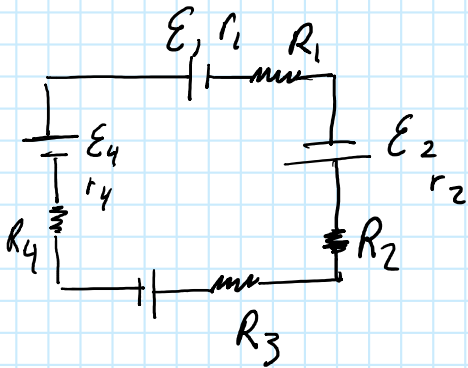


## 1] Circuitos C.D.

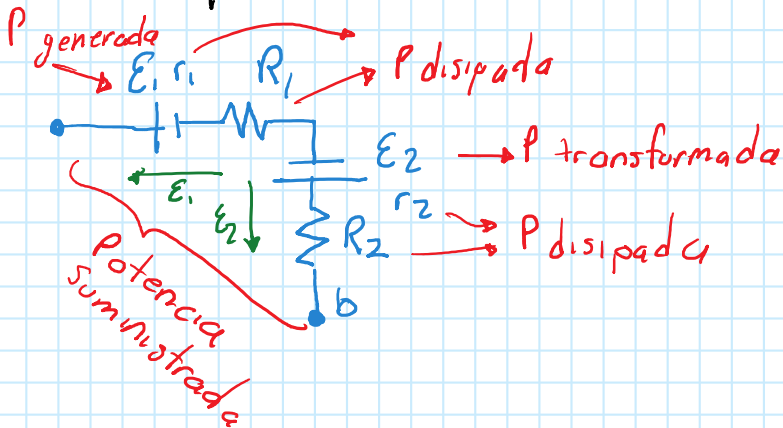


$$I = \frac{\sum \mathcal{E}}{\sum r} = \frac{80}{46} \approx 1.73 [A]$$

- $\varepsilon_1, \varepsilon_3 \stackrel{\Delta}{=} \text{Generatoren}$

•  $\varepsilon_2, \varepsilon_4 \stackrel{\Delta}{=} \text{Motors}$

$$V = \frac{E_{np}}{q}; \quad E_{np} = V_q; \quad \Delta E_{np} = q(\Delta V)$$



$$P_{\text{entrada}} = P_{\text{salida}}$$

$$P_{entrada} = P_{gen} + P_{sumin}$$

$$\xi = \frac{dE_{\text{Noel} \rightarrow \text{elc}}}{dq}$$

$$P = \frac{dE_u}{dt} = \frac{\epsilon d\phi}{dt}; P = \epsilon i$$

$$\frac{dE_{cap}}{dt} = V_{ab} \frac{dq}{dt} ;$$

$$\therefore P = V i$$

$$\rightarrow P_{\text{entrada}} = E_g i + \cancel{V_{ba} i}$$

$$\rightarrow P_{\text{salida}} = P_{\text{trans}} + P_{\text{disipada}}$$
$$= E_m i + \sum i^2 R$$

$$\cancel{E_y} + \cancel{V_{ab}} = \cancel{E_{m}} + \sum i^2 R ;$$

$$L_g \neq \tau \quad V_{ab} \neq -E_m \quad \tau < 0 \quad R ;$$

$$V_{ba} = -E_g + E_m + \sum iR$$

$$= \sum iR - (E_g - E_m)$$

$$// \sum_{alg} E = E_g - E_m$$

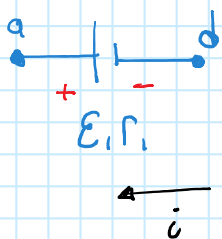
$$\therefore V_{ba} = \sum iR - \sum E$$

// Ejercicio  $\rightarrow$  Parte ①

$$\begin{aligned} V_{ba} &= (21)(1.73) - (40 + 100) \\ &= -23.67 \text{ [V]} \end{aligned} \quad \left\{ \begin{array}{l} \therefore V_{ab} = 23.67 \text{ [V]} \end{array} \right.$$

// Parte ②

$$\begin{aligned} V_{ab} &= (25)(1.73) - (30 + (-10)) \\ &= 23.25 \text{ [V]} \end{aligned}$$



// Fuente o Generador

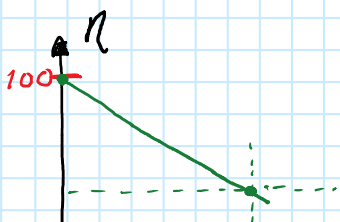
$$V_{da} = i r_{g1} - (E_{g1}) =$$

$$= (4)(1.73) - 100 = -93.08 \text{ [V]}$$

$$\rightarrow V_{ad} = 93.08$$

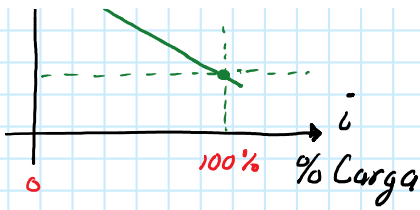
$$// \eta_g = \frac{P_{salida}}{P_{entrada}} = \frac{E_g i - i^2 r_g}{E_g i} = \frac{E_g - i r}{E_g}$$

$$\therefore \eta_g = \frac{V_{ad}}{E_g} = \frac{E_g - i r}{E_g}$$



$$\bullet \text{ if } i=0 ; E_g = V_{ad}$$

NOTA: Comportamiento de la eficiencia



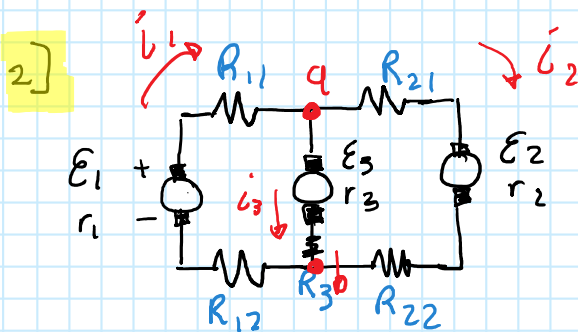
**NOTA:** Comportamiento de la eficiencia

$$\eta_{\text{motor}} = \frac{P_{\text{salida}}}{P_{\text{entrada}}}$$

$$P_{\text{entrada}} = \mathcal{E}_m i + i^2 r$$

$$P_{\text{salida}} = \mathcal{E}_m i$$

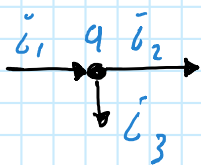
$$\therefore \eta_{\text{motor}} = \frac{\mathcal{E}_m}{\mathcal{E}_m + i r}$$



**NOTA**

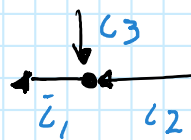
$$\text{Num}_{\text{ecuaciones}} = \text{Num}_{\text{nodos}} - 1$$

Nodo (a):



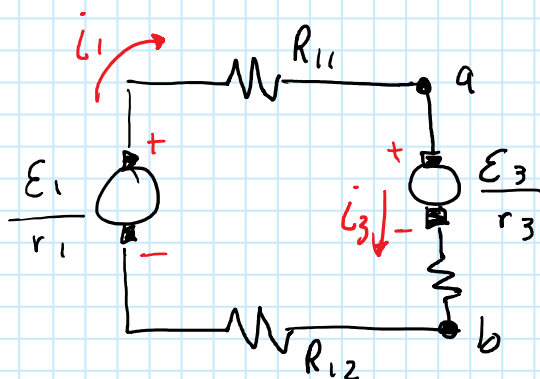
$$i_1 - i_2 - i_3 = 0$$

Nodo (b):



$$-i_1 + i_2 + i_3 = 0$$

// Ecuaciones de Mallas



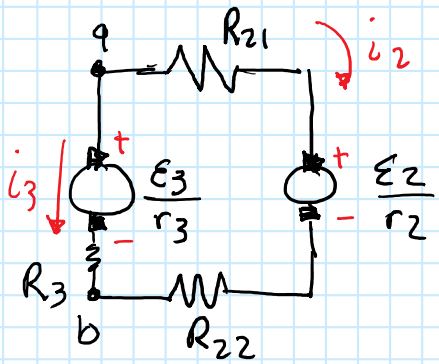
// 2° Ley Kirchhoff

$$V_{ab} = \sum r i - \sum \mathcal{E}$$

$$V_{aa} = V_a - V_a = 0$$

$$\sum r i = \sum \mathcal{E}$$

$$(R_{11} + R_{12} + r_1) \underline{i_1} + 0 \underline{i_2} + (R_3 + r_3) \underline{i_3} = \mathcal{E}_1 - \mathcal{E}_3$$



$$0 \underline{i_1} + (R_{21} + R_{22} + r_2) \underline{i_2} - (R_3 + r_3) \underline{i_3} = -\mathcal{E}_2 + \mathcal{E}_3$$

// Malha externa

$$(R_{11} + R_{12} + r_1) \underline{i_1} + (R_{21} + R_{22} + r_2) \underline{i_2} + 0 \underline{i_3} = \mathcal{E}_1 - \mathcal{E}_2$$

$$\underline{i_1} - \underline{i_2} - \underline{i_3} = 0$$

$$\sum R_1 \underline{i_1} + 0 \underline{i_2} + \sum R_3 \underline{i_3} = \sum \mathcal{E}_I$$

$$0 \underline{i_1} + \sum R_2 \underline{i_2} - \sum R_3 \underline{i_3} = \sum \mathcal{E}_{II}$$

$$\begin{bmatrix} 1 & -1 & -1 \\ R_1 & 0 & R_3 \\ 0 & R_2 & -R_3 \end{bmatrix} \begin{bmatrix} \underline{i_1} \\ \underline{i_2} \\ \underline{i_3} \end{bmatrix} = \begin{bmatrix} 0 \\ \mathcal{E}_I \\ \mathcal{E}_{II} \end{bmatrix} ; (R)(i) = \mathcal{E}$$

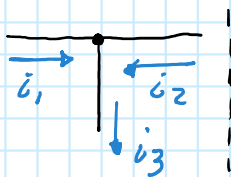
// Valores

$$\mathcal{E}_1 = 50 [\text{V}] ; r_1 = 3 [\Omega] ; R_{11} = 4 [\Omega] ; R_{22} = 7 [\Omega]$$

$$\mathcal{E}_2 = 20 [\text{V}] ; r_2 = 1 [\Omega] ; R_{12} = 5 [\Omega] ; R_3 = 8 [\Omega]$$

$$\mathcal{E}_3 = 30 [\text{V}] ; r_3 = 2 [\Omega] ; R_{21} = 6 [\Omega]$$

// Obteniendo corriente 3



$$i_1 + i_2 - i_3 = 0$$

$$i_3 = i_1 + i_2 =$$

## → Campos Magnéticos

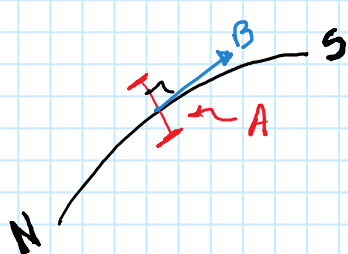
- Es aquel estado modificado del espacio en la vecindad de un iman
- Campo Magnético  $\triangleq \vec{B}$   $\left[ \frac{\text{Weber}}{\text{m}^2} \right]$
- Densidad de Campo Magnético o vector inducción magnético
- Líneas de Campo  $N \rightarrow S$

**NOTA** ① Los polos magnéticos no se pueden separar

② El campo magnético se puede representarse gráficamente con líneas conocidas como líneas de inducción

Además, el campo magnético es directamente proporcional a la cantidad de líneas de inducción

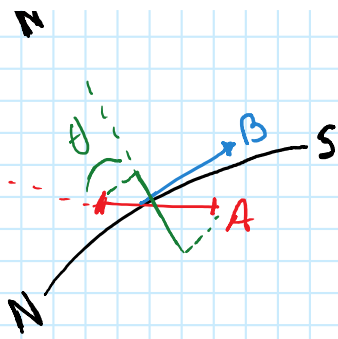
Las líneas de inducción deben dar la dirección del campo magnético.



$$\begin{aligned}
 N &\sim B \\
 N &\sim A \\
 \therefore N &= k B A
 \end{aligned}$$

## Casos

$A \triangleq$  Perpendicular



$$\begin{aligned} N &\sim B \\ N &\sim A_{\text{proyectorada}} \\ \therefore N &= B A \cos \theta \end{aligned}$$

$A \neq \text{Perpendicular}$

if  $B \neq \text{cte}$  en la superficie

$$\Delta A, \Delta N = B \cdot \Delta A \quad \left| \quad \lim \Delta A \rightarrow 0 \right.$$

$$N = \sum \Delta N \quad \left| \quad \therefore dN = B \cdot dA \right.$$

$$\int dN = \int B \cdot dA$$

$$\Phi = \int B \cdot dA \quad \triangleq \text{Lineas de Inducción o Flujo magnético}$$

$$\therefore N = \Phi$$

$$\Phi = \int B \cdot dA, \quad \int B \cdot dA = 0$$

S. cerrada

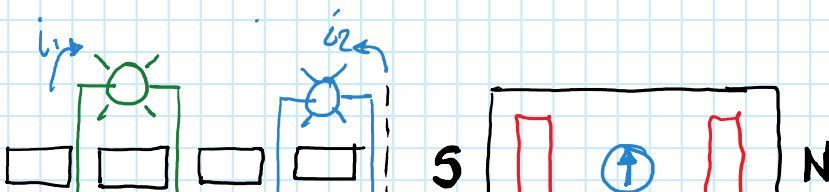
$$\rightarrow \int E \cdot dA = \int (\nabla \cdot E) dA$$

$$\rightarrow \int_{S.C} B \cdot dA = \int (\nabla \cdot B) d\tau = 0 \quad ; \quad \nabla \cdot B = 0$$

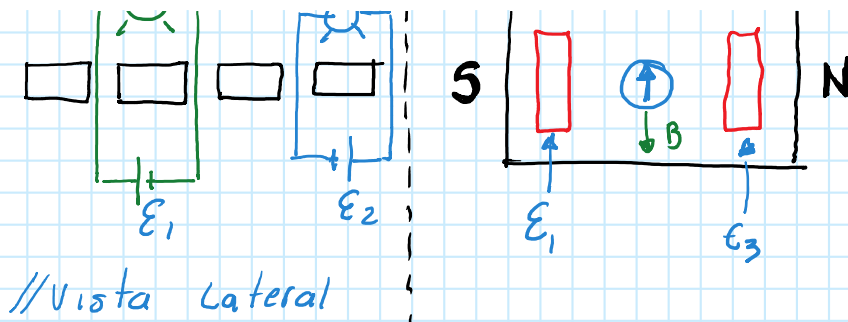
$$\Phi = \int B \cdot dA$$

$$d\Phi = B \cdot dA_{\text{pro}} ; \quad B = - \frac{d\Phi}{dA_{\text{pro}}}$$

Ley de Lenz



Experimento de Oersted



de Oersted

Regla de la  
Mano Derecha

$$\begin{aligned} \bullet B &= f(i) = f(q, v) \\ \bullet F_{\text{mag}} &= f(i, B) = f(i_1, i_2) \end{aligned}$$

- ① El campo magnético lo produce la carga eléctrica en movimiento o bien una corriente eléctrica y a su vez los campos magnéticos producen fuerzas magnéticas.
- Las fuerzas magnéticas se tienen sobre carga en movimiento.