Calcule a área da elipse
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1.$$

Resolução:

$$\begin{split} \frac{A}{2} &= \int_{-a}^{a} \sqrt{b^2 - b^2 (\frac{x}{a})^2} \ dx = ab \int_{-1}^{1} \sqrt{1 - u^2} \ du = -ab \int_{\pi}^{0} \sin^2 \theta \ d\theta = \\ &= -ab \int_{\pi}^{0} \frac{1 - \cos(2\theta)}{2} \ d\theta = -\frac{ab\theta}{2} |_{\pi}^{0} + \frac{ab \sin(2\theta)}{4} |_{\pi}^{0} = ab \frac{\pi}{2} \\ \boxed{A = ab\pi} \end{split}$$

$$x=au,\ u=\cos\theta,\ \theta\in[0,\pi]$$

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