal{F}}(2) = 4 \quad \pi_{\mathcal{F}}(3) = 8 \quad \pi_{\mathcal{F}}(4) = 14$$