

# FRICTION

between Solids.

friction between liquids (viscosity)

When there is no relative motion between surfaces.  
the force of friction acting in this case is called static friction

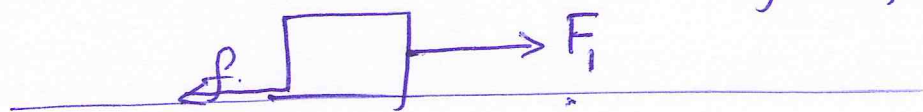
$\mu_s$  ← coefficient of static friction

When there is relative motion between the solid surfaces  
the force of friction acting in this case is called kinetic friction

$\mu_k$  ← coefficient of kinetic friction

- 1) If body is at rest and no force is acting on the body, then force of friction is zero.
- 2) If force is applied ~~to~~ to pull the body and it does not move, the friction acts in a direction opposite to tendency of motion with a magnitude equal to the force applied.

$$f = F_i$$



- 3) If the force applied on the body is increased, the force of friction will adjust to the magnitude of force applied, till the point the body starts moving,

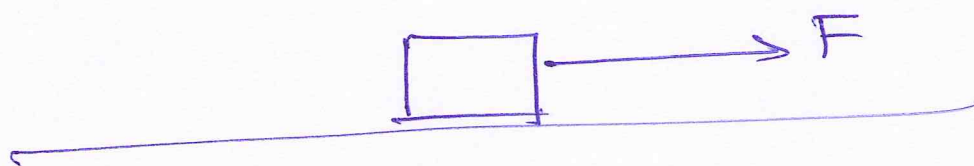
and after that

$$f_{\max} = \mu N$$

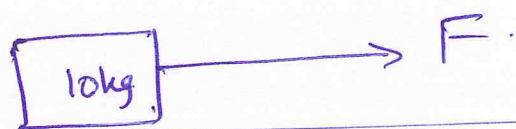
$\mu$  is coefficient of friction.

$$f \leq \mu N$$

$$f_{\max} = 5 \text{ N}$$



F	f
2 N	2 N
4 N	4 N
5 N	5 N
6 N	5 N



$$f_{\max} = 100 \times 0.05 = 5 \text{ N}$$

$$\mu_s = 0.05, \mu_k = 0.04$$

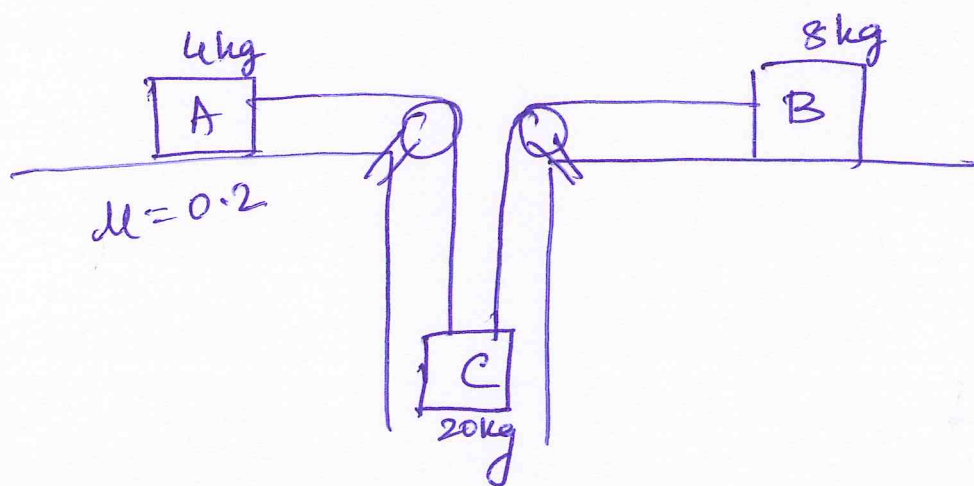
F	f	a.
4 N	4 N	0
5 N	5 N	0
6 N	4 N	0.2 m/s <sup>2</sup>
10 N	4 N	0.6 m/s <sup>2</sup>

$$F - f_k = ma$$

$$F - f_k = ma$$

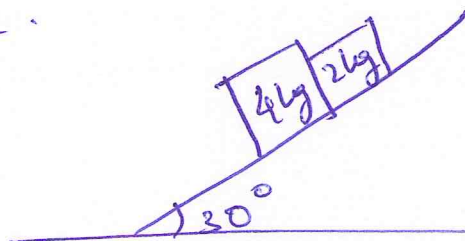
Q1 Consider the situation shown in figure.

The ~~block~~ block B moves on a frictionless surface, while coefficient of friction between A & surface on which it moves is 0.2. Find acceleration with which the masses move and also the tension in string. ( $g = 10 \text{ m/s}^2$ )



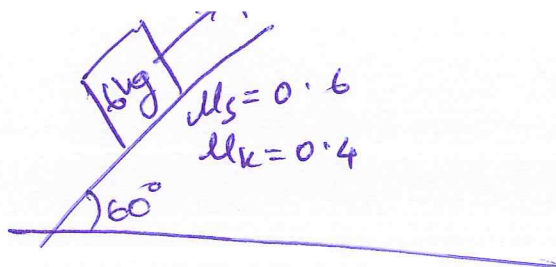
Q2

Push a block of mass  $4 \text{ kg}$ . If two blocks in contact sliding down an inclined surface of inclination  $30^\circ$ . The friction coefficient between the block of mass  $2 \text{ kg}$  and incline is  $\mu_1 = 0.2$  & between  $4 \text{ kg}$  and incline is  $\mu_2 = 0.3$ . Find acceleration of  $2 \text{ kg}$  block.





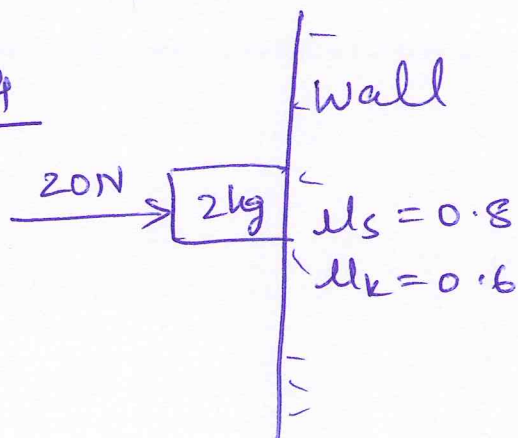
Q3



Find F

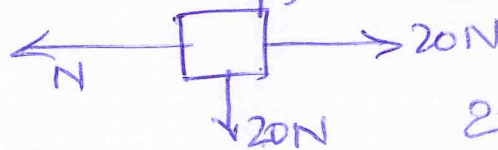
- to keep block stationary
- move block downwards with const velocity
- move block upwards with acceleration  $4\text{ m/s}^2$

Q4



Find acceleration &amp;

force of friction =  $20 \times 0.8 = 16\text{ N}$   
 $f_s^{\text{max}} = 20 \times 0.8 = 16\text{ N}$   
 $f_k^{\text{max}} = 20 \times 0.6 = 12\text{ N}$   
 $N = 20\text{ N}$

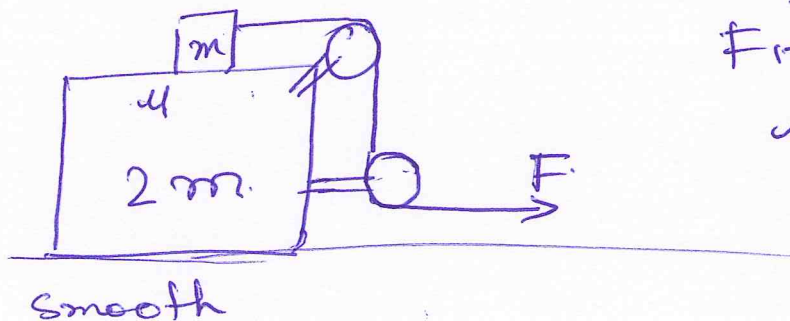


$$20 - 12 = 2a$$

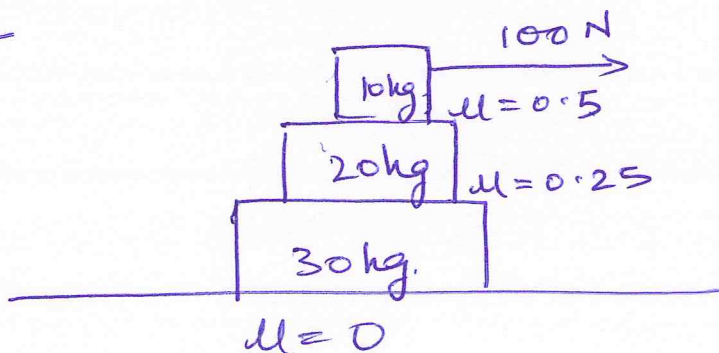
$$a = 4\text{ m/s}^2$$

Find ~~min~~ minimum  $\mu$  to avoid slipping

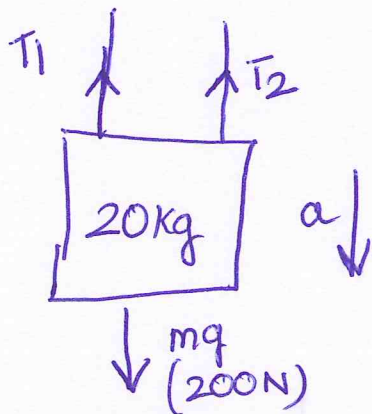
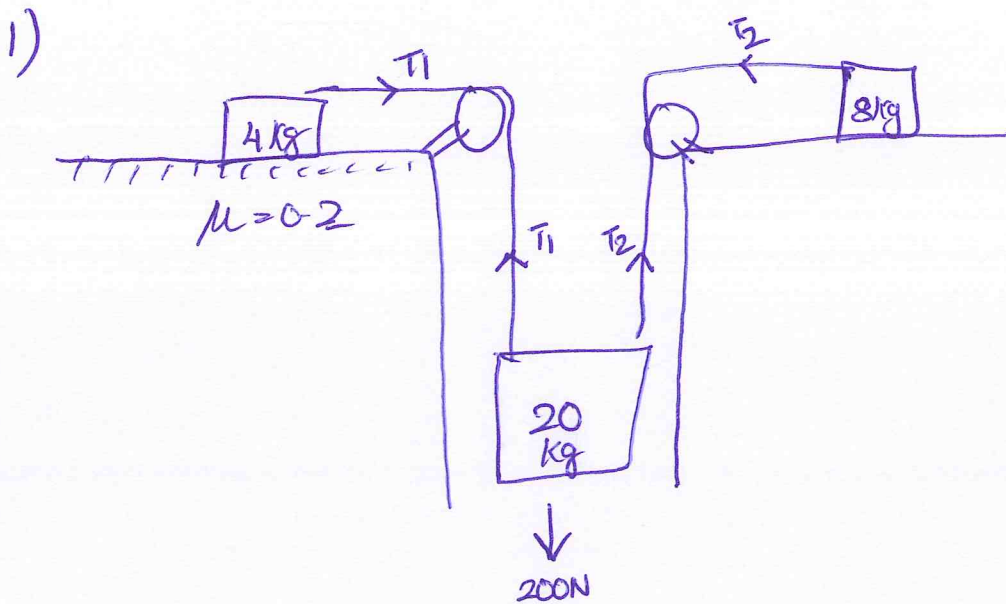
Q5



Q6

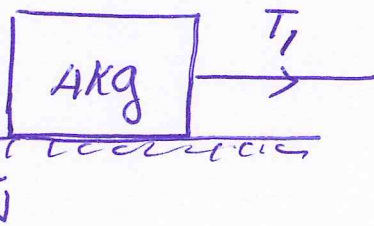


Find acceleration of all blocks.



$$200 - (T_1 + T_2) = 20a$$

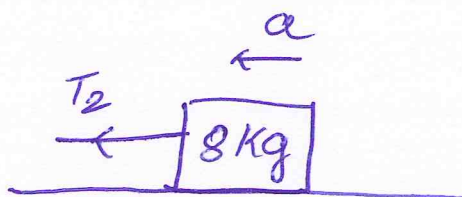
$a$   
→



$$f_{\max} = 40 \times 0.2 = 8 \text{ N}$$

$$T_1 - 8 = 4a$$

$$T_1 = 4a + 8$$



$$T_2 = 8a$$

$$200 - (4a + 8 + 8a) = 20a$$

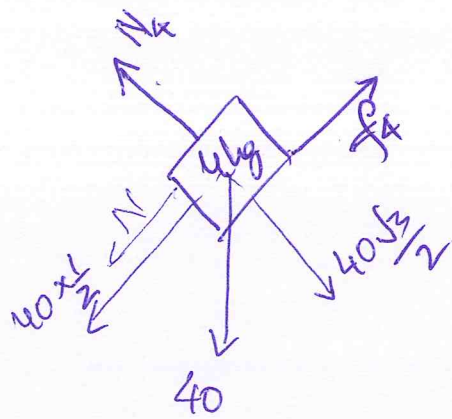
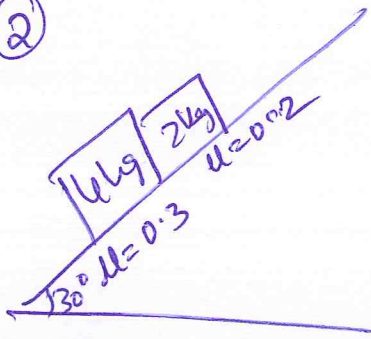
$$192 = 32a$$

$$a = 6 \text{ m/s}^2$$

$$T_2 = 8 \times 6 = 48 \text{ N}$$

$$T_1 = 24 + 8 = 32 \text{ N}$$

②



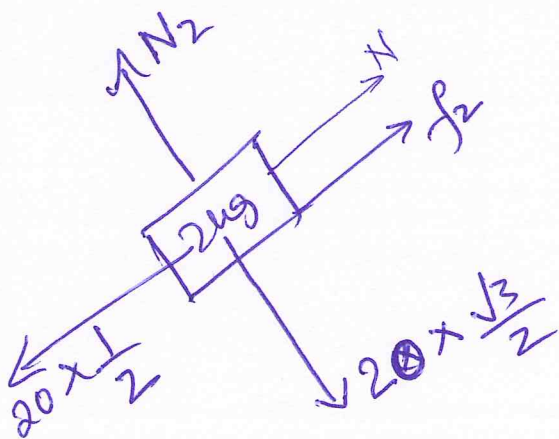
$$N_4 = \frac{40\sqrt{3}}{2}$$

$$f_4 = \mu_4 N_4 = 0.3 \times \frac{40\sqrt{3}}{2}$$

$$40 \times \frac{1}{2} - 0.3 \times \frac{40\sqrt{3}}{2} = 4a_4$$

$$\frac{20}{4} \left(1 - \frac{3\sqrt{3}}{10}\right) = a_4$$

$$a_4 = 5 \left(1 - \frac{3\sqrt{3}}{10}\right) = 5 - 1.5\sqrt{3}$$



$$N_2 = \frac{20\sqrt{3}}{2}$$

$$f_2 = \mu_2 N_2 = 0.2 \times \frac{20\sqrt{3}}{2} = 2\sqrt{3}$$

$$20 \times \frac{1}{2} - 2\sqrt{3} = 2a_2$$

$$a_2 = 5 - \sqrt{3}$$

$$40 \times \frac{1}{2} - 0.3 \times \frac{40\sqrt{3}}{2} + N = 4a.$$

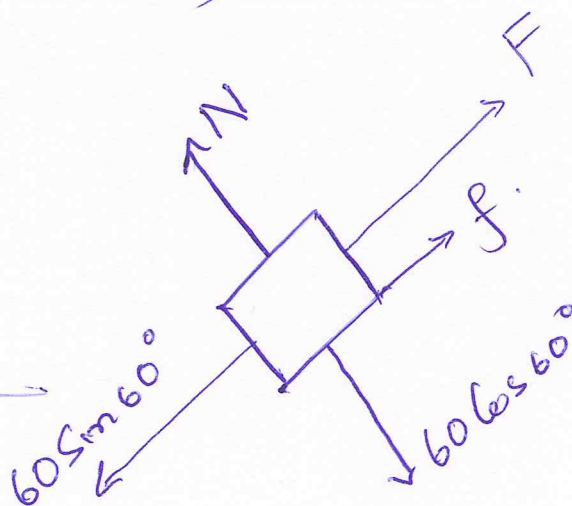
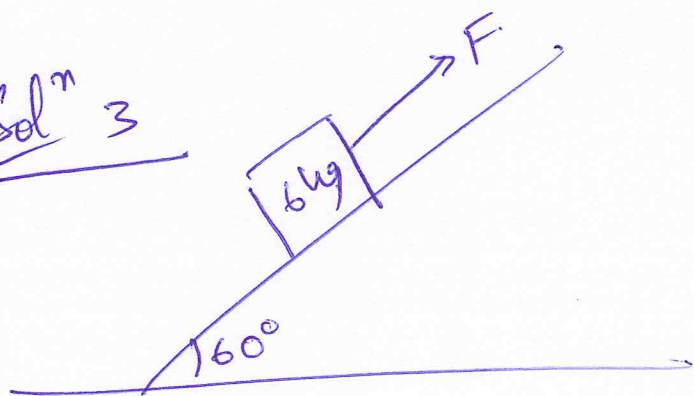
$$+ 20 \times \frac{1}{2} - 2\sqrt{3} - N = 2a.$$

$$60 \times \frac{1}{2} - 8\sqrt{3} = 6a.$$

$$a = \frac{30 - 8\sqrt{3}}{6}$$

$$= \left(5 - \frac{4\sqrt{3}}{3}\right) \text{ m/s}^2$$

Sol<sup>n</sup> 3



$$N = 60 \cos 60^\circ = 30 \text{ N}$$

$$f_{\text{max s}} = 0.6 \times 30 = 18 \text{ N}$$

$$f_{\text{max k}} = 0.4 \times 30 = 12 \text{ N}$$

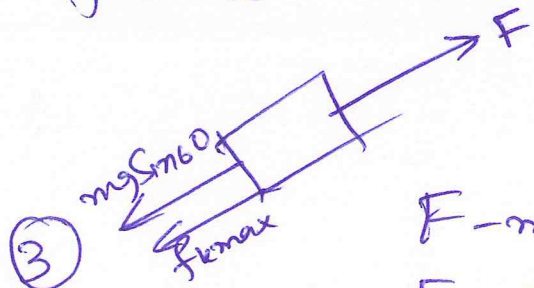
①

$$60 \sin 60^\circ = f_{\text{s max}} + F$$

$$(30\sqrt{3} - 18) = F$$

②  $60 \sin 60^\circ = f_{\text{k max}} + F$

$$(30\sqrt{3} - 12) = F$$

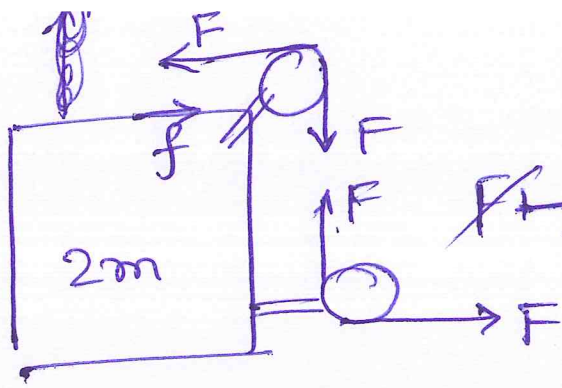


$$F - mg \sin 60 - f_{\text{k max}} = 6 \times 4.$$

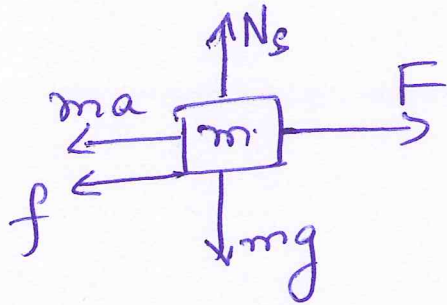
$$F = 24 + 30\sqrt{3} + 12 = (36 + 30\sqrt{3}) \text{ N}$$



Sol<sup>n</sup> 5.



$$\cancel{F} + \cancel{F} + f = 2ma$$



$$\underline{F = f + ma.}$$

$$N_s = mg$$



$$F = 3ma$$

$$a = \frac{F}{3m.}$$

$$f = 2ma.$$

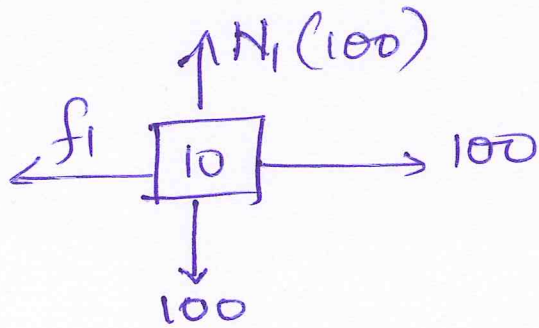
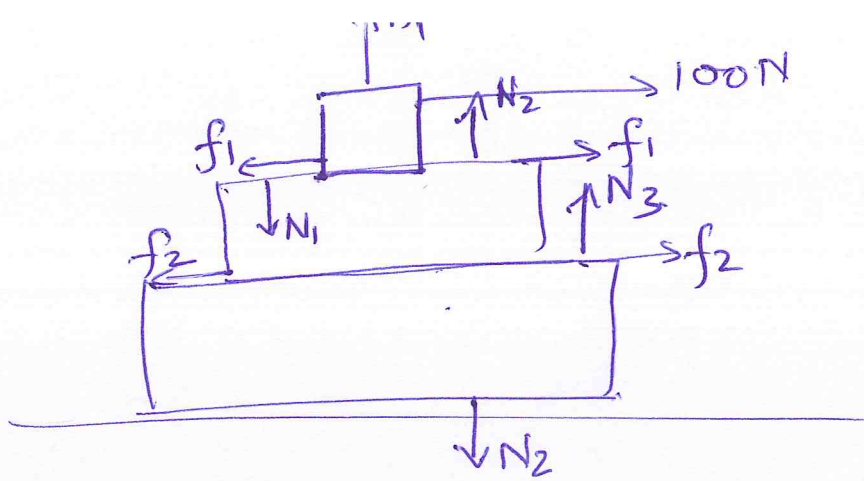
$$f = \cancel{2m} \times \frac{F}{\cancel{3m}} = \frac{2F}{3}.$$

$$f \leq \mu mg.$$

$$\frac{2F}{3} \leq \mu mg$$

$$\frac{2F}{3mg} \leq \mu$$



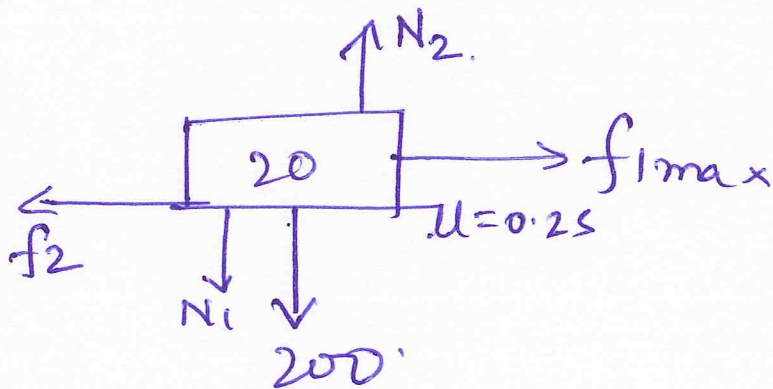


$$N_1 = 100$$

$$f_{1\max} = 0.5 \times N_1 = \underline{\underline{50\text{ N}}}$$

$$100 - 50 = 10 a_1$$

$$a_1 = 5\text{ m/s}^2$$



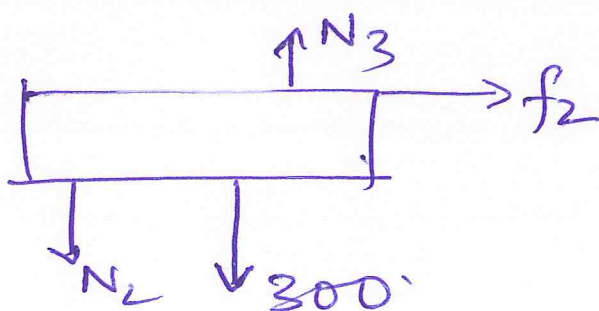
$$N_2 = 200 + N_1 = 300$$

$$f_{2\max} = 0.25 \times N_2 = 75\text{ N}$$

$$f_2 = 50\text{ N}$$

$$a_{\text{rel } 3} = 0$$

$$f_2 = 50\text{ N}$$



$$f_2 = 60 a$$

$$a = \frac{50}{60} \text{ m/s}^2$$

$$a_{\text{rel } 3} = 0$$