Conditional Inference Trees & Cox Regression to Predict Heart Failure Survival Time

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https://archive.ics.uci.edu/ml/datasets/Heart+failure+clinical+record (https://archive.ics.uci.edu/ml/datasets/Heart+failure+clinical+record

• All 299 patients had left ventricular systolic dysfunction

Initial Variables:

- age: age of the patient (years)
- anaemia: decrease of red blood cells or hemoglobin since last measure (boolean)
- high blood pressure: if the patient has hypertension (boolean)
- creatinine phosphokinase (CPK): level of the CPK enzyme in the blood (mcg/L)
- diabetes: if the patient has diabetes (boolean)
- ejection fraction: percentage of blood leaving the heart at each contraction (percentage)
- · platelets: platelets in the blood (kiloplatelets/mL)
- sex: woman or man (binary)
- · serum creatinine: level of serum creatinine in the blood (mg/dL)
- · serum sodium: level of serum sodium in the blood (mEq/L)
- smoking: if the patient smokes or not (boolean)
- · time: follow-up period (days)
- [target] death event: if the patient deceased during the follow-up period (boolean)

```
library(skimr)
library(ggplot2)
library(dplyr)
library(survival)
library(survminer)
library(partykit)
library(coin)
library(survminer)
library(survminer)
library(survminer)
library(survminer)
library(flexsurv)
library(flexsurv)
library(randomForestSRC)
library(gtsummary)
```

Loading in the data

Creating Left Ventricular Ejection Fraction Groups set by Cardiology Experts (https://www.ncbi.nlm.nih.gov/books/NBK459131/). Rounding for averages instead of only using data for men and women.

Data summary

Name	HF
Number of rows	299
Number of columns	14
Column type frequency:	
factor	7
numeric	7
Group variables	None

Variable type: factor

skim_variable	n_missing	complete_rate	ordered	n_unique	top_counts
anaemia	0	1	FALSE	2	0: 170, 1: 129
diabetes	0	1	FALSE	2	Abs: 174, Pre: 125
sex	0	1	FALSE	2	Mal: 194, Fem: 105
smoking	0	1	FALSE	2	0: 203, 1: 96
DEATH_EVENT	0	1	FALSE	2	0: 203, 1: 96
hypertension	0	1	FALSE	2	Abs: 194, Pre: 105
EF_Condition	0	1	FALSE	4	Mod: 126, Sev: 93, Mil: 41, Nor: 39

Variable type: numeric

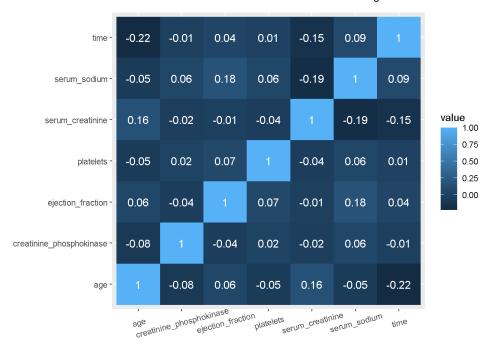
skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100	hist
age	0	1	60.83	11.89	40.0	51.0	60.0	70.0	95.0	
creatinine_phosphokinase	0	1	581.84	970.29	23.0	116.5	250.0	582.0	7861.0	
ejection_fraction	0	1	38.08	11.83	14.0	30.0	38.0	45.0	80.0	_=
platelets	0	1	263358.03	97804.24	25100.0	212500.0	262000.0	303500.0	850000.0	_=_
serum_creatinine	0	1	1.39	1.03	0.5	0.9	1.1	1.4	9.4	
serum_sodium	0	1	136.63	4.41	113.0	134.0	137.0	140.0	148.0	
time	0	1	130.26	77.61	4.0	73.0	115.0	203.0	285.0	

Correlation

Time and Serum_Creatinine have a correlation to Serum_Sodium of 0.15 & 0.19, respectively.

```
cormat <- HF %>% select(where(is.numeric)) %>% cor() %>% round(2)
melted_cormat <- reshape2::melt(cormat)

ggplot(data = melted_cormat, aes(x=Var1, y=Var2, fill=value)) +
    geom_tile() +
    geom_text(aes(Var2, Var1, label = value), color = "white", size = 4) +
    theme(axis.title.x=element_blank(),
        axis.title.y=element_blank(),
        axis.title.y=element_text(angle = 15, vjust = 0.8)
    )</pre>
```



Choosing to grab distributions based on having hypertension- what's traditionally seen as a good indicator of heart failure.

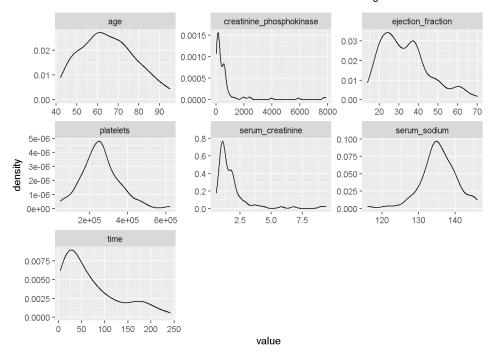
Doing so to look at, specifically, Ejection Fraction right after to see if there is correlation.

```
HF %>% filter(DEATH_EVENT==0) %>%
  purrr::keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
     facet_wrap(~ key, scales = "free") +
     geom_density()
                                                creatinine_phosphokinase
                                                                                      ejection_fraction
                     age
    0.03
                                      0.0015 -
                                                                          0.04
                                      0.0010 -
    0.02
                                                                          0.02
    0.01
                                      0.0005
    0.00
                                      0.0000
                                                                          0.00
         40
              50
                   60
                        70
                             80
                                  90
                                             ò
                                                 1000 2000 3000 4000 5000
                                                                                20
                                                                                                60
                                                                                        40
                                                                                                         80
                   platelets
                                                                                       serum_sodium
                                                    serum_creatinine
                                         1.5 -
                                                                          0.12
  6e-06
density
                                         1.0 -
                                                                          0.08
  4e-06
  2e-06
                                         0.5
                                                                          0.04 -
  0e+00
                                         0.0 -
                                                                          0.00
       0e+00 2e+05 4e+05 6e+05 8e+05
                                                                                    120
                                                                                           130
                                                                                                  140
                     time
   0.006
  0.004
   0.002
   0.000 -
                 100
                          200
                                                       value
HF %>% filter(DEATH EVENT==1) %>%
  purrr::keep(is.numeric) %>%
```

gather() %>%
ggplot(aes(value)) +

geom_density()

facet_wrap(~ key, scales = "free") +

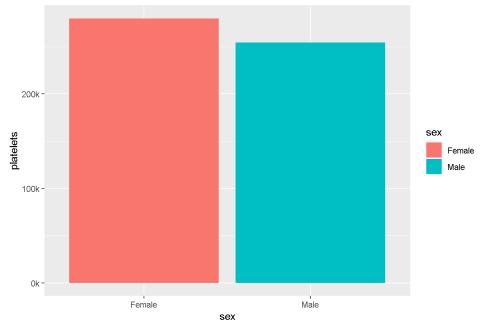


Comparing creatinine_phosphokinase to Men & Women— those who smoke and those who do not.

• Noticing that the average creatinine_phosphokinase is higher for non-smokers.

```
ggplot(HF, aes(x=sex, y=platelets, fill=sex)) +
  geom_bar(position = "dodge", stat="summary", fun="mean") +
  scale_y_continuous(labels = scales::label_number(suffix = "k", scale = 1e-3)) +
  ggtitle("Mean Platelets for Sexes")
```

Mean Platelets for Sexes



```
HF %>% group_by(sex, DEATH_EVENT) %>%
summarize(count = n(), .groups="drop")
```

```
## # A tibble: 4 × 3

## sex DEATH_EVENT count

## <fct> <fct> <int>
## 1 Female 0 71

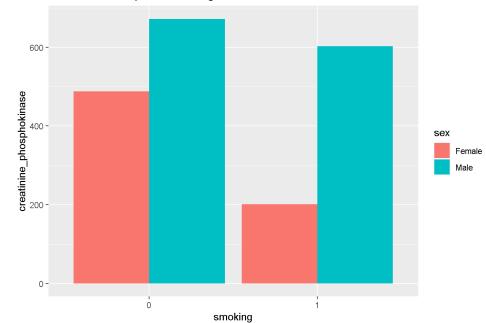
## 2 Female 1 34

## 3 Male 0 132

## 4 Male 1 62
```

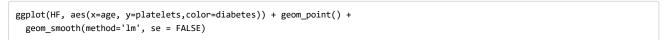
```
ggplot(HF, aes(x=smoking, y=creatinine_phosphokinase, fill=sex)) +
geom_bar(position = "dodge", stat="summary", fun="mean") +
ggtitle("Creatinine Phosphokinase Avg on Smokers & Non-Smokers")
```

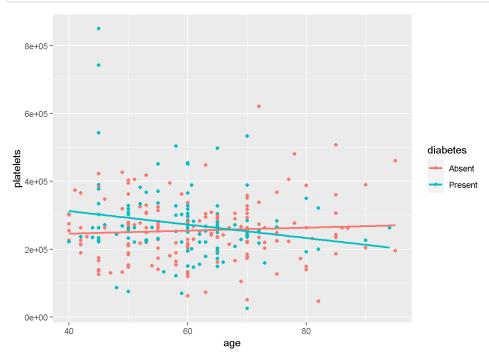
Creatinine Phosphokinase Avg on Smokers & Non-Smokers



- · Finding out that for those diabetic, plateletes reduce as age increases.
- · For those who aren't diabetic, plateletes generally stay the same and potentially, increase by a marginal amount.

Plateletes are incredibly important. Having too few plateletes can lead to internal bleeding in intestines or stroke.

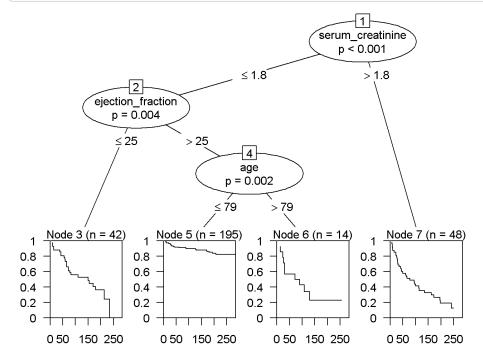




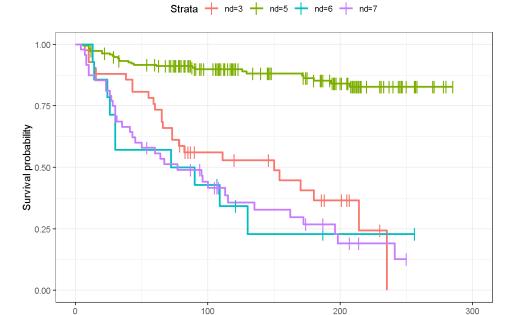
Conditional Inference Trees - Kaplan Maeier Curves

We can see we have remaining cases in which the person did was not declared deceased due to the ending of the curve not dropping down to n%

Insights from this graph include: * Serum Creatinine is highly significant with the showcased split at 1.8 for survival prediction.



Plotting all node distributions/curves in one plot.



Time

EXTRACTING SURVIVAL CURVE FOR ONLY ONE OBSERVATION/PERSON FROM THE CTREE! PULL OUT AT LEAST ONE INSIGHT. THE 'X' DETERMINES WHICH OBSERVATION YOU'LL LOOK AT. PERHAPS LOOK AT AN OUTLIER TO TALK ABOUT A SPECIAL CASE.

```
#nd1 <- predict(CondInfTree, type = "prob")[[X]]
#summary(nd1, times=c(20, 45, 60, 80, 100, 10*(11:15)))
```

Constructing an exponential curve for previous graph's second node. * 24% probability of survival after t=130 days for patients older than 79, that have less than or equal to 1.8 in serum creatine, and an ejection fraction over 25.

```
K <- HF %>%
  filter(serum_creatinine <= 1.8, ejection_fraction > 25, age > 79)

# This one is best.
# The ~ 1 is our way ofletting R know that we aren't using any x variables. Just time and whether event occured which are both y variabes.
pred_k_surv <- survfit(Surv(time, DEATH_EVENT) ~ 1, data = K)
summary(pred_k_surv, times=c(20, 45, 60, 80, 100, 10*(11:15)))</pre>
```

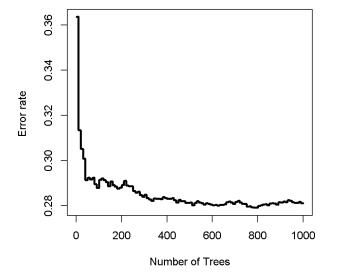
```
## Call: survfit(formula = Surv(time, DEATH_EVENT) ~ 1, data = K)
##
##
   time n.risk n.event survival std.err lower 95% CI upper 95% CI
##
     20
            12
                     2
                          0.857 0.0935
                                              0.6921
                                                           1.000
##
     45
             8
                     4
                          0.571 0.1323
                                              0.3630
                                                           0.899
##
     60
             8
                     0
                          0.571 0.1323
                                             0.3630
                                                           0.899
##
     80
             7
                          0.500 0.1336
                                             0.2961
                                                           0.844
                     1
##
    100
                          0.429 0.1323
                                              0.2341
                                                           0.785
             6
                     1
                                                           0.724
##
    110
                          0.343 0.1307
                                              0.1624
##
    120
             4
                     0
                          0.343 0.1307
                                              0.1624
                                                           0.724
##
    130
             3
                                              0.0765
                                                           0.683
                     1
                          0.229 0.1277
##
             2
                     0
                          0.229 0.1277
                                              0.0765
                                                           0.683
    140
                                              0.0765
                                                           0.683
    150
                          0.229 0.1277
```

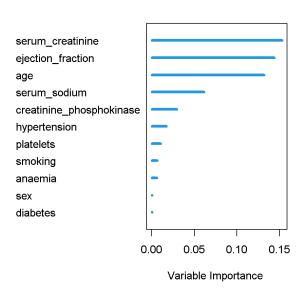
- No pruning was done since most trees found revolve around the same 3 variables.
- Probability of survival after 150 days for those younger than 70 is 77%.
- Probability of survival after 200 days for those younger than 70 is 70%.

```
survfit(Surv(time, DEATH_EVENT) ~ 1, data = HF %>% filter(age <= 70)) %>%
tbl_survfit(
  times = c(150,200),
  label_header = "**{time} Day Survival (95% CI) For Those Younger Than 70**"
)
```

Characteristic	150 Day Survival (95% CI) For Those Younger Than 70	200 Day Survival (95% CI) For Those Younger Than 70
Overall	77% (71%, 82%)	70% (64%, 77%)

Random Forest Survival





```
##
##
                                            Relative Imp
                              Importance
## serum_creatinine
                                   0.1527
                                                  1.0000
## ejection_fraction
                                   0.1435
                                                  0.9399
                                   0.1319
                                                  0.8635
## serum_sodium
                                   0.0614
                                                  0.4020
## creatinine_phosphokinase
                                   0.0295
                                                  0.1929
## hypertension
                                   0.0170
                                                  0.1112
## platelets
                                   0.0103
                                                  0.0674
## smoking
                                                  0.0404
                                   0.0062
                                   0.0059
                                                  0.0385
## anaemia
                                   0.0002
                                                  0.0014
## sex
## diabetes
                                   0.0001
                                                  0.0006
```

Cox Proportional Hazards Model (Cox Regression)

KM will make the curve based on event & time but that's all. We need to include the rest of the variables.

- At a given instance in time, someone who has hypertension is 0.42 times as likely to die as someone without hypertension adjusting for age.
- At any given instance in time, someone who does not have hypertension is 0.65 times as likely to die as someone who does, adjusting for
 age.
- Concordance: Goodness of fit for survival analysis.

```
# diabetes isn't stat significant.
coxMod1 <- coxph(Surv(time, DEATH_EVENT) ~ diabetes, data=HF)
summary(coxMod1)</pre>
```

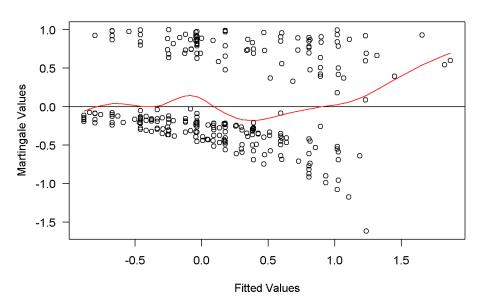
```
## Call:
## coxph(formula = Surv(time, DEATH EVENT) ~ diabetes, data = HF)
##
    n= 299, number of events= 96
##
                    coef exp(coef) se(coef) z Pr(>|z|)
##
## diabetesPresent -0.04184   0.95902   0.20728 -0.202   0.84
##
##
                 exp(coef) exp(-coef) lower .95 upper .95
## diabetesPresent 0.959 1.043 0.6388
##
## Concordance= 0.502 (se = 0.027 )
## Likelihood ratio test= 0.04 on 1 df, p=0.8
## Wald test = 0.04 on 1 df, p=0.8
## Score (logrank) test = 0.04 on 1 df, p=0.8
```

hypertension useful bc tree didn't output it. i paired it w/ age bc why not? historia mejor.
coxMod2 <- coxph(Surv(time, DEATH_EVENT) ~ hypertension + age, data=HF)
summary(coxMod2)</pre>

```
## coxph(formula = Surv(time, DEATH_EVENT) ~ hypertension + age,
##
      data = HF)
##
##
   n= 299, number of events= 96
##
##
                        coef exp(coef) se(coef)
                                                 z Pr(>|z|)
## hypertensionPresent 0.417717 1.518491 0.209708 1.992 0.0464 *
                   0.042424 1.043336 0.008693 4.880 1.06e-06 ***
## age
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
                    exp(coef) exp(-coef) lower .95 upper .95
## hypertensionPresent 1.518 0.6585 1.007
                                                     2.290
## age
                        1.043
                                  0.9585
                                           1.026
                                                     1.061
##
## Concordance= 0.638 (se = 0.031 )
## Likelihood ratio test= 27.36 on 2 df, p=1e-06
## Wald test = 27.52 on 2 df, p=1e-06
## Score (logrank) test = 28.25 on 2 df, p=7e-07
```

```
# so long as most part of red doesn't stray, it's linear. This one strays a lot at end bc of less values overall so they hold m
ore weight.
plot(predict(coxMod2), residuals(coxMod2, type = "martingale"), xlab = "Fitted Values",
    ylab = "Martingale Values", main = "Residual Plot", las = 1) +
abline(h=0) +
lines(smooth.spline(predict(coxMod2), residuals(coxMod2, type="martingale")), col="red")
```

Residual Plot



```
## integer(0)
# Do the Likelihood-Ratio Test
# Try to find combination that may be insightful and make them "oh? interesting".
anova(coxMod1, coxMod2, test = "LRT")
## Analysis of Deviance Table
   Cox model: response is Surv(time, DEATH_EVENT)
   Model 1: ~ diabetes
   Model 2: ~ hypertension + age
##
##
     loglik Chisq Df P(>|Chi|)
## 1 -509.18
## 2 -495.52 27.322 1 1.722e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# keep only variables that are significant. do manual stepwise, basically, and see what u get.
# boom, found it.
summary(coxph(Surv(time, DEATH_EVENT) ~ ., data=HF))
```

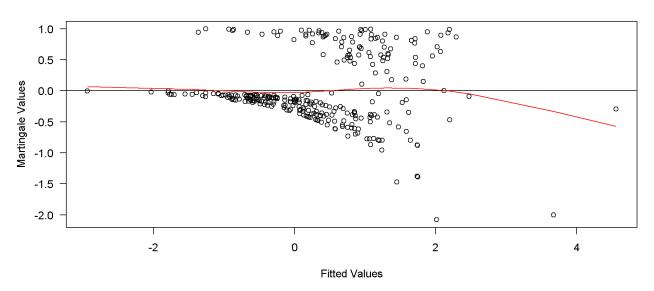
```
## coxph(formula = Surv(time, DEATH_EVENT) ~ ., data = HF)
##
##
    n= 299, number of events= 96
##
##
                                coef exp(coef) se(coef)
                                                             z Pr(>|z|)
                           4.641e-02 1.048e+00 9.324e-03 4.977 6.45e-07 ***
## age
## anaemia1
                          4.601e-01 1.584e+00 2.168e-01 2.122 0.0338 *
## creatinine phosphokinase 2.207e-04 1.000e+00 9.919e-05 2.225 0.0260 *
## diabetesPresent 1.399e-01 1.150e+00 2.231e-01 0.627 0.5307
                         -4.894e-02 9.522e-01 1.048e-02 -4.672 2.98e-06 ***
## ejection_fraction
                       -4.635e-07 1.000e+00 1.126e-06 -0.412 0.6806
## platelets
## serum_creatinine 3.210e-01 1.379e+00 7.017e-02 4.575 4.76e-06 ***
## serum_sodium -4.419e-02 9.568e-01 2.327e-02 -1.899 0.0575 .
## sexMale
                         -2.375e-01 7.886e-01 2.516e-01 -0.944
                                                                 0.3452
## smoking1
                         1.289e-01 1.138e+00 2.512e-01 0.513 0.6078
## hypertensionPresent
                        4.757e-01 1.609e+00 2.162e-01 2.201 0.0278 *
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
                          exp(coef) exp(-coef) lower .95 upper .95
## age
                            1.0475
                                       0.9547
                                                1.0285
                             1.5843
                                       0.6312
                                                1.0358
                                                           2.423
                           1.0002
## creatinine_phosphokinase
                                       0.9998
                                                1,0000
                                                           1,000
## diabetesPresent
                            1.1501 0.8695 0.7427
                                                          1.781
## ejection_fraction
                           0.9522 1.0502 0.9329
                                                          0.972
## platelets
                           1.0000 1.0000 1.0000
## serum_creatinine
                          1.3786
                                       0.7254 1.2014
                                                        1.582
                            0.9568 1.0452 0.9141
## serum_sodium
                                                          1,001
                                      1.2681
## sexMale
                            0.7886
                                                0.4816
                                                          1.291
## smoking1
                            1.1376
                                       0.8790
                                                0.6953
                                                           1.861
## hypertensionPresent
                            1.6092
                                       0.6214
                                                1.0534
                                                           2.458
## Concordance= 0.741 (se = 0.027 )
## Likelihood ratio test= 81.95 on 11 df, p=6e-13
             = 87.27 on 11 df, p=6e-14
## Score (logrank) test = 88.39 on 11 df, p=3e-14
```

```
## coxph(formula = Surv(time, DEATH_EVENT) ~ age + anaemia + creatinine_phosphokinase +
##
      ejection fraction + serum creatinine + hypertension, data = HF)
##
##
    n= 299, number of events= 96
##
##
                               coef exp(coef) se(coef)
                                                            7 Pr(>|7|)
                          4.361e-02 1.045e+00 8.853e-03 4.926 8.41e-07 ***
## age
                          3.933e-01 1.482e+00 2.129e-01 1.847 0.0648 .
## anaemia1
## creatinine_phosphokinase 1.965e-04 1.000e+00 9.856e-05 1.993 0.0462 *
## ejection_fraction -5.179e-02 9.495e-01 1.005e-02 -5.152 2.57e-07 ***
## serum creatinine
                          3.483e-01 1.417e+00 6.550e-02 5.318 1.05e-07 ***
## hypertensionPresent
                          4.668e-01 1.595e+00 2.129e-01 2.192
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
                         exp(coef) exp(-coef) lower .95 upper .95
## age
                           1.0446 0.9573 1.0266 1.0629
## anaemia1
                           1.4818
                                      0.6749 0.9762
                                                       2.2493
## creatinine_phosphokinase
                          1.0002 0.9998
                                                       1.0004
                                               1,0000
                    0.9495
## ejection fraction
                                      1.0531
                                                        0.9684
                                               0.9310
## serum_creatinine
                           1.4167
                                      0.7059
                                               1.2460
                                                         1.6108
## hypertensionPresent
                           1.5948
                                      0.6270
                                               1.0506
                                                         2,4209
## Concordance= 0.738 (se = 0.028)
## Likelihood ratio test= 77.02 on 6 df, p=1e-14
## Wald test
               = 85.82 on 6 df, p=2e-16
## Score (logrank) test = 83.51 on 6 df, p=7e-16
```

Checking Linearity of Model * Linearity of the final cox regression is sufficient.

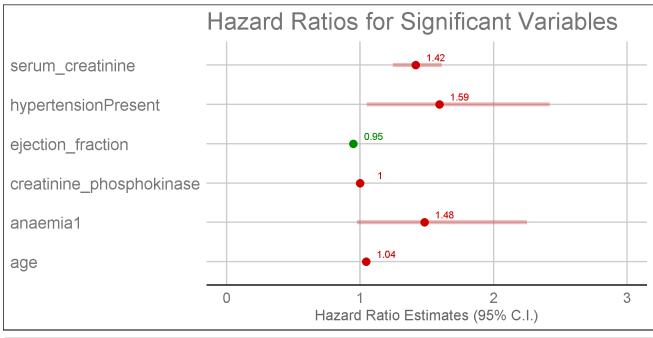
SAY SOMETHING ABOUT THE HAZARD RATIO PLOT

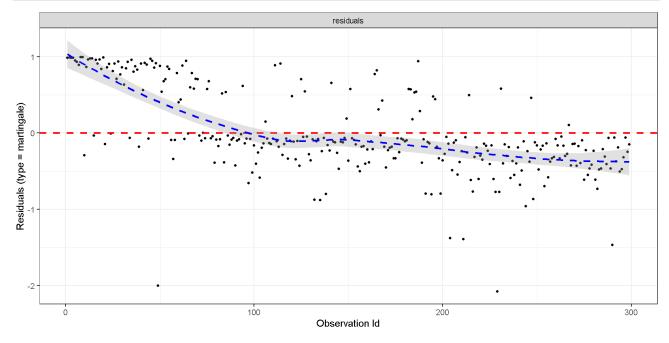
Residual Plot



integer(0)

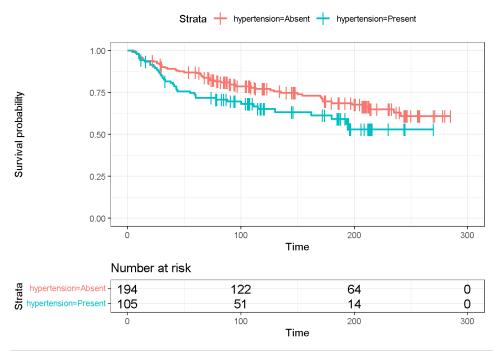
```
#ggforest(sigMod, data = HF)
library(ggthemes)
finMod <- sigMod %>% tidy()
finMod %>% mutate(upper = estimate + 1.96 * std.error,
        lower = estimate - 1.96 * std.error) %>%
 mutate(across(all_of(c("estimate", "lower", "upper")), exp)) %>%
 ggplot(aes(estimate, term, color = estimate > 1)) +
 geom_vline(xintercept = 1, color = "gray75") +
 geom_linerange(aes(xmin = lower, xmax = upper), size = 2.25, alpha = 0.28) +
  geom_point(size = 4) +
 theme_gdocs(base_size = 16) +
 scale_color_manual(values = c("green4", "red3"), guide = "none") +
 xlim(c(0, 3)) +
 labs(title = "Hazard Ratios for Significant Variables", y = NULL,
      x = "Hazard Ratio Estimates (95% C.I.)") +
 theme(axis.text.y = element_text(hjust = 0, size = 18)) +
   geom_text(label = exp(finMod$estimate) %>% round(2),
              nudge_y = .2, nudge_x = .15)
```





Performing the Log-Rank Test on the $\,$ hypertension $\,$ & diabetes .

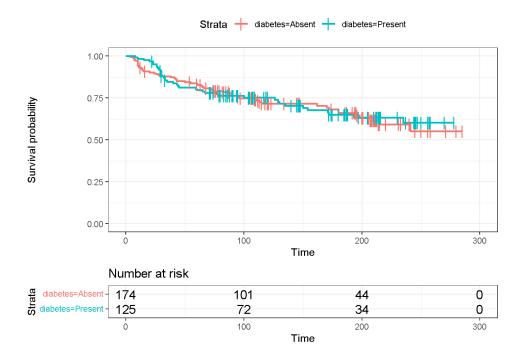
- Finding out that the distribution of present hypertension is statistically significant when compared against the distribution of the absence of it.
- The presence of diabetes, however, does not impact survival rate.



```
survdiff(Surv(time,DEATH_EVENT) ~ hypertension, data=HF)
```

```
## Call:
## survdiff(formula = Surv(time, DEATH_EVENT) ~ hypertension, data = HF)
##

## N Observed Expected (0-E)^2/E (0-E)^2/V
## hypertension=Absent 194 57 66.4 1.34 4.41
## hypertension=Present 105 39 29.6 3.00 4.41
##
## Chisq= 4.4 on 1 degrees of freedom, p= 0.04
```



```
survdiff(Surv(time,DEATH_EVENT) ~ diabetes, data=HF)
```

QUESTIONS TO ASK:

- Probability that person survives longer than time = x? CHECK
- Typical survival rate for person in a certain region? N/A
- Out of 10 random observations, how many do we expect to be deceased after 60 days?

NEXT STEPS: BUILD A LOGISTIC MODEL FOR PREDICITONS RIGHT AFTER, PERHAPS.

Findings:

- Diabetes isn't a statistically significant predictor of survival time.
- At a given instance in time, someone who has hypertension is 0.42 times as likely to die as someone without hypertension adjusting for age.
- At any given instance in time, someone who does not have hypertension is 0.65 times as likely to die as someone who does, adjusting for
 age
- Probability of survival after 150 days for those younger than 70 is 77%.
- Probability of survival after 200 days for those younger than 70 is 70%.
- 24% probability of survival after t=130 days for patients older than 79, that have less than or equal to 1.8 in serum creatine, and an ejection fraction over 25.
- For those diabetic, plateletes reduce as age increases.
- On average, creatinine phosphokinase is higher for non-smokers.
- $\bullet \ \ \text{Men, on average, have higher creatinine_phosphokinase} \ .$
- · Women, on average, have a higher platelets count.