Livro senos e cossenos explícitos.

$$\sin\frac{\pi}{2} = 1$$

$$\cos \frac{\pi}{2} = 0$$

$$\sin\frac{\pi}{4} = \frac{1}{\sqrt{2}}$$

$$\cos\frac{\pi}{4} = \frac{1}{\sqrt{2}}$$

$$\sin\frac{\pi}{8} = \frac{\sqrt{\sqrt{2}-1}}{2^{\frac{3}{4}}}$$

$$\cos\frac{\pi}{8} = \frac{\sqrt{\sqrt{2}+1}}{2^{\frac{3}{4}}}$$

$$\sin\frac{\pi}{16} = \frac{\sqrt{2^{\frac{3}{4}} - \sqrt{\sqrt{2} + 1}}}{2^{\frac{7}{8}}}$$

$$\cos \frac{\pi}{16} = \frac{\sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}{2^{\frac{7}{8}}}$$

$$\sin\frac{\pi}{32} = \frac{\sqrt{2^{\frac{7}{8}} - \sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}}{2^{\frac{15}{16}}}$$

$$\cos\frac{\pi}{32} = \frac{\sqrt{2^{\frac{7}{8}} + \sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}}{2^{\frac{15}{16}}}$$

$$\sin\frac{\pi}{64} = \frac{\sqrt{2\frac{15}{16} - \sqrt{2\frac{7}{8} + \sqrt{2\frac{3}{4} + \sqrt{\sqrt{2} + 1}}}}}{2^{\frac{31}{32}}}$$

$$\cos\frac{\pi}{64} = \frac{\sqrt{2^{\frac{15}{16}} + \sqrt{2^{\frac{7}{8}} + \sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}}}{2^{\frac{31}{32}}}$$

$$\sin\frac{\pi}{128} = \frac{\sqrt{2\frac{\frac{31}{32} - \sqrt{2\frac{15}{16} + \sqrt{2\frac{7}{8} + \sqrt{2\frac{3}{4} + \sqrt{\sqrt{2} + 1}}}}}}{2\frac{63}{64}}$$

$$\cos\frac{\pi}{128} = \frac{\sqrt{2^{\frac{31}{32}} + \sqrt{2^{\frac{15}{16}} + \sqrt{2^{\frac{7}{8}} + \sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}}}{2^{\frac{63}{64}}}$$

$$\sin\frac{\pi}{256} = \frac{\sqrt{2\frac{63}{64} - \sqrt{2\frac{31}{32} + \sqrt{2\frac{15}{16} + \sqrt{2\frac{7}{8} + \sqrt{2\frac{3}{4} + \sqrt{\sqrt{2} + 1}}}}}}{2^{\frac{127}{128}}}$$

$$\cos\frac{\pi}{256} = \frac{\sqrt{2\frac{63}{64} + \sqrt{2\frac{31}{32} + \sqrt{2\frac{15}{16} + \sqrt{2\frac{7}{8} + \sqrt{2\frac{3}{4} + \sqrt{\sqrt{2} + 1}}}}}}{2^{\frac{127}{128}}}$$

$$\sin\frac{\pi}{512} = \frac{\sqrt{2^{\frac{127}{128}} - \sqrt{2^{\frac{63}{64}} + \sqrt{2^{\frac{31}{32}} + \sqrt{2^{\frac{15}{16}} + \sqrt{2^{\frac{7}{8}} + \sqrt{2^{\frac{3}{4}} + \sqrt{\sqrt{2} + 1}}}}}}{2^{\frac{255}{256}}}$$

$$\cos\frac{\pi}{512} = \frac{\sqrt{\frac{2125}{256}} + \sqrt{\frac{252}{256}} + \sqrt{\frac{252}{15}} + \sqrt{\frac{252}{15}} + \sqrt{\frac{25}{15}} + \sqrt{\frac{25}{15}}$$

$$\sin \frac{\pi}{37708} = \frac{2889}{21883} - 2889 + 2888 + 2188 + 2$$

$$\sin\frac{\pi}{192} = \frac{\sqrt{2 - \sqrt{\sqrt{\sqrt{\sqrt{3} + 2} + 2} + 2} + 2}}{2}$$

$$\cos\frac{\pi}{192} = \frac{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{3}+2}+2}+2}+2}+2}}{2}$$

$$\sin\frac{\pi}{384} = \frac{\sqrt{2 - \sqrt{\sqrt{\sqrt{\sqrt{3} + 2} + 2 + 2 + 2 + 2 + 2 + 2}}}}{2}$$

$$\sin\frac{\pi}{768} = \frac{\sqrt{2 - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{3+2} + 2} + 2} + 2} + 2} + 2} + 2}}{2}$$

$$\sin\frac{\pi}{1536} = \frac{\sqrt{2 - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{3} + 2} + 2} + 2 + 2 + 2 + 2 + 2}}}}}{2}$$

$$\cos\frac{\pi}{12288} = \frac{2}{2}$$

$$\sin\frac{\pi}{24576} = \frac{2}{2}$$

$$\sin\frac{\pi}{49152} = \frac{2}{2}$$

$$\cos\frac{\pi}{49152} = \frac{2}{2}$$

$$\cos\frac{\pi}{38304} = \frac{2}{2}$$

 $\sin\frac{\pi}{20} = \frac{\sqrt{2^{\frac{3}{2}} - \sqrt{\sqrt{5} + 5}}}{2^{\frac{5}{4}}}$ 

 $\cos\frac{\pi}{20} = \frac{\sqrt{\sqrt{\sqrt{5}+5}+2^{\frac{3}{2}}}}{2^{\frac{5}{4}}}$ 

$$\sin \frac{\pi}{40} = \frac{\sqrt{2\frac{2}{4} - \sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}{2\frac{8}{8}}}{2\frac{8}{8}}$$

$$\cos \frac{\pi}{40} = \frac{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}} + 2\frac{5}{4}}}}{2\frac{15}{16}}$$

$$\sin \frac{\pi}{80} = \frac{\sqrt{2\frac{2}{8} - \sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{5}{4}}}}}{2\frac{15}{16}}$$

$$\cos \frac{\pi}{80} = \frac{\sqrt{2\frac{17}{16} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}{2\frac{15}{16}}$$

$$\sin \frac{\pi}{160} = \frac{\sqrt{2\frac{17}{16} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}{2\frac{33}{32}}$$

$$\cos \frac{\pi}{160} = \frac{\sqrt{2\frac{33}{2} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}{2\frac{33}{32}}$$

$$\sin \frac{\pi}{320} = \frac{\sqrt{2\frac{33}{2} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}{2\frac{33}{64}}$$

$$\cos \frac{\pi}{320} = \frac{\sqrt{2\frac{33}{2} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}{2\frac{364}{64}}$$

$$\sin \frac{\pi}{640} = \frac{\sqrt{2\frac{63}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}{2\frac{128}{128}}$$

$$\cos \frac{\pi}{640} = \frac{\sqrt{2\frac{63}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}{2\frac{128}{128}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}{2\frac{128}{128}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}{2\frac{128}{128}}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}}{2\frac{25}{2}}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}}{2\frac{25}{2}}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}}{2\frac{25}{2}}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}}{2\frac{25}{2}}}$$

$$\sin \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2} + 2\frac{3}{4}}}}}}}}}}{2\frac{25}{2}}}$$

$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{23}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}}}{2\frac{25}{2}}}$$

$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}}}{2\frac{25}{2}}}}$$

$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}}}}{2\frac{25}{2}}}}$$

$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}}}{2\frac{25}{2}}}}$$

$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}{2\frac{25}{2}}}}$$

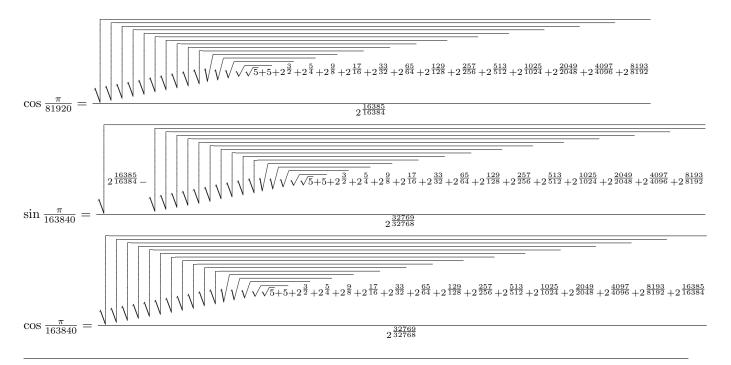
$$\cos \frac{\pi}{1280} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}{2\frac{25}{2}}}}$$

$$\cos \frac{\pi}{1280}} = \frac{\sqrt{2\frac{25}{2} - \sqrt{\sqrt{\sqrt{5+5} + 2\frac{3}{2}}}}}}}}{2\frac{25}{2}}}}$$

$$\frac{25}{2}}$$

$$\frac{25$$

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\frac{\frac{1}{5+5+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}}}{5+5+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}
\frac{\frac{1}{2}}{5+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{8}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}+2^{\frac{513}{512}}
                          \frac{\frac{1}{\sqrt{5}+5}+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}+2^{\frac{513}{512}}
                   \frac{2}{1024} + 2\frac{3}{2} + 2\frac{5}{4} + 2\frac{9}{8} + 2\frac{17}{16} + 2\frac{33}{32} + 2\frac{65}{64} + 2\frac{129}{128} + 2\frac{257}{256} + 2\frac{513}{512} + 2\frac{1025}{1024}
     \sqrt[4]{\sqrt{\sqrt{\sqrt{5+5}+2^{\frac{3}{2}}}+2^{\frac{5}{4}}}+2^{\frac{9}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}+2^{\frac{513}{512}}+2^{\frac{1025}{1024}}}
      \frac{\frac{1}{\sqrt{5+5+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}}} + 2^{\frac{17}{16}} + 2^{\frac{33}{32}} + 2^{\frac{65}{64}} + 2^{\frac{129}{128}} + 2^{\frac{257}{256}} + 2^{\frac{513}{512}} + 2^{\frac{1025}{1024}} + 2^{\frac{2049}{2048}}
                                         \frac{1}{\sqrt{5+5}+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}+2^{\frac{513}{512}}+2^{\frac{1025}{1024}}+2^{\frac{2049}{2048}}
           \frac{}{\sqrt{5+5}+2^{\frac{3}{2}}+2^{\frac{5}{4}}+2^{\frac{9}{8}}+2^{\frac{17}{16}}+2^{\frac{33}{32}}+2^{\frac{65}{64}}+2^{\frac{129}{128}}+2^{\frac{257}{256}}+2^{\frac{513}{512}}+2^{\frac{1025}{1024}}+2^{\frac{2049}{2048}}+2^{\frac{4097}{4096}}
                                                                                    2^{\frac{8193}{8192}}
                              \overline{\sqrt{\sqrt{5} + 5 + 2^{\frac{3}{2}} + 2^{\frac{5}{4}}} + 2^{\frac{8}{8}} + 2^{\frac{17}{16}} + 2^{\frac{33}{32}} + 2^{\frac{65}{64}} + 2^{\frac{129}{128}} + 2^{\frac{257}{256}} + 2^{\frac{513}{512}} + 2^{\frac{1025}{1024}} + 2^{\frac{2049}{2048}} + 2^{\frac{4097}{4096}}
                                                                                                  2\frac{16385}{16384}
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