## Example-rounding-single-precision

## January 21, 2019

```
In [1]: import numpy as np
       def round_floats(vals, nbits=23):
           mask = 0xFFFF_FFFF << (23 - nbits)</pre>
            # Binary conversion and copy
           uvals = np.array( vals, dtype=np.float32 ).view(np.int32)
           # Apply mask
           uvals &= mask
           # Convert to single precision
           result = uvals.view(np.float32)
           return result
In [2]: # From 0. to 50.
       vals = np.array( 50*np.random.rand(1000000), dtype=np.float32 )
In [3]: import matplotlib.pyplot as plt
       %matplotlib inline
        # Example with 14 bits
       plt.hist( ( vals - round_floats( vals, nbits=14 ) ), bins=100 )
Out[3]: (array([53023., 38955., 35329., 29659., 29542., 28888., 24147., 22536.,
               22357., 24181., 22590., 22674., 19259., 16838., 15837., 16285.,
               16142., 15704., 17740., 16067., 16490., 15957., 16901., 16045.,
                15994., 10011., 9842., 10938., 9783., 9848.,
                                                               9877., 10251..
                9730.,
                        9686., 9851., 9699., 10999., 9817.,
                                                               9818.,
                        9904., 9839., 9873., 9625., 11091.,
               10454.,
                                                               9775.,
                        9765., 4170., 3569., 3544., 3482.,
                                                               4156.,
                9867.,
                                                                       3609.,
                                3502., 3627., 3364., 3493.,
                3448.,
                        3613.,
                                                                3502., 4112.,
                                                               3598., 3649.,
                3635.,
                       3541., 3537., 3436., 3514., 3505.,
                       3551., 3583., 3457., 3422., 3574.,
                                                               3546., 3548.,
                4268.,
                3570.,
                        4128., 3490., 3542., 3545., 3552.,
                                                                3593., 3474.,
                3595., 3458., 4045., 3586.,
                                                3541., 3506.,
                                                               3475., 3563.,
                3532., 3524., 3430., 4238.]),
        array([0.0000000e+00, 1.9493104e-05, 3.8986207e-05, 5.8479309e-05,
               7.7972414e-05, 9.7465512e-05, 1.1695862e-04, 1.3645172e-04,
               1.5594483e-04, 1.7543793e-04, 1.9493102e-04, 2.1442413e-04,
               2.3391724e-04, 2.5341034e-04, 2.7290345e-04, 2.9239655e-04,
```

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3.1188966e-04, 3.3138276e-04, 3.5087587e-04, 3.7036894e-04,
       3.8986205e-04, 4.0935515e-04, 4.2884826e-04, 4.4834136e-04,
       4.6783447e-04, 4.8732758e-04, 5.0682068e-04, 5.2631379e-04,
       5.4580689e-04, 5.6530000e-04, 5.8479310e-04, 6.0428621e-04,
       6.2377931e-04, 6.4327242e-04, 6.6276552e-04, 6.8225863e-04,
       7.0175173e-04, 7.2124484e-04, 7.4073789e-04, 7.6023099e-04,
       7.7972410e-04, 7.9921720e-04, 8.1871031e-04, 8.3820341e-04,
       8.5769652e-04, 8.7718962e-04, 8.9668273e-04, 9.1617584e-04,
       9.3566894e-04, 9.5516205e-04, 9.7465515e-04, 9.9414820e-04,
       1.0136414e-03, 1.0331344e-03, 1.0526276e-03, 1.0721206e-03,
       1.0916138e-03, 1.1111068e-03, 1.1306000e-03, 1.1500930e-03,
       1.1695862e-03, 1.1890793e-03, 1.2085724e-03, 1.2280655e-03,
       1.2475586e-03, 1.2670517e-03, 1.2865448e-03, 1.3060379e-03,
       1.3255310e-03, 1.3450241e-03, 1.3645173e-03, 1.3840103e-03,
       1.4035035e-03, 1.4229965e-03, 1.4424897e-03, 1.4619827e-03,
       1.4814758e-03, 1.5009689e-03, 1.5204620e-03, 1.5399551e-03,
       1.5594482e-03, 1.5789414e-03, 1.5984344e-03, 1.6179276e-03,
       1.6374206e-03, 1.6569138e-03, 1.6764068e-03, 1.6959000e-03,
       1.7153930e-03, 1.7348862e-03, 1.7543792e-03, 1.7738724e-03,
       1.7933655e-03, 1.8128586e-03, 1.8323517e-03, 1.8518448e-03,
       1.8713379e-03, 1.8908310e-03, 1.9103241e-03, 1.9298173e-03,
       1.9493103e-03], dtype=float32),
<a list of 100 Patch objects>)
```



0.000000.000250.000500.000750.001000.001250.001500.001750.00200

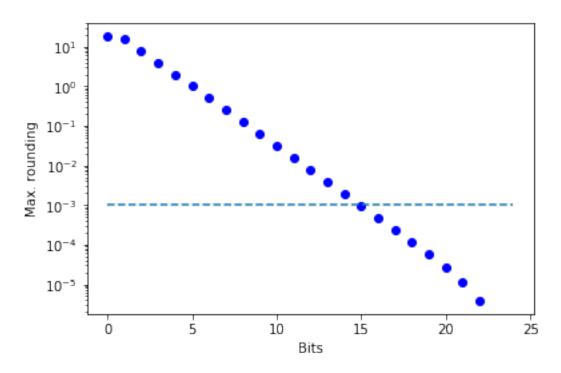
```
for i in range(24):
    bits.append( i )
    rounded = round_floats( vals, nbits=i )
    max_vals.append( np.max( vals - rounded ) )

In [5]: plt.plot(bits, max_vals, 'bo')
    plt.yscale('log')
    #plt.axis(ymin=0., ymax=1.)

precision = 0.001

xlin = np.linspace(0,24,100)
    plt.plot( xlin, [precision for i in range(len(xlin))], '---')

plt.xlabel( 'Bits' )
    plt.ylabel( 'Max. rounding' )
Out[5]: Text(0, 0.5, 'Max. rounding')
```



```
In [6]: max_vals_arr = np.asarray( max_vals )
    sel = max_vals_arr < precision
    print ( sel )
    print ( max_vals_arr[ sel ] )
    print ( np.array( bits )[sel] )</pre>
```

[False False False