Tutorial

2 more challenges to get your next star!



Problem Submissions Leaderboard Editorial 🛆

Terms you'll find helpful in completing today's challenge are outlined below.

Day 4: Geometric Distribution I ☆

Negative Binomial Experiment

A negative binomial experiment is a statistical experiment that has the following properties:

- The experiment consists of n repeated trials.
- The trials are independent.
- The outcome of each trial is either success (\boldsymbol{s}) or failure (\boldsymbol{f}).
- P(s) is the same for every trial.
- The experiment continues until $m{x}$ successes are observed.

If X is the number of experiments until the x^{th} success occurs, then X is a discrete random variable called a negative binomial.

Negative Binomial Distribution

Consider the following probability mass function:

$$b^*(x,n,p) = inom{n-1}{x-1} \cdot p^x \cdot q^{(n-x)}$$

The function above is negative binomial and has the following properties:

- The number of successes to be observed is **2**.
- The total number of trials is **n**.
- The probability of success of **1** trial is **p**
- The probability of failure of ${f 1}$ trial ${m q}$, where ${m q}={f 1}-{m p}$.
- $b^*(x,n,p)$ is the negative binomial probability, meaning the probability of having x-1 successes after n-1 trials and having x successes after n-1 trials.

Note: Recall that $\binom{n}{x} = \frac{n!}{x!(n-x)!}$. For further review, see the Combinations and Permutations Tutorial.

Geometric Distribution

The geometric distribution is a special case of the negative binomial distribution that deals with the number of Bernoulli trials required to get a success (i.e., counting the number of failures before the first success). Recall that \boldsymbol{X} is the number of successes in \boldsymbol{n} independent Bernoulli trials, so for each \boldsymbol{i} (where

 $1 \leq i \leq n$):

$$X_i = \left\{ egin{array}{ll} 1 & ext{if the } i^{th} ext{ trial is a success} \ 0 & ext{otherwise.} \end{array}
ight.$$

The geometric distribution is a negative binomial distribution where the number of successes is 1. We express this with the following formula:

$$g(n,p)=q^{(n-1)}\cdot p$$

Example

Bob is a high school basketball player. He is a 70% free throw shooter, meaning his probability of making a free throw is 0.70. What is the probability that Bob makes his first free throw on his fifth shot?

For this experiment, n=5, p=0.7 and q=0.3, So, $g(n=5,p=0.7)=0.3^40.7=0.00567$



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