$$\begin{array}{c|cccc} x_1 & 3 & -1x_5 - 2x_7 \\ x_3 & -4 & +1x_2 - 1x_4 & -1x_7 \\ x_6 & 7 & -1x_2 & -2x_5 \\ \hline z & 1 & -1x_2 + 2x_4 + 3x_5 + 1x_7 \\ \end{array}$$

#### 1.1 Initialization Phase: Aux Problem Solving

 $x_3$  leaves

$$\begin{array}{c|cccc} x_1 & 7 & -1x_2 + 1x_4 - 1x_5 - 1x_7 + 1x_3 \\ x_0 & 4 & -1x_2 + 1x_4 & +1x_7 + 1x_3 \\ x_6 & 11 & -2x_2 + 1x_4 - 2x_5 + 1x_7 + 1x_3 \\ \hline z & -4 & +1x_2 - 1x_4 & -1x_7 - 1x_3 \\ \end{array}$$

 $x_2$  enters and  $x_0$  leaves

Final Dictionary

### 1.2 Optimization Phase

Problem is feasible Initialization phase yields a zero answer

$$\begin{array}{c|cccc} x_1 & 3 & -1x_5 - 2x_7 \\ x_2 & 4 & +1x_4 & +1x_7 + 1x_3 \\ x_6 & 3 & -1x_4 - 2x_5 - 1x_7 - 1x_3 \\ \hline z & -3 & +1x_4 + 3x_5 & -1x_3 \\ \end{array}$$

$$\begin{array}{c|cccc} x_3 & -1 & +1x_1 - 1x_2 \\ x_4 & -2 & +1x_1 + 2x_2 \\ \hline x_5 & 1 & -1x_2 \\ \hline z & 0 & -2x_1 - 1x_2 \end{array}$$

#### 2.1 Initialization Phase: Aux Problem Solving

$$\begin{array}{c|cccc} x_3 & -1 & +1x_1 - 1x_2 + 1x_0 \\ x_4 & -2 & +1x_1 + 2x_2 + 1x_0 \\ x_5 & 1 & -1x_2 + 1x_0 \\ \hline z & 0 & -1x_0 \\ \end{array}$$

 $x_4$  leaves

$$\begin{array}{c|cccc} x_3 & 1 & -3x_2 + 1x_4 \\ x_0 & 2 & -1x_1 - 2x_2 + 1x_4 \\ x_5 & 3 & -1x_1 - 3x_2 + 1x_4 \\ \hline z & -2 & +1x_1 + 2x_2 - 1x_4 \\ \end{array}$$

 $x_1$  enters and  $x_0$  leaves

$$\begin{array}{c|cccc} x_3 & 1 & -3x_2 + 1x_4 \\ x_1 & 2 & -1x_0 - 2x_2 + 1x_4 \\ x_5 & 1 & +1x_0 - 1x_2 \\ \hline z & 0 & -1x_0 \end{array}$$

Final Dictionary

#### 2.2 Optimization Phase

Problem is feasible Initialization phase yields a zero answer

$$\begin{array}{c|cccc} x_3 & 1 & -3x_2 + 1x_4 \\ x_1 & 2 & -2x_2 + 1x_4 \\ x_5 & 1 & -1x_2 \\ \hline z & -4 & +3x_2 - 2x_4 \end{array}$$

$$\begin{array}{c|ccccc} x_4 & 10 & -1x_1 & +1x_3 \\ x_5 & 12 & +1x_2 -1x_3 \\ x_6 & 14 & +1x_1 -1x_2 -1x_3 \\ x_7 & -40 & +1x_3 \\ x_8 & -25 & +1x_2 \\ x_9 & -15 & +1x_1 \\ \hline z & 0 & +2x_1 -3x_2 +1x_3 \\ \end{array}$$

#### 3.1 Initialization Phase: Aux Problem Solving

 $x_7$  leaves

 $x_3$  enters and  $x_8$  leaves

$$\begin{array}{c|cccc} x_4 & 50 & -1x_1 & +1x_7 \\ x_5 & 22 & -1x_2 + 2x_8 - 1x_7 \\ x_6 & 24 & +1x_1 - 3x_2 + 2x_8 - 1x_7 \\ x_0 & 25 & -1x_2 + 1x_8 \\ x_3 & 15 & +1x_2 - 1x_8 + 1x_7 \\ x_9 & 10 & +1x_1 - 1x_2 + 1x_8 \\ \hline z & -25 & +1x_2 - 1x_8 \\ \end{array}$$

 $x_2$  enters and  $x_6$  leaves

 $x_1$  enters and  $x_5$  leaves

$$\begin{array}{c|ccccc} x_4 & 8 & +3x_5 - 1x_6 - 4x_8 + 3x_7 \\ x_1 & 42 & -3x_5 + 1x_6 + 4x_8 - 2x_7 \\ x_2 & 22 & -1x_5 & +2x_8 - 1x_7 \\ x_0 & 3 & +1x_5 & -1x_8 + 1x_7 \\ x_3 & 37 & -1x_5 & +1x_8 \\ x_9 & 30 & -2x_5 + 1x_6 + 3x_8 - 1x_7 \\ \hline z & -3 & -1x_5 & +1x_8 - 1x_7 \\ \end{array}$$

 $x_8$  enters and  $x_4$  leaves

Final Dictionary

Problem is Infeasible Initialization phase yields negative answer

### 4 Dictionary # 4

$$\begin{array}{c|cccc} x_4 & 1 & -1x_1 \\ x_3 & -2 & -1x_2 + 2x_1 \\ x_5 & 0 & -2x_2 \\ \hline z & 1 & +3x_1 \\ \hline \end{array}$$

$$\begin{array}{c|cccc} x_4 & 1 & -1x_1 + 1x_0 \\ x_3 & -2 & -1x_2 + 2x_1 + 1x_0 \\ x_5 & 0 & -2x_2 & +1x_0 \\ \hline z & 0 & -1x_0 \\ \hline \end{array}$$

 $x_3$  leaves

$$\begin{array}{c|cccc} x_4 & 3 & +1x_2 - 3x_1 + 1x_3 \\ x_0 & 2 & +1x_2 - 2x_1 + 1x_3 \\ x_5 & 2 & -1x_2 - 2x_1 + 1x_3 \\ \hline z & -2 & -1x_2 + 2x_1 - 1x_3 \\ \end{array}$$

 $x_1$  enters and  $x_0$  leaves

$$\begin{array}{c|cccc} x_4 & 0 & -0.5x_2 + 1.5x_0 - 0.5x_3 \\ x_1 & 1 & +0.5x_2 - 0.5x_0 + 0.5x_3 \\ \hline x_5 & 0 & -2x_2 & +1x_0 \\ \hline z & 0 & -1x_0 \\ \hline \end{array}$$

Final Dictionary

### 4.2 Optimization Phase

Problem is feasible Initialization phase yields a zero answer

$$\begin{array}{c|cccc} x_4 & 0 & -0.5x_2 - 0.5x_3 \\ x_1 & 1 & +0.5x_2 + 0.5x_3 \\ x_5 & 0 & -2x_2 \\ \hline z & 4 & +1.5x_2 + 1.5x_3 \end{array}$$

# 5 Dictionary # 5

$$\begin{array}{c|cccc} x_6 & -6 & -1x_4 - 3x_3 + 2x_1 \\ x_2 & -12 & -6x_3 - 1x_1 - 1x_5 \\ x_8 & 3 & +1x_4 & -1x_1 + 5x_5 \\ x_9 & 2 & -1x_5 \\ x_7 & 4 & -1x_3 \\ \hline z & 0 & +2x_4 + 1x_3 - 3x_1 + 4x_5 \\ \end{array}$$

$$\begin{array}{c|ccccc} x_6 & -6 & -1x_4 - 3x_3 + 2x_1 & +1x_0 \\ x_2 & -12 & -6x_3 - 1x_1 - 1x_5 + 1x_0 \\ x_8 & 3 & +1x_4 & -1x_1 + 5x_5 + 1x_0 \\ x_9 & 2 & -1x_5 + 1x_0 \\ x_7 & 4 & -1x_3 & +1x_0 \\ \hline z & 0 & -1x_0 \\ \end{array}$$

 $x_2$  leaves

$$\begin{array}{c|cccc} x_6 & 6 & -1x_4 + 3x_3 + 3x_1 + 1x_5 + 1x_2 \\ x_0 & 12 & +6x_3 + 1x_1 + 1x_5 + 1x_2 \\ x_8 & 15 & +1x_4 + 6x_3 & +6x_5 + 1x_2 \\ x_9 & 14 & +6x_3 + 1x_1 & +1x_2 \\ x_7 & 16 & +5x_3 + 1x_1 + 1x_5 + 1x_2 \\ \hline z & -12 & -6x_3 - 1x_1 - 1x_5 - 1x_2 \\ \end{array}$$

Final Dictionary Problem is Infeasible Initialization phase yields negative answer

# 6 Dictionary # 6

$$\begin{array}{c|cccc} x_4 & 0 & -1x_5 \\ x_6 & 2 & +1x_3 \\ x_2 & 1 & -2x_5 + 2x_3 \\ x_1 & -3 & +1x_5 + 1x_3 \\ \hline z & 0 & +6x_5 - 5x_3 \\ \end{array}$$

#### 6.1 Initialization Phase: Aux Problem Solving

$$\begin{array}{c|cccc} x_4 & 0 & -1x_5 & +1x_0 \\ x_6 & 2 & +1x_3 + 1x_0 \\ x_2 & 1 & -2x_5 + 2x_3 + 1x_0 \\ x_1 & -3 & +1x_5 + 1x_3 + 1x_0 \\ \hline z & 0 & -1x_0 \end{array}$$

 $x_1$  leaves

$$\begin{array}{c|cccc} x_4 & 3 & -2x_5 - 1x_3 + 1x_1 \\ x_6 & 5 & -1x_5 & +1x_1 \\ x_2 & 4 & -3x_5 + 1x_3 + 1x_1 \\ x_0 & 3 & -1x_5 - 1x_3 + 1x_1 \\ \hline z & -3 & +1x_5 + 1x_3 - 1x_1 \\ \end{array}$$

 $x_3$  enters and  $x_0$  leaves

$$\begin{array}{c|cccc} x_4 & 0 & -1x_5 + 1x_0 \\ x_6 & 5 & -1x_5 & +1x_1 \\ x_2 & 7 & -4x_5 - 1x_0 + 2x_1 \\ x_3 & 3 & -1x_5 - 1x_0 + 1x_1 \\ \hline z & 0 & -1x_0 \end{array}$$

Final Dictionary Problem is feasible Initialization phase yields a zero answer

#### 6.2 Optimization Phase

$$\begin{array}{c|cccc} x_4 & 0 & -1x_5 \\ x_6 & 5 & -1x_5 + 1x_1 \\ x_2 & 7 & -4x_5 + 2x_1 \\ x_3 & 3 & -1x_5 + 1x_1 \\ \hline z & -15 & +11x_5 - 5x_1 \end{array}$$

# 7 Dictionary # 7

 $x_7$  leaves

 $x_2$  enters and  $x_8$  leaves

$$\begin{array}{c|ccccc} x_4 & 4 & +1x_1 + 3x_8 - 2x_3 - 2x_7 \\ x_5 & 27 & +1x_1 & -2x_3 + 1x_7 \\ x_6 & 20 & +1x_3 + 1x_7 \\ x_0 & 8 & +1x_8 - 1x_3 \\ x_2 & 7 & -1x_8 + 1x_3 + 1x_7 \\ x_9 & 13 & +1x_1 + 1x_8 - 1x_3 \\ \hline z & -8 & -1x_8 + 1x_3 \\ \hline \end{array}$$

 $x_3$  enters and  $x_4$  leaves

 $x_1$  enters and  $x_0$  leaves

$$\begin{array}{c|cccc} x_3 & 8 & -1x_0 + 1x_8 \\ x_5 & 23 & -3x_8 + 1x_4 + 3x_7 \\ x_6 & 28 & -1x_0 + 1x_8 & +1x_7 \\ x_1 & 12 & -2x_0 - 1x_8 + 1x_4 + 2x_7 \\ x_2 & 15 & -1x_0 & +1x_7 \\ x_9 & 17 & -1x_0 - 1x_8 + 1x_4 + 2x_7 \\ \hline z & 0 & -1x_0 \end{array}$$

#### Final Dictionary

Problem is feasible Initialization phase yields a zero answer

#### 7.2 Optimization Phase

# 8 Dictionary 8

 $x_5$  leaves

 $x_1$  enters and  $x_9$  leaves

Final Dictionary Problem is Infeasible Initialization phase yields negative answer

#### 9.1 Initialization Phase: Aux Problem Solving

 $x_9$  leaves

 $x_3$  enters and  $x_4$  leaves

 $x_1$  enters and  $x_6$  leaves

```
0.330636903543
                       -0.038911x_6 + 0.298792x_2 - 0.060414x_4 + 0.099324x_9
x_3
     1.6254454229
                       -0.101167x_6 - 8.796826x_2 + 0.658714x_4 + 0.442453x_9
x_5
    0.755068605366
                       -0.116732x_6 - 0.998362x_2 + 0.081917x_4 + 0.034815x_9
x_1
                       +0.350195x_6 +0.068769x_2 +0.938460x_4 -0.288655x_9
     5.26900471022
x_7
     5.3170182265
                       -0.210117x_6 - 4.733893x_2 + 1.305345x_4 - 0.095228x_9
x_8
                       +0.221790x_6 -1.850481x_2 +0.475937x_4 +0.302273x_9
     2.69694859717
x_0
                       -0.221790x_6 + 1.850481x_2 - 0.475937x_4 - 0.302273x_9
    -2.69694859717
```

 $x_2$  enters and  $x_5$  leaves

```
0.385846550685
                      -0.042347x_6 -0.033966x_5 -0.038040x_4 +0.114352x_9
x_3
     0.18477635846
                       -0.0115x_6 -0.113677x_5 + 0.074881x_4 + 0.050297x_9
x_2
    0.570594972867
                      -0.105250x_6 + 0.113491x_5 + 0.007159x_4 -0.0154x_9
x_1
     5.28171163243
                      +0.349404x_6 -0.007818x_5 +0.943609x_4 -0.285196x_9
x_7
                      -0.155675x_6 + 0.538137x_5 + 0.950867x_4 - 0.333329x_9
     4.44230669842
x_8
     2.35502340827
                      +0.243071x_6 +0.210358x_5 +0.337371x_4 +0.2092x_9
x_0
     -2.35502340827
                      -0.243071x_6 - 0.210358x_5 - 0.337371x_4 - 0.2092x_9
```

Final Dictionary

# 10 Dictionary # 10

$$\begin{array}{c|cccc} x_4 & 3 & +3x_2 - 1x_3 - 1x_1 \\ x_7 & -4 & -1x_3 + 1x_1 \\ x_6 & -20 & -1x_2 + 1x_3 + 4x_1 \\ x_5 & 11 & -1x_2 & -2x_1 \\ x_8 & -4 & -1x_3 + 1x_1 \\ \hline z & 0 & +1x_2 + 2x_3 - 2x_1 \end{array}$$

#### 10.1 Initialization Phase: Aux Problem Solving

$$\begin{array}{c|cccc} x_4 & 3 & +3x_2 - 1x_3 - 1x_1 + 1x_0 \\ x_7 & -4 & -1x_3 + 1x_1 + 1x_0 \\ x_6 & -20 & -1x_2 + 1x_3 + 4x_1 + 1x_0 \\ x_5 & 11 & -1x_2 & -2x_1 + 1x_0 \\ x_8 & -4 & -1x_3 + 1x_1 + 1x_0 \\ \hline z & 0 & -1x_0 \\ \end{array}$$

 $x_6$  leaves

 $x_1$  enters and  $x_4$  leaves

$$\begin{array}{c|cccc} x_1 & 4.6 & +0.8x_2 -0.4x_3 -0.2x_4 +0.2x_6 \\ x_7 & 2.2 & -1.4x_2 -0.8x_3 +0.6x_4 +0.4x_6 \\ x_0 & 1.6 & -2.2x_2 +0.6x_3 +0.8x_4 +0.2x_6 \\ x_5 & 3.4 & -4.8x_2 +1.4x_3 +1.2x_4 -0.2x_6 \\ x_8 & 2.2 & -1.4x_2 -0.8x_3 +0.6x_4 +0.4x_6 \\ \hline z & -1.6 & +2.2x_2 -0.6x_3 -0.8x_4 -0.2x_6 \end{array}$$

 $x_2$  enters and  $x_5$  leaves

 $x_3$  enters and  $x_0$  leaves

Final Dictionary Problem is feasible Initialization phase yields a zero answer