## December 1, 2021

## Task 4

Consider the cover

$$C = \{i \mid y_i^* = 1\}.$$

This is indeed a cover, since the  $\mathbf{y}^*$  solution must satisfy

$$\sum_{i \in C} w_i = \sum_{i \in C} w_i + \sum_{i \notin C} w_i(0) = \sum_{i=1}^n w_i y_i^* > c.$$

Now if  $\sum_{i=1}^{n} (1-x_i^*)y_i^* < 1$ , we can make the following inference

$$\sum_{i=1}^{n} (1 - x_i^*) y_i^* < 1$$

$$\sum_{i \in C} (1 - x_i^*) < 1$$

$$|C| - \sum_{i \in C} x_i^* < 1$$

$$- \sum_{i \in C} x_i^* < 1 - |C|$$

$$\sum_{i \in C} x_i^* > |C| - 1$$

Therefore  $\mathbf{x}^*$  violates the inequality corresponding to C. So to construct a cover, one must simply choose the variables where  $y_i^* = 1$ .