2.1) 
$$2^{2^{N}} = > 2^{2^{3}} = 256$$

2.2)  $k = 0 = > 1$   $k = 8 = > 1$   $sum = 2$ 
 $k = 1 \Rightarrow 8$   $k = 7 = > 8$   $sum = 2 + 16 = 18$ 
 $k = 1 \Rightarrow 8$   $k = 7 \Rightarrow 8$   $sum = 18 + 12 = 30$ 
 $k = 6$  same as  $k = 1 \Rightarrow 1$   $sum = 30 + 12 \Rightarrow 41$ 
 $k = 3 \Rightarrow 1$   $sum = 42 + 24 \Rightarrow 66$ 
 $k = 5$  same as  $k = 3 \Rightarrow 2\pi$   $sum = 66 + 2\pi = 90$ 
 $k = 4$ 
 $sum = 90 + 6 + 8 \Rightarrow 100$ 

```
TargetC = [1, 1, 1, 1, 1, 1, 1, -1, 1, 1, -1, -1, 1, 1, -1, 1];
TargetD = [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, -1, 1, 1, 1, 1, 1];
TargetF = [1, -1, 1, 1, 1, -1, 1, 1, 1, 1, 1, 1, -1, 1, 1, 1];
target = TargetF; %I just change this
inputs = readmatrix('input_data_numeric.csv');
%initiate random weights and threshold
xmin = -0.2;
xmax = 0.2;
numOfInputs=4;
w = xmin+rand(1,numOfInputs)*(xmax-xmin);
threshold = -1 + rand(1,1)*(2);
%____
n = 0.02;
outputs = zeros(16,1);
for i = 1:100000
   u = randi(16);
   in = inputs(u, 2:5);
   %Feed in
   in = in';
   Bi = (w*in)-threshold;
   outputs(u) = tanh((1/2)*Bi);
   %Update
   derBi = ( (sech(Bi/2))^2) * (1/2);
   weightedError = (target(u) - outputs(u))*derBi;
   inTmp = in';
   deltaW = n*weightedError*inTmp;
   w = w + deltaW;
   %Check outputs
   if(mod(i,16) == 0)
      tmpOutputs = outputs';
      for u2 = 1:16
          if tmpOutputs(u2) >= 0
             tmpOutputs(u2) = 1;
          else
             tmpOutputs(u2) = -1;
          end
      end
      if target == tmpOutputs
          disp("SUCCESS!");
```

break; end end

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```
%---- THIS IS MAIN, BELOW IS ALL FUNCTONS. IN REALITY THEY ARE
 SEPARATE M-FILES!!
trainingSet = csvread("training_set.csv");
targetOuts = trainingSet(:,3);
v1 size = 8;
v2 \text{ size} = 6;
n = 0.02;
outThreshold = 0;
v1 thresholds = zeros(v1 size,1);
v2_thresholds = zeros(v2_size,1);
wjk = randn(v1_size,2); %first
wij = randn(v2_size,v1_size); %second
wOut = randn(1, v2_size); %out
allXs = trainingSet(:,1:2);
for i = 1:1000000 %10000
     randIndx = randi([1 10000],1,1);
    %---- FORWARD PROP-----
    xs = allXs(randIndx,:);
    xs = xs';
    local_v1 = (wjk*xs) - v1_thresholds;
    v1 = tanh(local_v1);
    local_v2 = (wij*v1) - v2_thresholds;
    v2 = tanh(local_v2);
    local_out = (wOut*v2) - outThreshold;
    out = tanh(local_out);
    %---- ERROR BACKPROP----
    %error acc with outputlayer
    outError = OutputError(targetOuts(randIndx),out,local_out);
    outError;
    %error acc with v2
    v2Error = ((wOut') * outError) .* (1-((tanh(local_v2).^2)));
    v2Error;
    %error acc with v1
    v1Error = ((wij') * v2Error) .* (1-((tanh(local_v1).^2)));
    v1Error;
```

```
%----UPDATE WEIGHTS-----
    wjk = wjk + (n* v1Error * (xs'));
    wij = wij + (n * v2Error * (v1'));
    wOut = wOut + (n*outError * (v2'));
    %----UPDATE THRESHOLDS----
    v1_thresholds = v1_thresholds + -(n*v1Error);
    v2_thresholds = v2_thresholds + -(n*v2Error);
    outThreshold = outThreshold + -(n*outError);
end
%----Compute C -----
validationSet = csvread("validation_set.csv");
allValXs = validationSet(:,1:2);
validationTargets = validationSet(:,3);
valIters = size(validationTargets,1);
realOs = zeros(valIters,1);
for i = 1:valIters
    valXs = allValXs(i,:);
    valXs = valXs';
    v1B = LocalFieldB(v1 thresholds, wjk, valXs, v1 size);
    v1 = tanh(v1B);
    v2B = LocalFieldB(v2_thresholds, wij, v1, v2_size);
    v2 = tanh(v2B);
    outB = OutputB(outThreshold, wOut, v2);
    out = tanh(outB);
    realOs(i) = out;
end
C = ClassificationError(realOs, validationTargets, valIters);
csvwrite('w1.csv',wjk);
csvwrite('w2.csv',wij);
csvwrite('w3.csv',wOut);
csvwrite('t1.csv',v1_thresholds);
csvwrite('t2.csv',v2_thresholds);
csvwrite('t3.csv',outThreshold);
%----- END OF MAIN, FOLLOWING ARE FUNCTIONS------
function c = ClassificationError(os, ts,u)
errors = 0;
```

```
% os
signedOs = zeros(u,1);
   for i = 1:u
       o = os(i);
       if o >= 0
           0 = 1;
       else
           0 = -1;
       end
       signedOs(i) = o;
   end
응
     signed0s
응
   for i = 1:u
       o = signedOs(i);
       t = ts(i);
       if(o \sim = t)
           errors = errors + 1;
       end
   end
   c = errors/u;
end
% -----
function v = LocalFieldB(thresholds, weights, xs, neuronSize)
   v = zeros(neuronSize,1);
   for j = 1:neuronSize
       rowWeights = weights(j,:);
       thresJ = thresholds(j);
       vj = -thresJ + (rowWeights*xs);
       v(j) = vj;
   end
end
%-----
function o = OutputB(threshold, weights, v2)
   sum = weights*v2;
   sum = -threshold + sum;
   o = sum;
end
% -----
function delta = OutputError(t,o,b)
   delta = (t-o)*(1-(tanh(b))^2);
end
%----
```

