

# **Linear adversarial training, robustness in machine learning and applications to cardiology**

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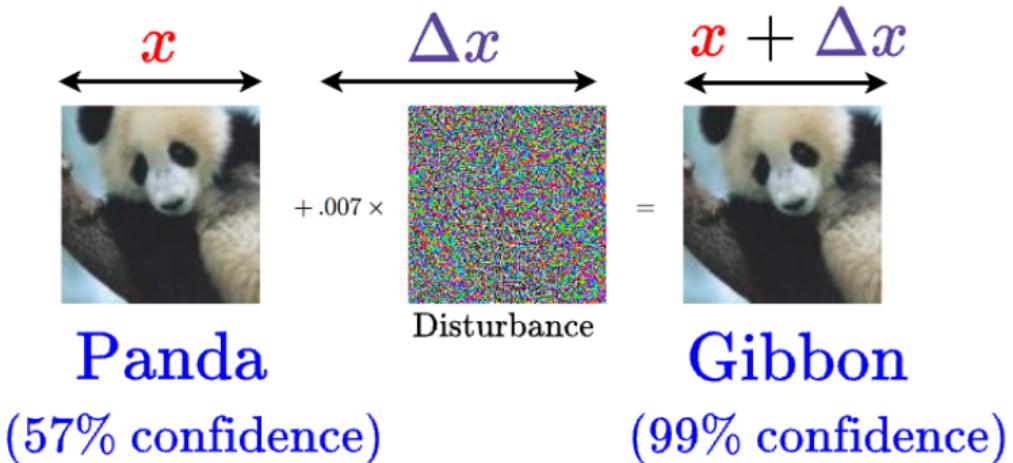
**Antônio H. Ribeiro**

Uppsala University, Sweden

KTH, Royal Institute of Technology  
Stockholm, Sweden

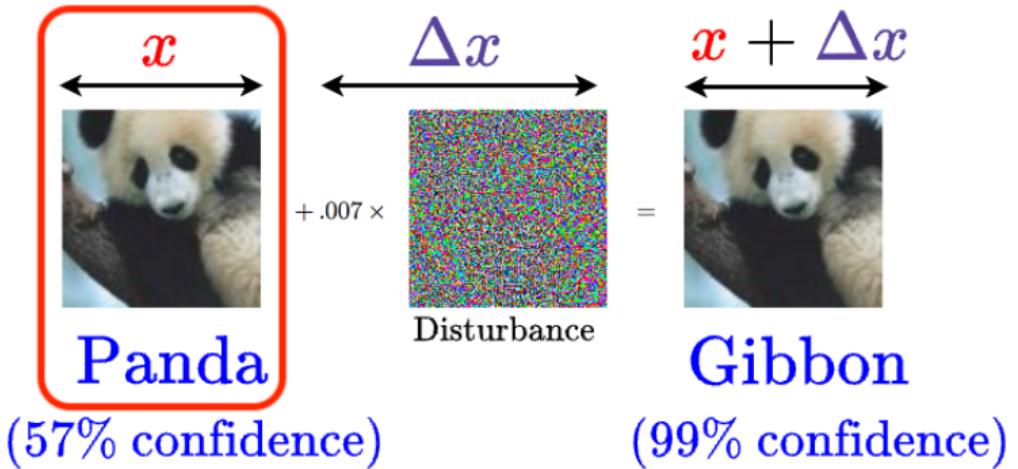
2023

# Adversarial attacks



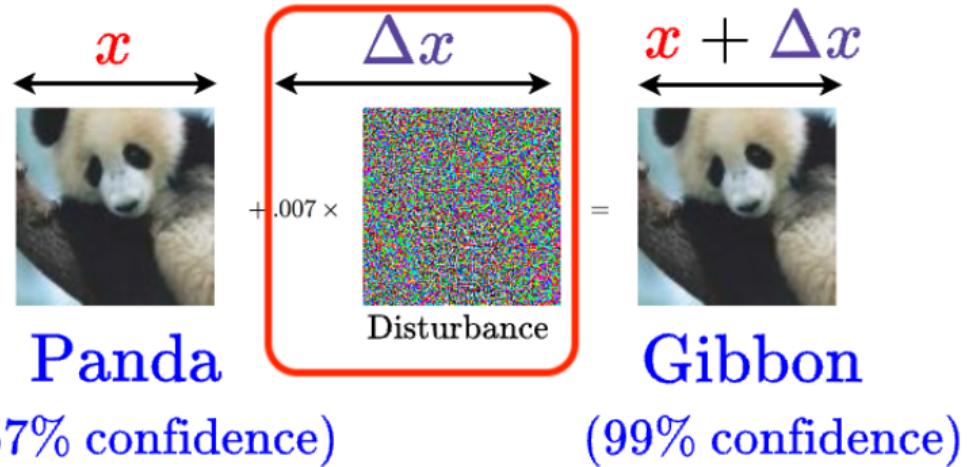
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## Adversarial attacks



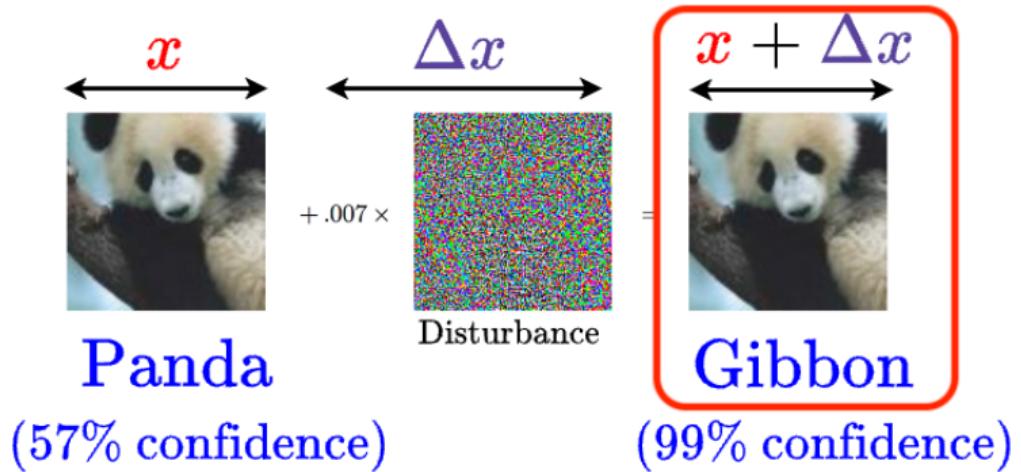
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**Adversarial training:** *Each training sample is modified by an adversary.*

## Part I. Linear adversarial training

Regularization properties of adversarially-trained linear regression

Antônio H. Ribeiro, Dave Zachariah, Francis Bach, Thomas B. Schön.

*NeurIPS* (2023) - Spotlight

## Part II. Robustness of overparameterized models

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## Part III. Automatic ECG analysis

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# Adversarially-trained linear regression

- ▶ Linear regression:

$$\min_{\beta} \sum_{i=1}^{\#train} (\textcolor{blue}{y}_i - \beta^\top \textcolor{red}{x}_i)^2$$

# Adversarially-trained linear regression

## ► Linear regression:

$$\min_{\beta} \sum_{i=1}^{\#train} (\underbrace{y_i}_{\text{observed}} - \underbrace{\beta^\top x_i}_{\text{linear prediction}})^2$$

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- ▶ **Adversarial training** in linear regression:

$$(\mathbf{y}_i - \beta^\top (\mathbf{x}_i + \Delta \mathbf{x}_i))^2$$

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$$\sum_{i=1}^{\#train} \max_{\|\Delta x_i\| \leq \delta} (\mathbf{y}_i - (\mathbf{x}_i + \Delta \mathbf{x}_i)^T \boldsymbol{\beta})^2$$

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$$\sum_{i=1}^{\#\text{train}} \max_{\|\Delta x_i\| \leq \delta} (\mathbf{y}_i - (\mathbf{x}_i + \Delta \mathbf{x}_i)^T \boldsymbol{\beta})^2$$

It can be **rewritten** as:

$$\sum_{i=1}^{\#\text{train}} \left( |\mathbf{y}_i - \mathbf{x}_i^T \boldsymbol{\beta}| + \delta \|\boldsymbol{\beta}\|_* \right)^2$$

where  $\|\cdot\|_*$  is the **dual norm**.

## Adversarially-trained linear regression

$$\sum_{i=1}^{\#train} \max_{\|\Delta x_i\|_\infty \leq \delta} (\mathbf{y}_i - (\mathbf{x}_i + \Delta \mathbf{x}_i)^\top \boldsymbol{\beta})^2$$

It can be **rewritten** as:

$$\sum_{i=1}^{\#train} \left( |\mathbf{y}_i - \mathbf{x}_i^\top \boldsymbol{\beta}| + \delta \|\boldsymbol{\beta}\|_1 \right)^2$$

where  $\|\cdot\|_1$  is the **dual norm**.

## Similarities with Lasso

- $\ell_\infty$ -adversarial attacks:

$$\sum_{i=1}^{\#train} \left( |\textcolor{blue}{y}_i - \textcolor{red}{x}_i^\top \textcolor{magenta}{\beta}| + \delta \|\textcolor{magenta}{\beta}\|_1 \right)^2$$

- Lasso:

$$\sum_{i=1}^{\#train} \left( |\textcolor{blue}{y}_i - \textcolor{red}{x}_i^\top \textcolor{magenta}{\beta}| \right)^2 + \lambda \|\textcolor{magenta}{\beta}\|_1.$$

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### Main results:

#1. Map  $\lambda \leftrightarrow \delta$  for which they yield the **same result**.

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- #2. **More parameters than data**: abrupt transition into interpolation.

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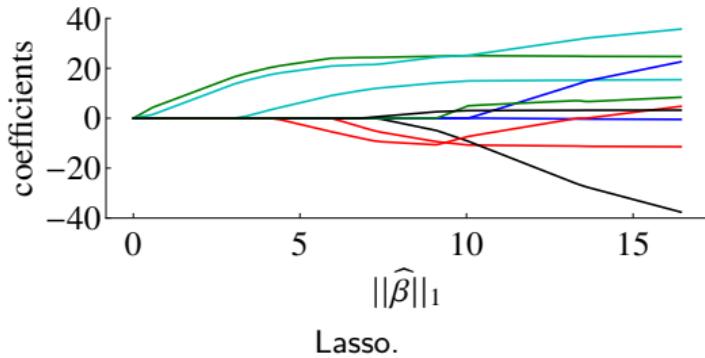
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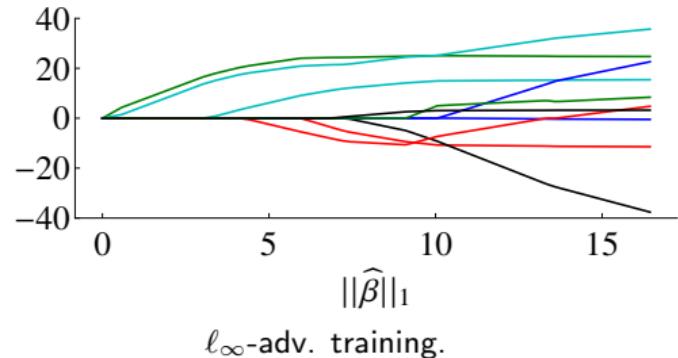
- #1. Map  $\lambda \leftrightarrow \delta$  for which they yield the **same result**.
- #2. **More parameters than data**: abrupt transition into interpolation.
- #3. **Optimal choice** of  $\delta$  independent on noise level.

## # 1. Equivalence with Lasso

Map  $\lambda \leftrightarrow \delta$  for which they yield the **same result**.



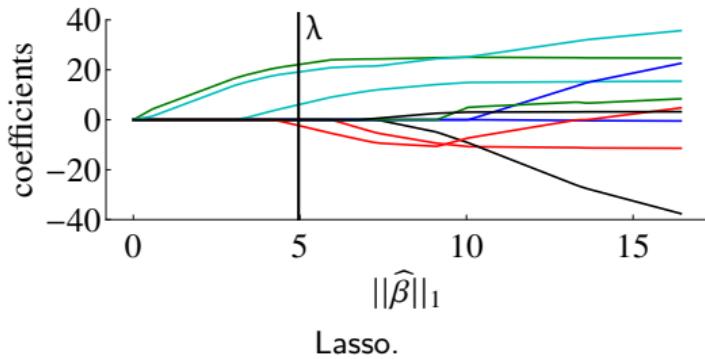
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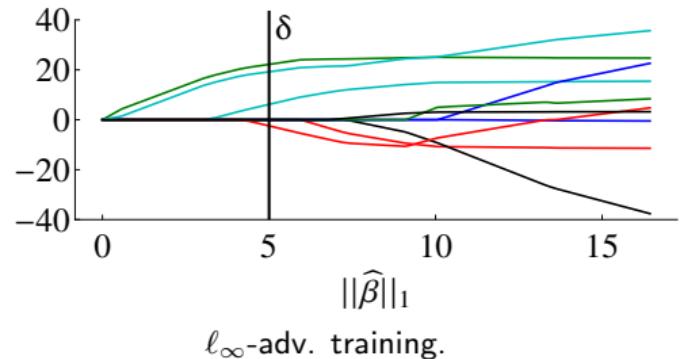
$\ell_\infty$ -adv. training.

## # 1. Equivalence with Lasso

**Map**  $\lambda \leftrightarrow \delta$  for which they yield the **same result**.



Lasso.



$\ell_\infty$ -adv. training.

The that yield the **same result** are **not** necessarily the same, i.e.:  $\delta \neq \lambda$

## # 2. More parameters than data

**Lasso:** transition **only in the limit**

$$\lambda \rightarrow 0^+ \Rightarrow \sum_{i=1}^{\#train} (\textcolor{blue}{y}_i - \textcolor{red}{x}_i^T \textcolor{violet}{\beta})^2 \rightarrow 0$$

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**Adversarial training:**

$$\delta \in (0, \text{threshold}] \Rightarrow \sum_{i=1}^{\#train} (\mathbf{y}_i - \mathbf{x}_i^\top \boldsymbol{\beta})^2 = 0$$

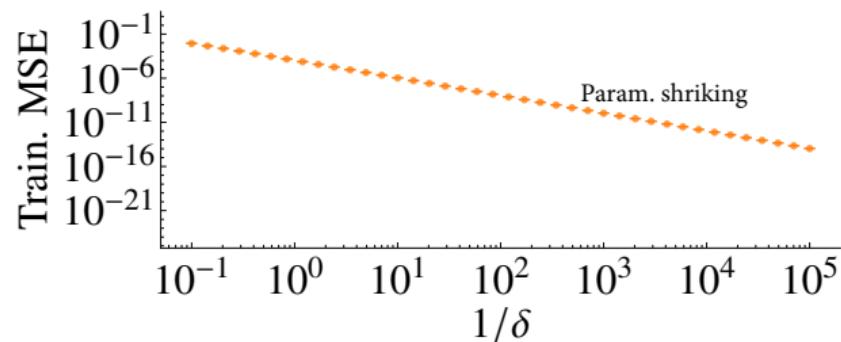
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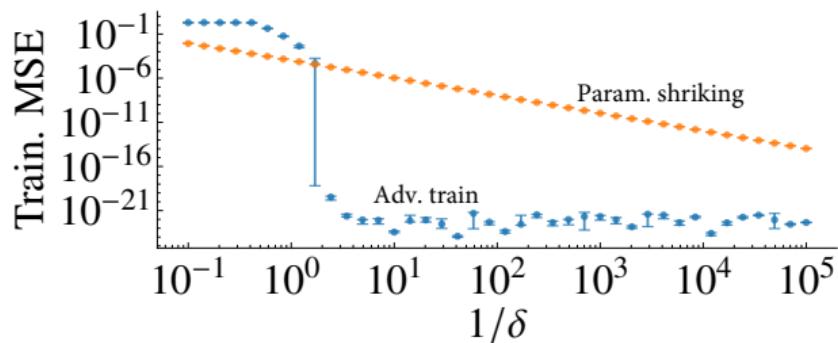
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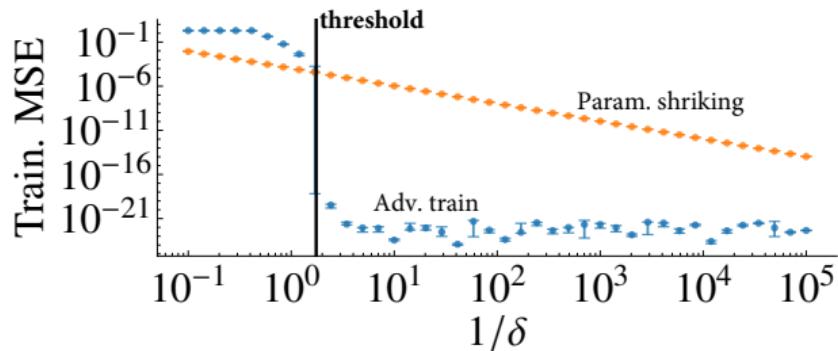
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## # 2. Equivalence with minimum norm interpolator

For  $\delta \in (0, \text{threshold}]$ , the minimum-norm interpolator is the solution to adversarial training.

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### Relevance

Connect **adversarial training** with **double descent** and **benign overfitting**

## # 3. Invariance to noise levels

*To obtain near-oracle performance.*

- ▶ Lasso:

$$\lambda \propto \sigma \sqrt{\log(\#params) / \#train}$$

- ▶  $\ell_\infty$ -adversarial attack:

$$\delta \propto \sqrt{\log(\#params) / \#train}$$

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### Data model

$$y = \underbrace{\mathbf{x}^\top \boldsymbol{\beta}^*}_{\text{signal}} + \underbrace{\sigma}_{\text{noise std.}} \varepsilon.$$

# Regularization properties of adversarially-trained linear regression

Additional results:

- ▶  $\ell_2$ -adv. attacks and ridge regression.

Regularization properties of adversarially-trained linear regression

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NeurIPS (2023) - Spotlight

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# Regularization properties of adversarially-trained linear regression

Additional results:

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- ▶ Connection to robust regression and  $\sqrt{\text{Lasso}}$ .

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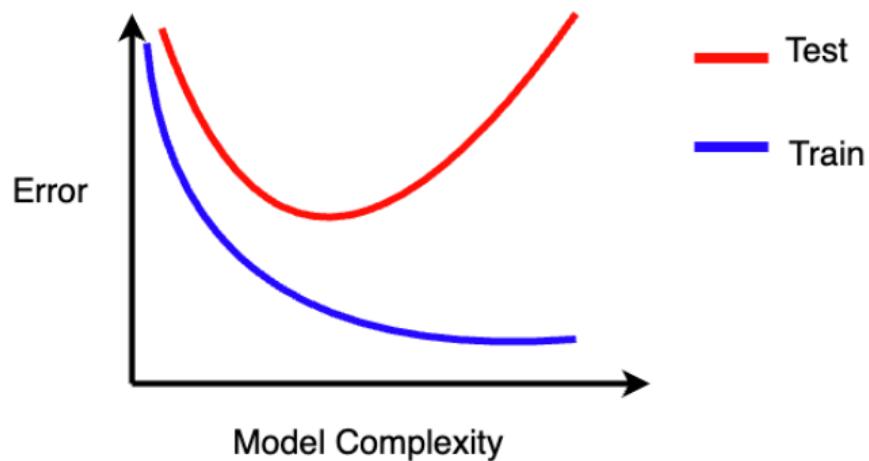
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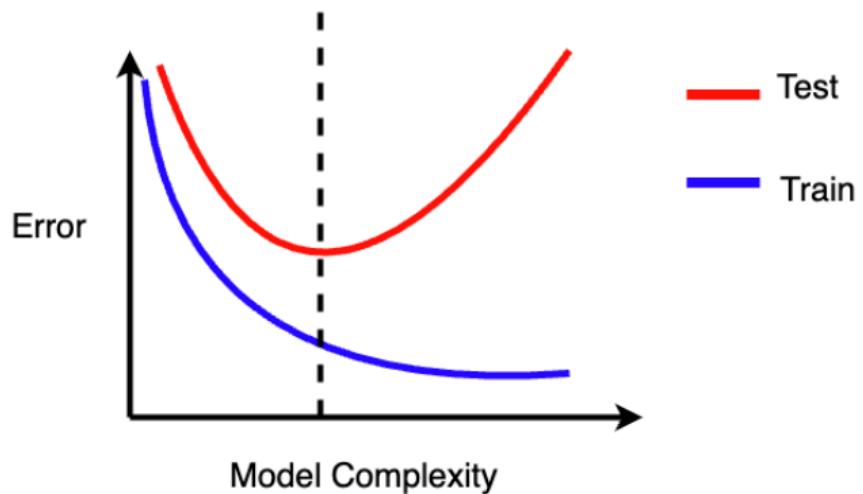
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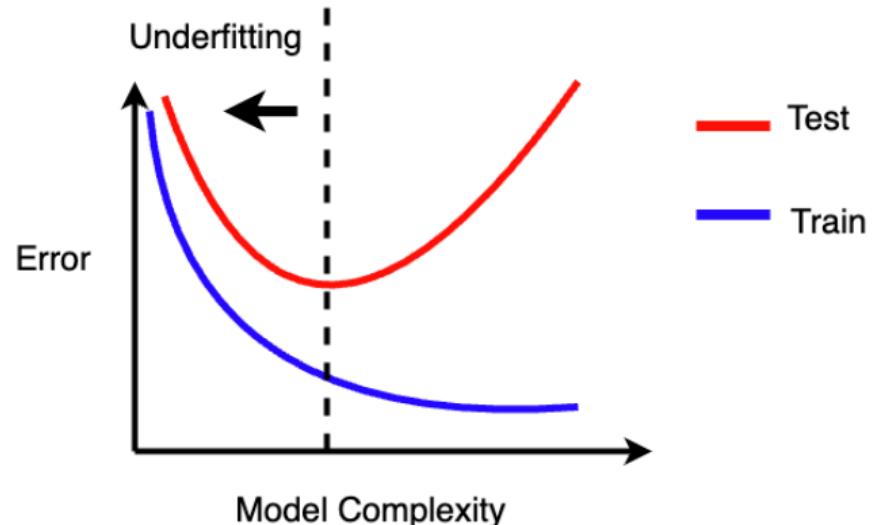
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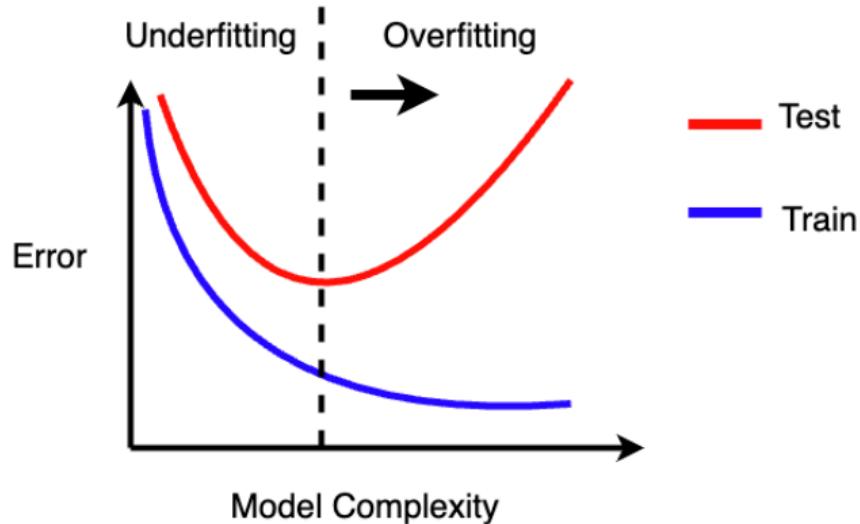
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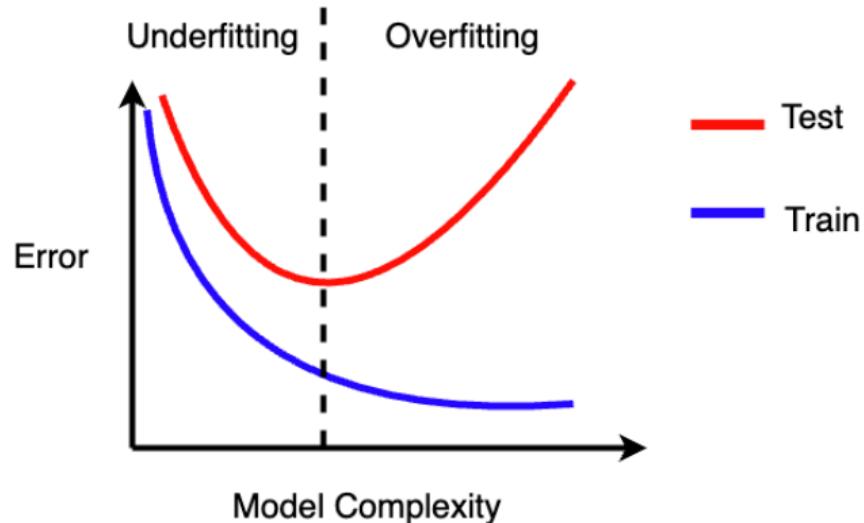
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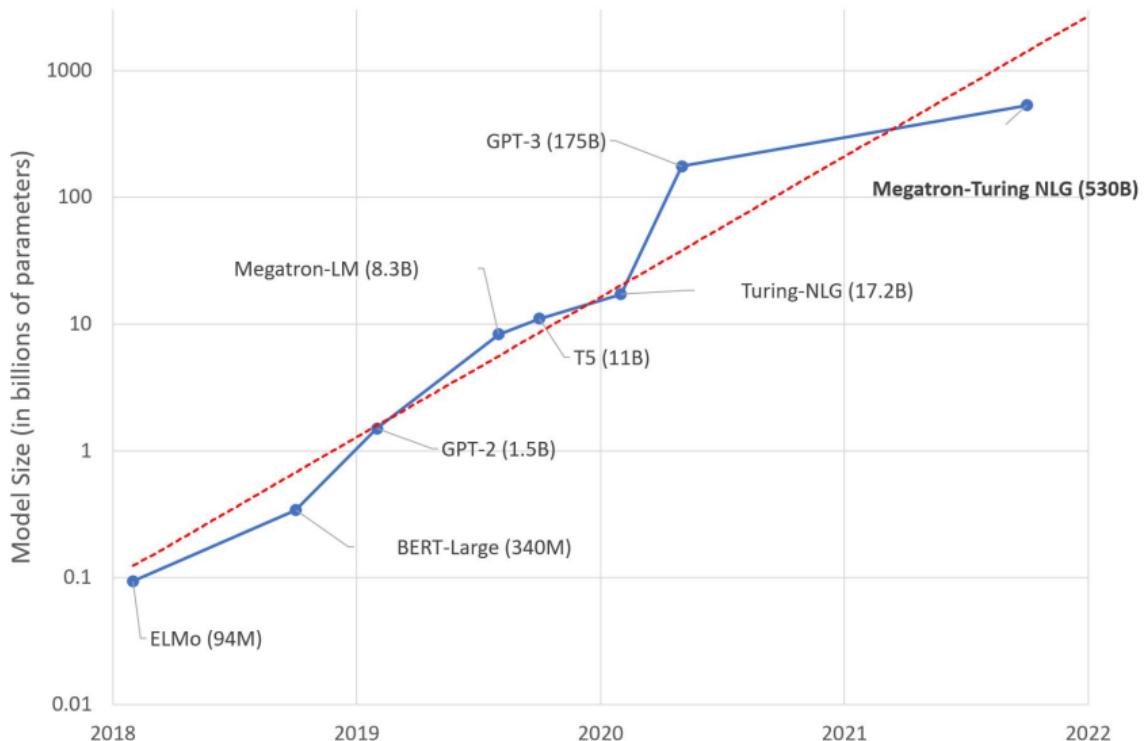
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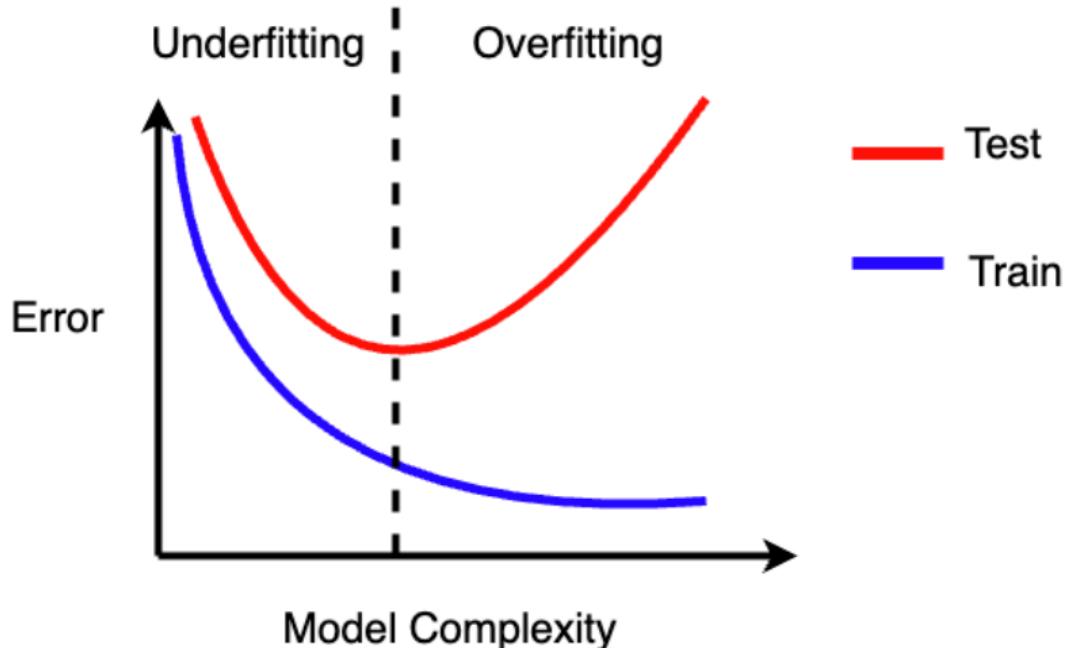


# Generalization of deep neural networks



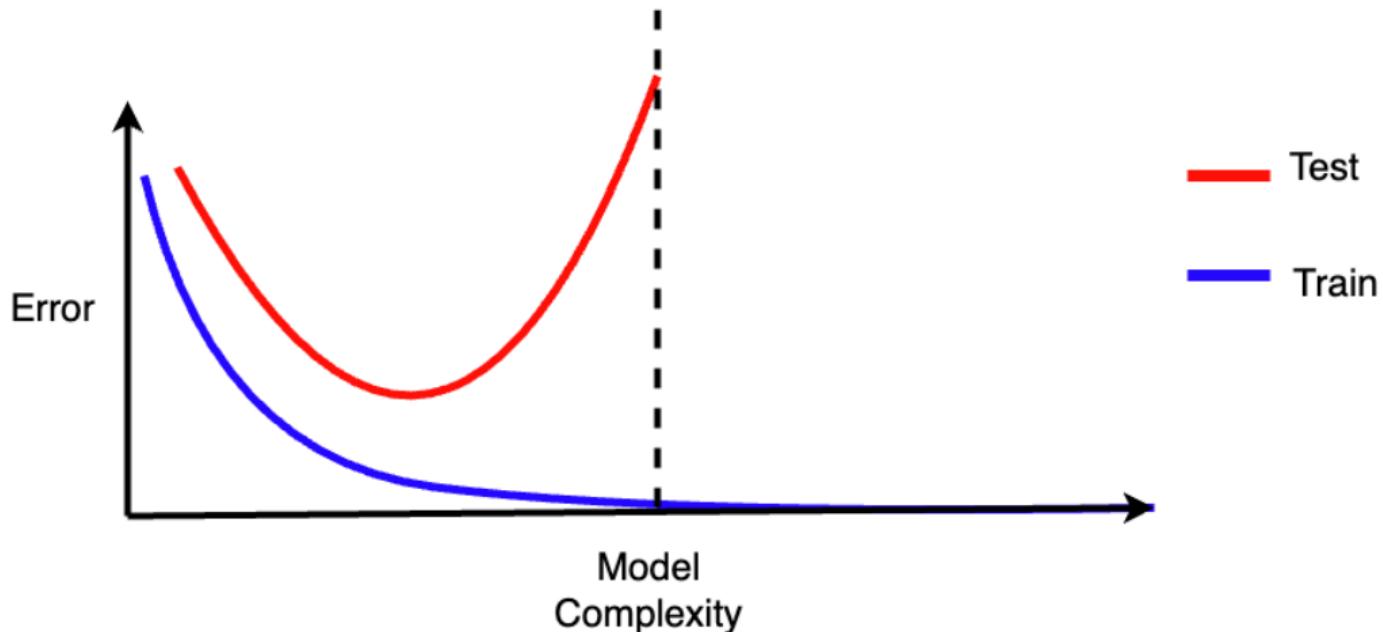
C. Zhang, S. Bengio, M. Hardt, B. Recht, and O. Vinyals. Understanding deep learning requires rethinking generalization. ICLR, 2017

## Double-descent curves



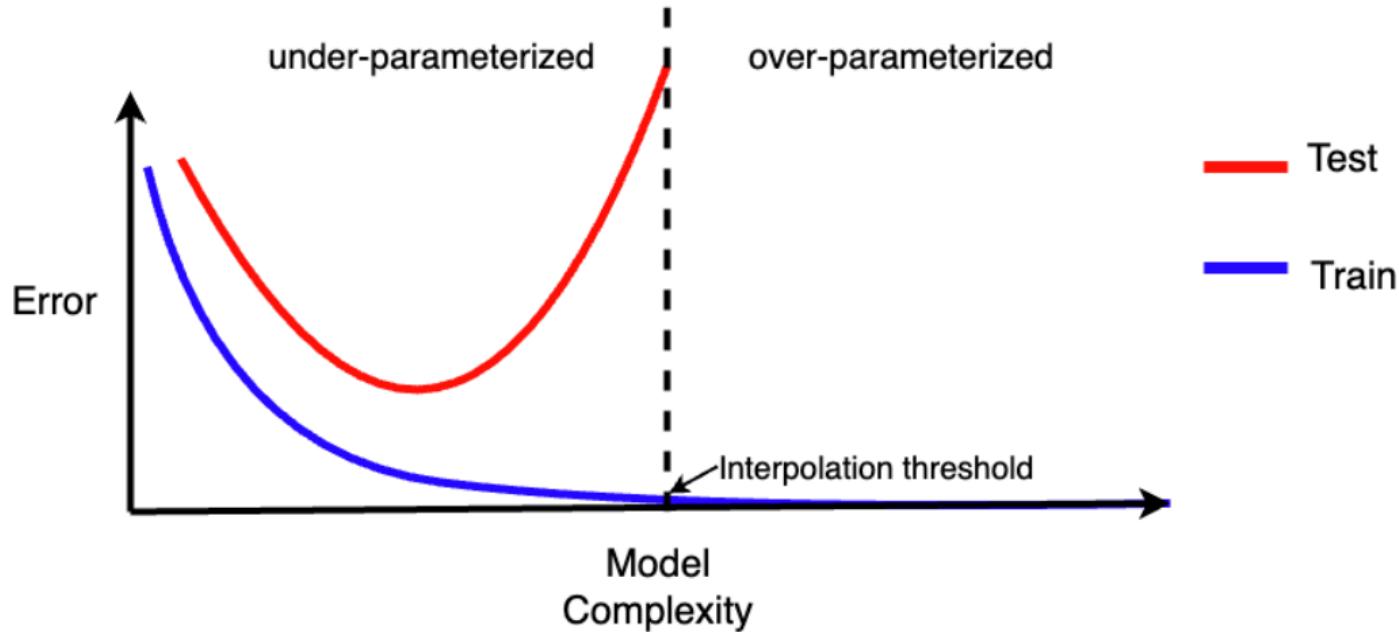
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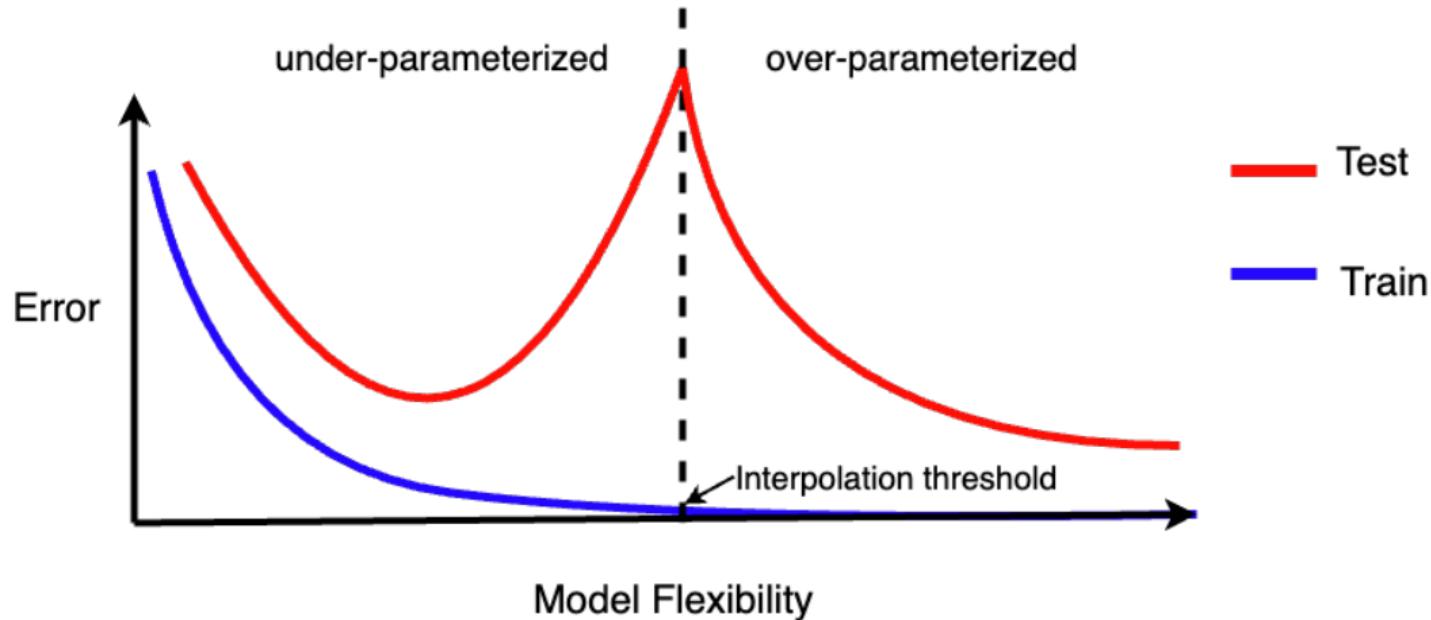
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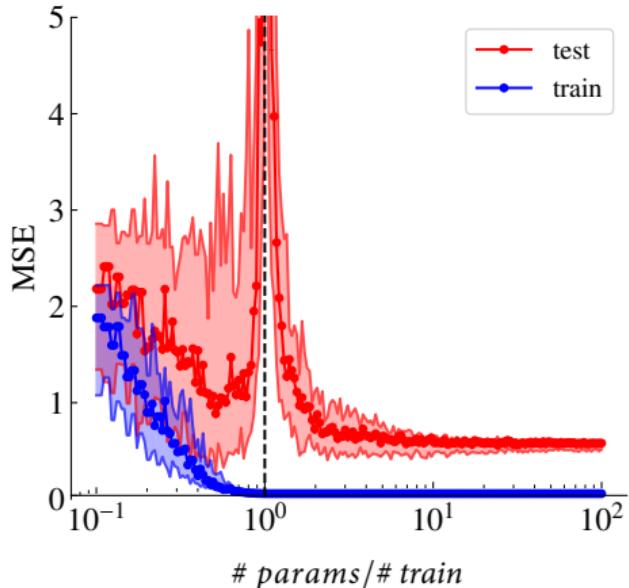
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Beyond Occam's Razor in System Identification: Double-Descent when Modeling Dynamics

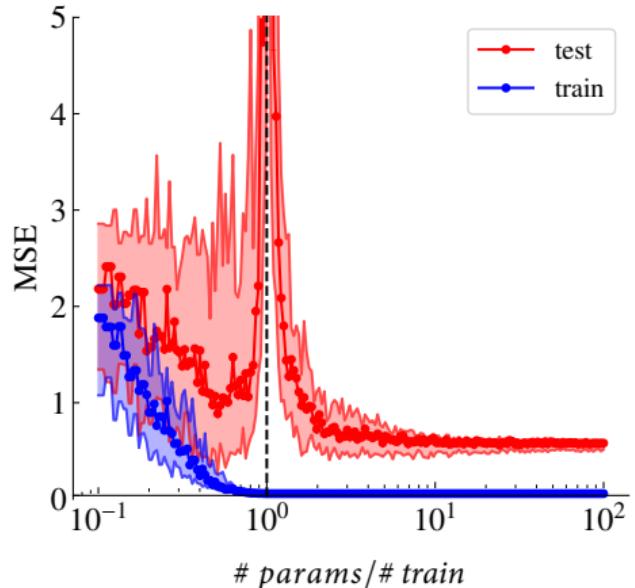
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Deep networks for system identification: a Survey

Gianluigi Pillonetto, Aleksandr Aravkin, Daniel Gedon, Lennart Ljung, Antonio H. Ribeiro, Thomas Bo Schön.

Automatica (Provisionally accepted), 2023.

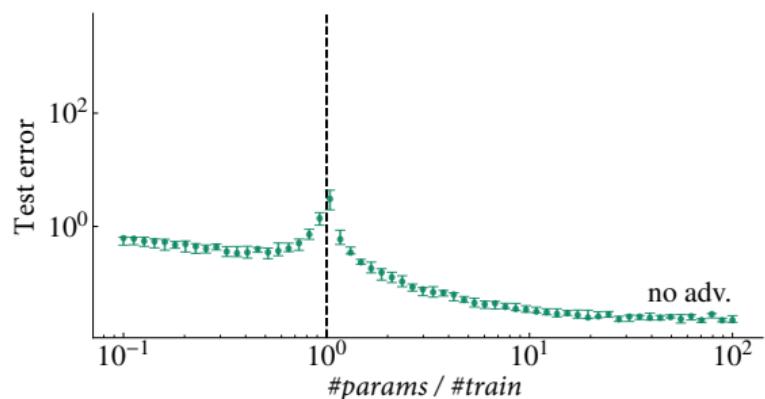
Can **double descent** be observed **in adversarial settings**?

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Given a **test point**  $(\mathbf{x}_0, \mathbf{y}_0)$ , the error is:

- ▶ no adversary

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**Figure:** Adv. risk. min.  $\ell_2$ -norm interpolator

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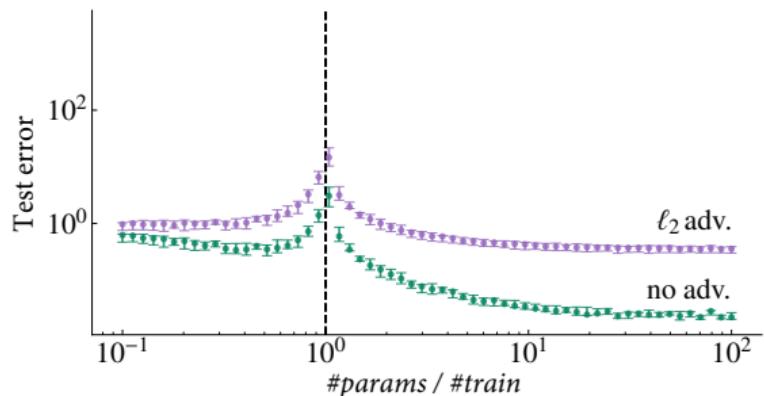
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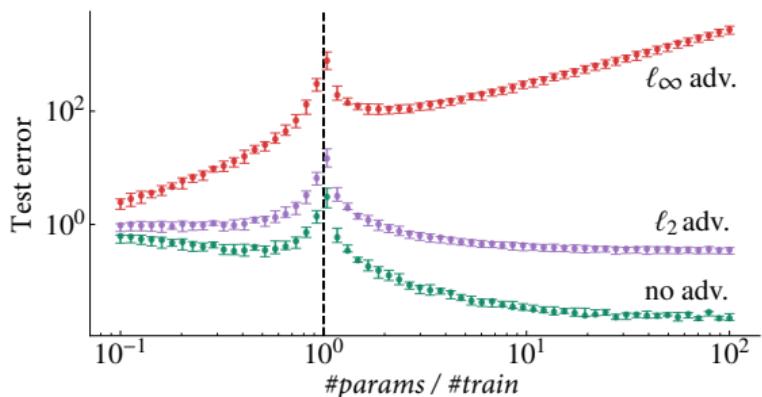
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**Figure:** Adv. risk. min.  $\ell_2$ -norm interpolator

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# Overparameterized Linear Regression under Adversarial Attack

## Interpretation

Minimum  $\ell_2$ -norm interpolation  $\Leftrightarrow \ell_2\text{-adversarial training}$ . (Result #2, Part I)

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Analysis:

- ▶ **Assimptotic results** showing the phenomena
- ▶ **Non-asymptotic results**: concentration inequalities

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# The electrocardiogram (ECG) exam

Cardiovascular diseases:

- ▶ ≈18 million **deaths** in 2019 (**32%**).

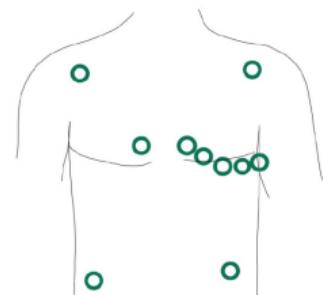
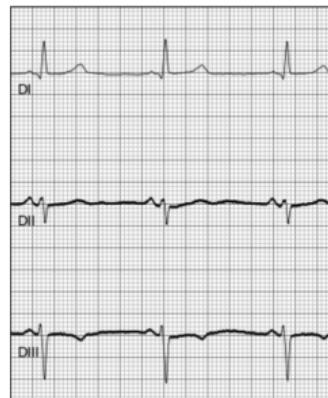
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The ECG is the **major diagnostic tool**.

- ▶ Low-cost, safe and non-invasive
- ▶ Can detect arrhythmias, myocardial infarction, cardiomyopathy...



**Left:** ECG signal **Right:** Electrode placement.

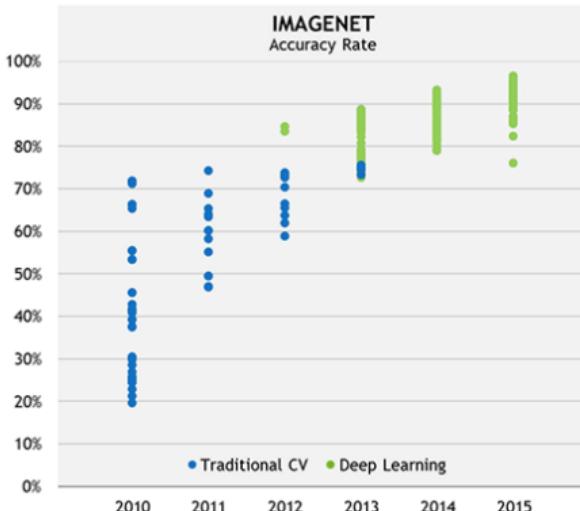
# Computational electrocardiography



**Figure Automated ECG interpretation Glasgow (1971).**

Macfarlane, P.W.; Kennedy, J. "Automated ECG Interpretation—A Brief History from High Expectations to Deepest Networks." *Hearts* 2021.

# The transition into end-to-end learning



**Figure: Accuracy on Imagenet** as models **transitioned** from feature extraction to end-to-end.

J. Deng, W. Dong, R. Socher, L.-J. Li, K. Li, and L. Fei-Fei, "Imagenet: A large-scale hierarchical image database," CVPR (2009)

# Telehealth and automatic diagnosis

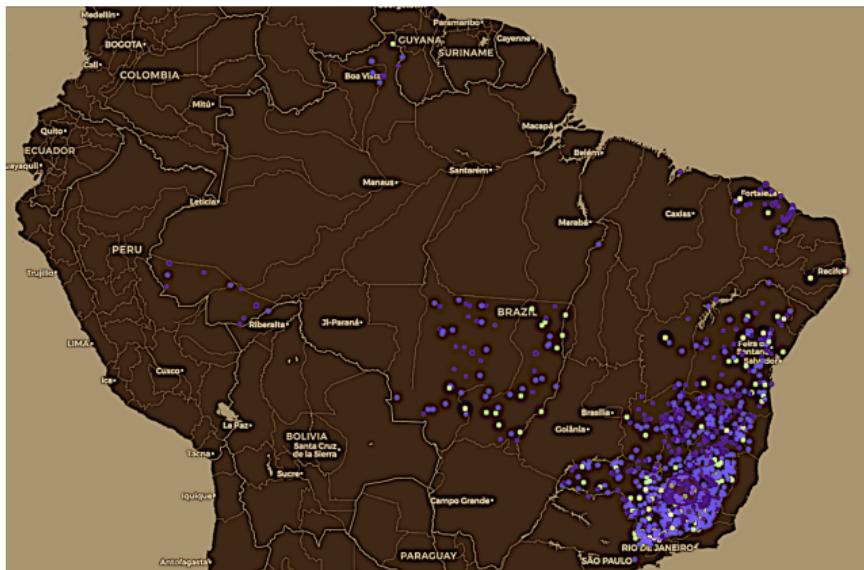


**Figure:** State of Minas Gerais

# Telehealth and automatic diagnosis

## Telehealth Center of Minas Gerais

- ▶ 1100 municipalities
- ▶ > 3 500 ECGs per day



**Figure:** Municipalities assisted by the telehealth center

## Automatic diagnosis of the ECG

- ▶ CODE dataset: historical data 2010 to 2017.
  - ▶  $n = 1.6M$  patients

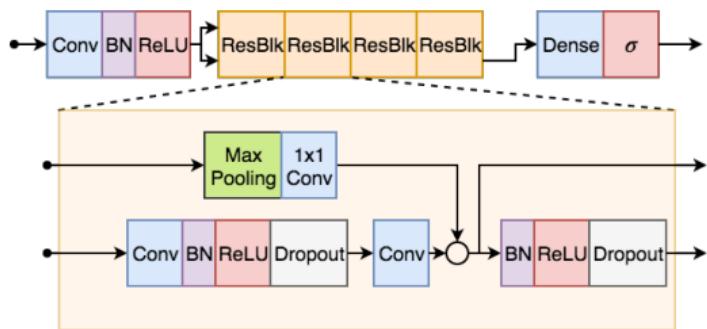
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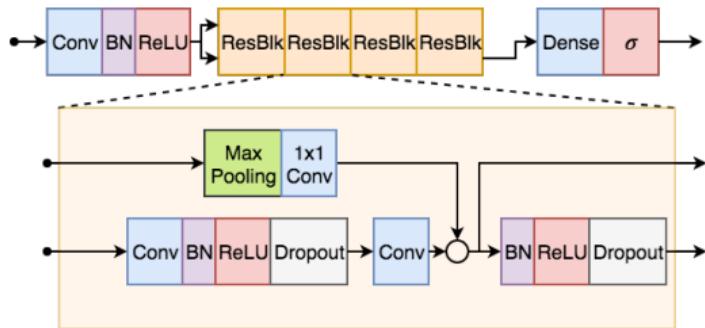
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Automatic diagnosis of the 12-lead ECG using a deep neural network

A. H. Ribeiro , M.H. Ribeiro, Paixão, G.M.M. et al

Nature Communications (2020)



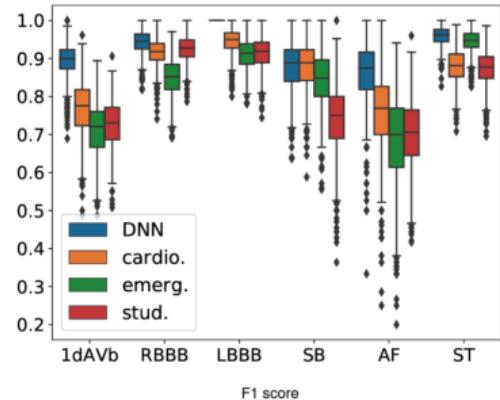
# Automatic diagnosis of the ECG (cont.)

- **Result:** Deep neural network (DNN) performs at least as well as experts

cardio. → 4th year cardiology residents

emerg. → 3rd year emergency residents

stud. → 5th year Medical students



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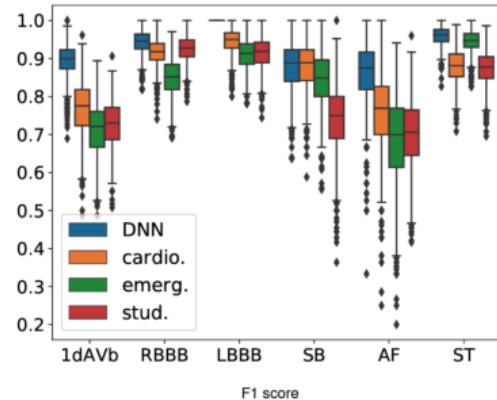
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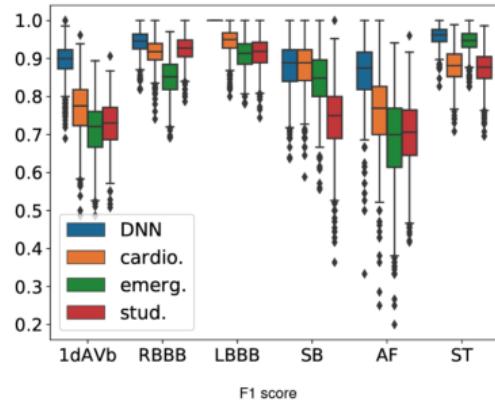
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- ▶ **Goal:** Improve the **accuracy**  
assist **more patients**

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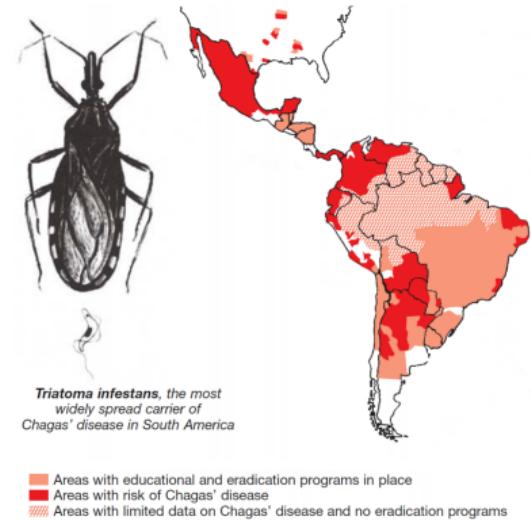


## Three directions

1. Automatic diagnosis;
2. Screening;
3. Prognosis.

# Screening for Chagas disease from the ECG using deep neural networks

- ▶ **6 million** people infected.
- ▶ Diagnosed with **blood test**.
- ▶ Early diagnosis and treatment **halt progression**.
- ▶ **Low detection rates**

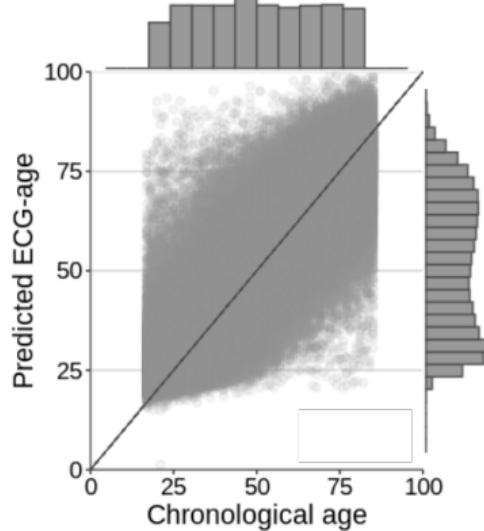


Map source: PAHO

## Screening for Chagas disease from the electrocardiogram using a deep neural network

Carl Jidling, Daniel Gedon, Thomas B. Schön, Cláudia Di Lorenzo Oliveira, Clareci Silva Cardoso, Ariela Mota Ferreira, Luana Giatti, Sandhi Maria Barreto, Ester C. Sabino, Antônio L. P. Ribeiro, **Antônio H. Ribeiro**  
*Plos Neglected Tropical Diseases* (2023)

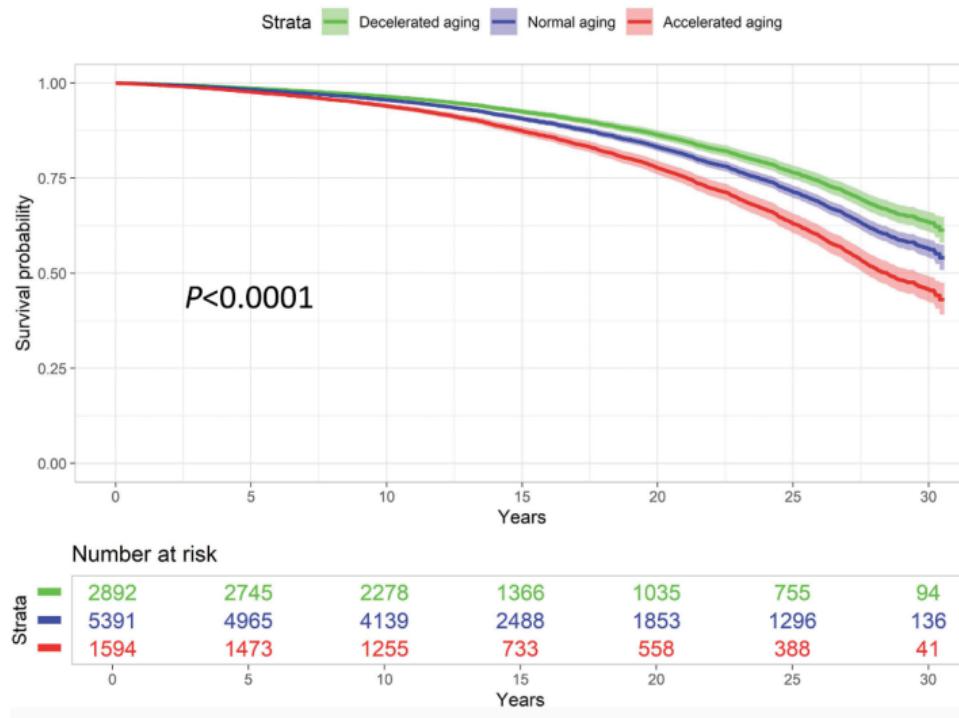
## ECG predicted-age



Deep neural network estimated electrocardiographic-age as a mortality predictor

Emilly M. Lima\*, Antônio H. Ribeiro\*, Gabriela MM Paixão\*, et. al. *Equal contribution*  
*Nature Communications* (2021)

# Risk predictor of cardiovascular events



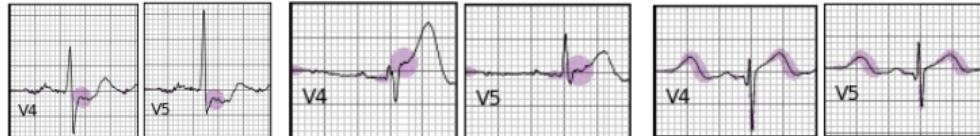
Electrocardiographic Age Predicts Cardiovascular Events in Community: The Framingham Heart Study

Luisa C C Brant, Antônio H Ribeiro, Marcelo M Pinto-Filho, et. al.

Circulation: Cardiovascular Quality and Outcomes (2023)

# Challenges

- ▶ **Interpretability** Attempt to draw real electrocardiographic **knowledge**.

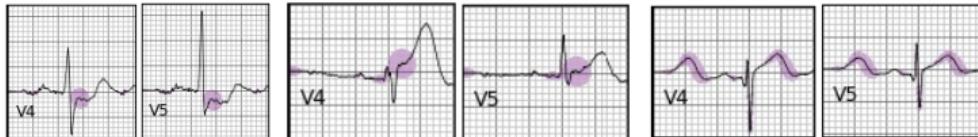


**Figure:** Grad-CAM plots. **(Left)** STEMI. **(Middle)** STEMI. **(Right)** NSTEMI.

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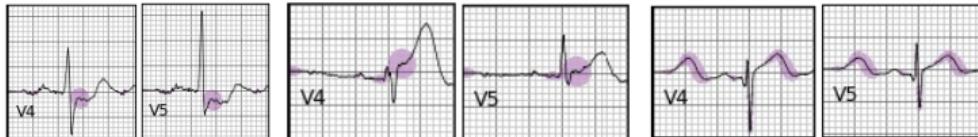
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*Scientific Reports* (2022)

- ▶ **Robustness.** Ability to work in **real situations**.

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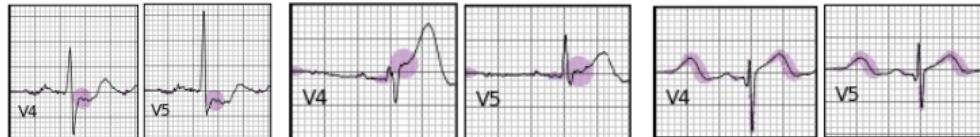
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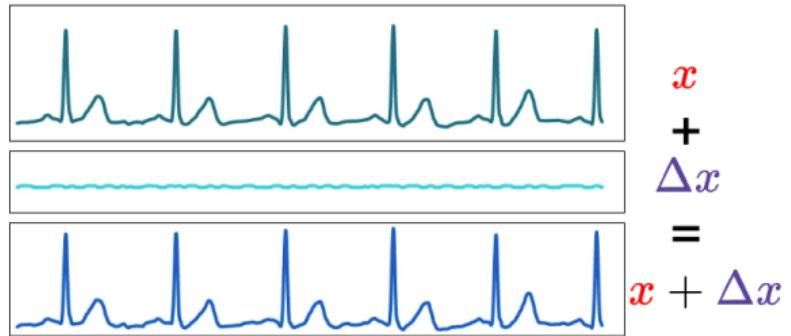
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*ML algorithms don't need to be really interpretable to be useful in clinical practice.  
But they need to be robust!*

# Adversarial attacks in ECGs

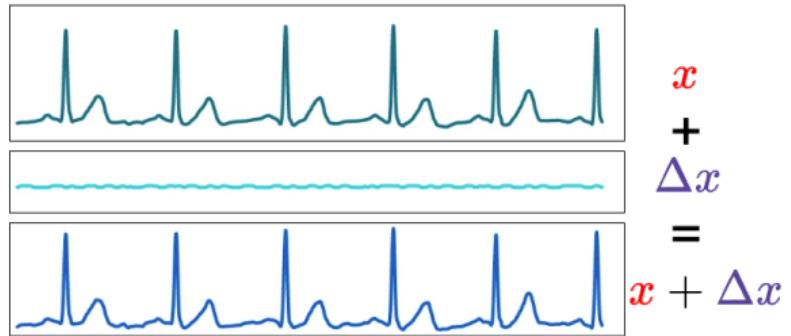
- $x \rightarrow \hat{y}$  :  
**Normal** (Probability = 0.99)



Han, X., Hu, Y., Foschini, L. et al. Deep learning models for electrocardiograms are susceptible to adversarial attacks. *Nature Medicine.* (2020)

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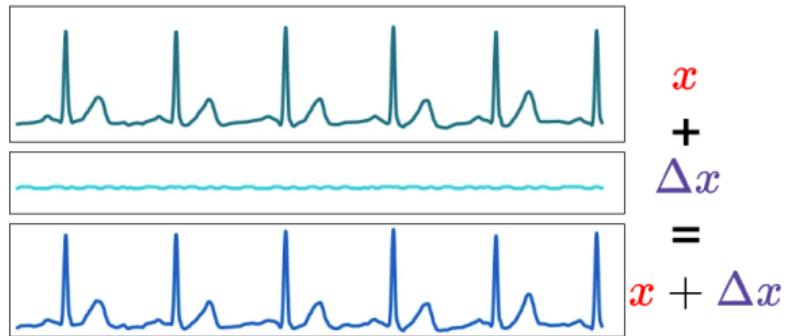
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- ▶  $\|\Delta x\| < \delta$



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# Adversarial attacks in ECGs

- ▶  $x \rightarrow \hat{y}$  :  
**Normal** (Probability = 0.99)
- ▶  $\|\Delta x\| < \delta$
- ▶  $x + \Delta x \rightarrow \tilde{y}$  :  
**AFib** (Probability = 1.00)



Han, X., Hu, Y., Foschini, L. et al. Deep learning models for electrocardiograms are susceptible to adversarial attacks. *Nature Medicine.* (2020)

# Conclusion

- ▶ **Large-scale models** have great potential for medicine (and critical applications).
- ▶ **Robustness** is a major challenge.
- ▶ **Adversarial attacks** framework allows for analysis of **worst-case scenarios**.
- ▶ **Linear models** for insight and analysis.
- ▶ **Adversarially-trained linear regression** is a competitive regression method.

Thank you!

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