## Demonstração da regra da cadeia.

Sejam f e g funções diferenciáreis,

$$f'(u) = \lim_{\Delta u \to 0} \frac{f(u + \Delta u) - f(u)}{\Delta u} = \lim_{\Delta u \to 0} \frac{\Delta f(u)}{\Delta u};$$

$$g'(x) = \lim_{\Delta x \to 0} \frac{g(x + \Delta x) - g(x)}{\Delta x} = \lim_{\Delta x \to 0} \frac{\Delta g(x)}{\Delta x}.$$

Observemos que  $\Delta g(x) \to 0 \iff \Delta x \to 0$ .

$$(f\circ g)'(x) = \lim_{\Delta g(x)\to 0} \frac{\Delta(f\circ g)(x)}{\Delta g(x)} = \lim_{\Delta g(x)\to 0} \left[\frac{\Delta(f\circ g)(x)}{\Delta x} \cdot \frac{\Delta g(x)}{\Delta g(x)}\right] =$$

$$= \lim_{\Delta g(x) \to 0} \frac{\Delta(f \circ g)(x)}{\Delta g(x)} \cdot \lim_{\Delta g(x) \to 0} \frac{\Delta g(x)}{\Delta x} = f'[g(x)] \cdot g'(x)$$

Quod Erat Demonstrandum.

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