

Week 1

1. Python program to Use and demonstrate basic data structures.

Algorithm:

Step 1:[Input Operation & Import time]

```
import time  
start = time.time()  
List=[1,2,"ABC", 3, "xyz", 2.3]  
Dict={"a":1,"b":2,"c":3}  
Tup=(1,2,3,4,5)  
S={1,1,2,2,3,3,4,4,5,5}
```

Step 2:[Output operation]

```
Print list("List")  
Print ("\nDictionary")  
Print ("\n Tuples")  
Print ("\n Sets")  
Print(list)  
Print (Dict)  
Print (Tup)  
Print (s)  
end = time.time()  
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time  
start = time.time()
```

```
print("List")
List = [1, 2,"ABC", 3, "xyz", 2.3]
print(List)
print("\nDictionary")
Dict={"a":1,"b":2,"c":3}
print(Dict)
print("\n Tuples")
Tup=(1,2,3,4,5)
print (Tup)
print("\n Sets")
s={1,1,2,2,3,3,4,4,5,5}
print(s)
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Output:

```
List
[1, 2, 'ABC', 3, 'xyz', 2.3]
```

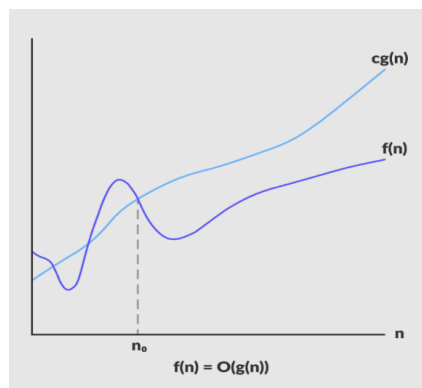
```
Dictionary
{'a': 1, 'b': 2, 'c': 3}
```

```
Tuples
(1, 2, 3, 4, 5)
```

```
Sets
{1, 2, 3, 4, 5}
Runtime of the program is 0.1248924732208252
```

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



- List. Insert: $O(n)$ Get Item: $O(1)$...
- Dictionary. Get Item: $O(1)$ Set Item: $O(1)$...
- Set. Check for item in set: $O(1)$ Difference of set A from B: $O(\text{length of A})$...
- Tuples. Tuples support all operations that do not mutate the data structure (and they have the same complexity classes).

2. Implement an ADT with all its operations

Algorithm

Step 1: [Create class of stack & import time]

```
import time
```

```
start = time.time()
```

```
class Stack:
```

Step 2: [Define functions of basic operations under class stack]

```
def __init__(self):
    self.items = []
def isEmpty(self):
    return self.items == []
def push(self, item):
    self.items.append(item)
    print(item)
def pop(self):
    return self.items.pop()
def peek(self):
    return self.items[len(self.items) - 1]
def size(self):
    return len(self.items)

s=Stack()
print(s.isEmpty()," - because stack is empty")
print("elements are pushed into stack for Operation")
s.push(11)
s.push(12)
s.push(13)
```

Step 3: [Output Operation]

```
print("Size",s.size())
print("Peek",s.peek())
print("Pop Operation")
print(s.pop())
print(s.pop())
```

```
print("Size",s.size())
```

```
print(40* '*')
```

Step 4: [Create class of Queue]

```
class Queue:
```

Step 5: [Define functions of basic operations class queue]

```
def __init__(self):
```

```
    self.items = []
```

```
def isEmpty(self):
```

```
    return self.items == []
```

```
def enqueue(self,item):
```

```
    self.items.append(item)
```

```
    print(item)
```

```
def dequeue(self):
```

```
    return self.items.pop(0)
```

```
def front(self):
```

```
    return self.items[len(self.items)-1]
```

```
def size(self):
```

```
    return len(self.items)
```

Step 6: [Output Operation]

```
print(q.isEmpty(),"- because queue is empty")
```

```
print("Enqueue")
```

```
q.enqueue(11)
```

```
q.enqueue(12)
```

```
q.enqueue(13)
```

```
print("Front",q.front())
```

```
print("Deque")
print(q.dequeue())
print(q.dequeue())
print("Size",q.size())
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
start = time.time()
class Stack:
    def __init__(self):
        self.items = []
    def isEmpty(self):
        return self.items == []
    def push(self, item):
        self.items.append(item)
        print(item)
    def pop(self):
        return self.items.pop()
    def peek(self):
        return self.items[len(self.items) - 1]
    def size(self):
        return len(self.items)
s=Stack()
```

```
print(s.isEmpty()," - because stack is empty")
print("elements are pushed into stack for Operation")
s.push(11)
s.push(12)
s.push(13)
print("Size",s.size())
print("Peek",s.peek())
print("Pop Operation")
print(s.pop())
print(s.pop())
print("Size",s.size())
print((40* '*'))
class Queue:
    def __init__(self):
        self.items = []
    def isEmpty(self):
        return self.items == []
    def enqueue(self,item):
        self.items.append(item)
        print(item)
    def dequeue(self):
        return self.items.pop(0)
    def front(self):
        return self.items[len(self.items)-1]
    def size(self):
```

```

        return len(self.items)

q=Queue()
print(q.isEmpty(),"- because queue is empty")
print("Enqueue")
q.enqueue(11)
q.enqueue(12)
q.enqueue(13)
print("Front",q.front())
print("Dequeue")
print(q.dequeue())
print(q.dequeue())
print("Size",q.size())
end = time.time()
print(f"Runtime of the program is {end - start}")

```

OUTPUT:

True - because stack is empty
elements are pushed into stack for Operation

11

12

13

Size 3

Peek 13

Pop Operation

13

12

Size 1

True - because queue is empty

Enqueue

11

12

13

Front 13

Deque

11

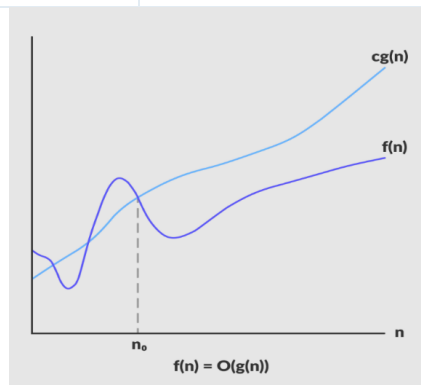
12

Size 1

Runtime of the program is 0.42179059982299805

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time Complexity · Best Case Scenario is $O(1)$ as only one elements needs to be pushed onto the stack. · Average Case Scenario would be $O(1)$.

Week 2

1. Implement an ADT and Compute space and time complexities.

Algorithm

Step 1:[input operation & import time]

Import time

Start = time.time()

Class stack:

```
def __init__(self):
    self.items = []
def isEmpty(self):
    return self.items == []
def push(self, item):
    self.items.append(item)
    print(item)
def pop(self):
    return self.items.pop()
def peek(self):
    return self.items[len(self.items) - 1]
def size(self):
    return len(self.items)
```

step 2:[output operation]

```
s=Stack()
print(s.isEmpty())
print("Push")
s.push(11)
s.push(12)
s.push(13)
print("Peek",s.peak())
```

```
print("Pop")
print(s.pop())
print(s.pop())
print("Size",s.size())
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Python code

```
import time
start = time.time()
class Stack:
    def __init__(self):
        self.items = []
    def isEmpty(self):
        return self.items == []
    def push(self, item):
        self.items.append(item)
        print(item)
    def pop(self):
        return self.items.pop()
    def peek(self):
        return self.items[len(self.items) - 1]
    def size(self):
        return len(self.items)
s=Stack()
```

```
print(s.isEmpty())
print("Push")
s.push(11)
s.push(12)
s.push(13)
print("Peek",s.peek())
print("Pop")
print(s.pop())
print(s.pop())
print("Size",s.size())
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Output:

True

Push

11

12

13

Peek 13

Pop

13

12

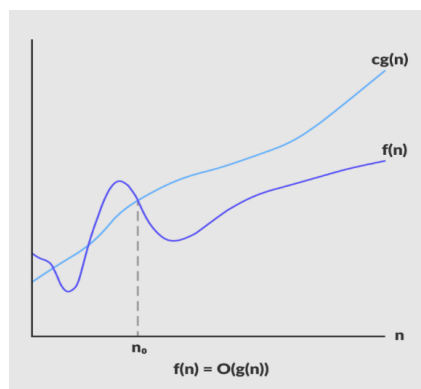
Size 1

Runtime of the program is 0.015621423721313477

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

Time Complexity



- Worst Case Scenario is $O(1)$, as Deletion operation only removes the top element.
- Best Case Scenario is $O(1)$.
- Average Case Scenario would be $O(1)$ as only the top element is needed to be removed.

Space Complexity

- Space Complexity of Pop Operation is $O(1)$ as no additional space is required for it.

2. Implement above solution using array and Compute space and time complexities and compare two solutions.

Algorithm

Step 1:[input operation & import time]

Import time

Start = time.time()

Step 2:[add values for the variable a]

A = [1,2,3,4]

Step 3:[output operation]

print(a)

a.insert(4,5)

print(a)

a.pop(0)

print(a)

l=len(a)

print(l)

end = time.time()

print(f"Runtime of the program is {end - start}")

Python Code

import time

start = time.time()

a = [1,2,3,4]

print(a)

a.insert(4,5)

print(a)

a.pop(0)

print(a)

l=len(a)

```
print(l)
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Output:

[1, 2, 3, 4]

[1, 2, 3, 4, 5]

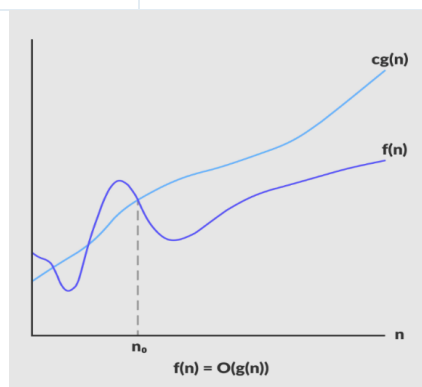
[2, 3, 4, 5]

4

Runtime of the program is 0.015436410903930664

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Space complexity (for n push)

Time complexity of push()

Time complexity of pop()

Time complexity of length()

Time complexity of is_empty()

Week 3

1. Implement Linear Search compute space and time complexities, plot graph using asymptomatic notations.

Linear search algorithm

Step 1: [Import time]

```
import time
```

```
start=time.time()
```

Step 2: [Define a function for linear search]

```
def linearsearch(a, key):
```

```
    n = len(a)
```

```
    for i in range(n):
```

```
        if a[i] == key:
```

```
            return i;
```

```
    return -1
```

Step 3: [Define an array]

```
a = [13,24,35,46,57,68,79]
```

```
print("the array elements are:",a)
```

Step 4: [Enter the element to be searched]

```
k = int(input("enter the key element to search:"))
```

Step 5: [Output operation]

```
i = linearsearch(a,k)
```



```
if i == -1:
    print("Search UnSuccessful")
else:
    print("Search Successful key found at location:",i+1)
end=time.time()
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
start=time.time()
def linearsearch(a, key):
    n = len(a)
    for i in range(n):
        if a[i] == key:
            return i;
    return -1
a = [13,24,35,46,57,68,79]
print("the array elements are:",a)
k = int(input("enter the key element to search => "))
i = linearsearch(a,k)
if i == -1:
    print("Search UnSuccessful")
else:
    print("Search Successful key found at location:",i+1)
end=time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Output:

The array elements are : [13, 24, 35, 46, 57, 68, 79]

enter the key element to search => 46

Search Successful key found at location : 4

Runtime of the program is 2.468712568283081

The array elements are : [13, 24, 35, 46, 57, 68, 79]

enter the key element to search => 20

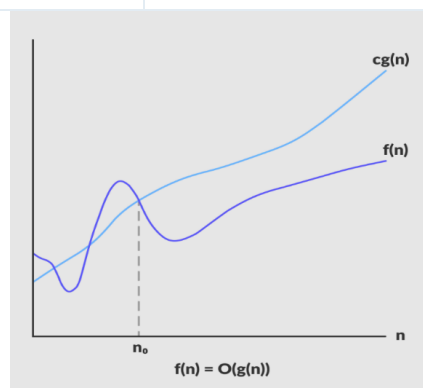
Search UnSuccessful

Runtime of the program is 2.468712568283081

The complexity of Linear Search Technique

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time Complexity: $O(n)$

Space Complexity: $O(1)$

2. Implement Bubble, Selection, insertion sorting algorithms compute space and time complexities, plot graph using asymptomatic notations.

Bubble sort Algorithm

Step 1: [Import time and define a function for Bubble sort]

```
import time
start=time.time()
def bubblesort(a):
    n = len(a)
    for i in range(n-2):
        for j in range(n-2-i):
            if a[j]>a[j+1]:
                temp = a[j]
                a[j] = a[j+1]
                a[j+1] = temp
```

Step 2: [Create array and do the operation]

```
alist = [34,46,43,27,57,41,45,21,70]
```

Step 3: [Output operation]

```
print("Before sorting:",alist)
bubblesort(alist)
end=time.time()
print(f"Runtime of the program is {end - start}")
```

Python Code

```

import time
start=time.time()
def bubblesort(a):
    n = len(a)
    for i in range(n-2):
        for j in range(n-2-i):
            if a[j]>a[j+1]:
                temp = a[j]
                a[j] = a[j+1]
                a[j+1] = temp
alist = [34,46,43,27,57,41,45,21,70]
print("Before sorting:",alist)
bubblesort(alist)
print("After sorting:",alist)
end=time.time()
print(f"Runtime of the program is {end - start}")

```

Output:

Before sorting: [34, 46, 43, 27, 57, 41, 45, 21, 70]

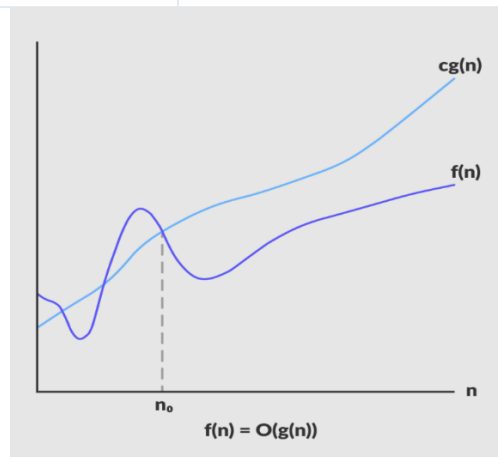
After sorting: [21, 27, 34, 41, 43, 45, 46, 57, 70]

Runtime of the program is 0.06250619888305664

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



The bubble sort algorithm is a reliable sorting algorithm. This algorithm has a worst-case time complexity of $O(n^2)$. The bubble sort has a space complexity of $O(1)$.

Selection Sort Algorithm

Step 1: [Import time & create function of selection sort]

```
import time
start=time.time()
def selectionsort(a):
    n = len(a)
    for i in range(n-2):
        min = i
        for j in range(i+1,n-1):
            if a[j]<a[min]:
                temp = a[j]
```

```
a[j] = a[min]
```

```
a[min] = temp
```

Step 2: [Define array & execute the operation]

```
alist = [34,46,43,27,57,41,45,21,70]
```

```
print("Before sorting:",alist)
```

```
selectionsort(alist)
```

```
print("After sorting:",alist)
```

```
end=time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
```

```
start=time.time()
```

```
def selectionsort(a):
```

```
    n = len(a)
```

```
    for i in range(n-2):
```

```
        min = i
```

```
        for j in range(i+1,n-1):
```

```
            if a[j]<a[min]:
```

```
                temp = a[j]
```

```
                a[j] = a[min]
```

```
                a[min] = temp
```

```
alist = [34,46,43,27,57,41,45,21,70]
```

```
print("Before sorting:",alist)
```

```
selectionsort(alist)
```

```
print("After sorting:",alist)
```

```
end=time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Output:

Before sorting: [34, 46, 43, 27, 57, 41, 45, 21, 70]

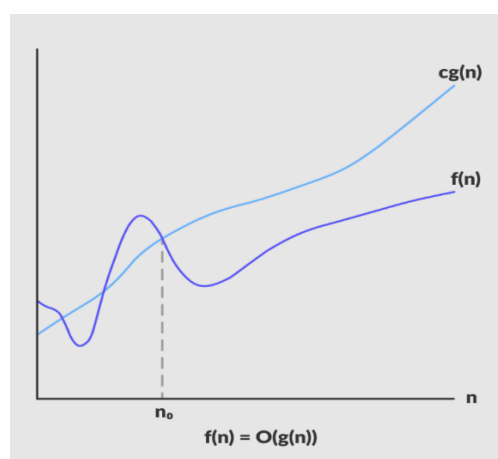
After sorting: [21, 27, 34, 41, 43, 45, 46, 57, 70]

Runtime of the program is 0.06238508224487305

Time Complexities:

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



The time complexity of the bubble sort is $O(n^2)$

Worst Case Complexity: $O(n^2)$: If we want to sort in ascending order and the array is in descending order then the worst case occurs.

Best Case Complexity: $O(n^2)$: If the array is already sorted, then there is no need for sorting.

Average Case Complexity: $O(n^2)$: It occurs when the elements of the array are in random order.

Space Complexity: Space complexity is $O(1)$ because an extra variable (temp) is used for swapping.

Insertion sort Algorithm

Step 1: [Define insertion sort long with importing time]

```
import time
start=time.time()
def insertionsort(a):
    n = len(a)
    for i in range(1,n-1):
        k = a[i]
        j = i-1
        while j>=0 and a[j]>k:
            a[j+1] = a[j]
            j=j-1
        a[j+1] = k
```

Step 2: [Create an array]

```
alist = [34,46,43,27,57,41,45,21,70]
print("Before sorting:",alist)
```

Step 3: [Output operation]

```
insertionsort(alist)
print("After sorting:",alist)
```



```
end=time.time()

print(f"Runtime of the program is {end - start}")
```

Python code

```
import time

start=time.time()

def insertionsort(a):

    n = len(a)

    for i in range(1,n-1):

        k = a[i]

        j = i-1

        while j>=0 and a[j]>k:

            a[j+1] = a[j]

            j=j-1

        a[j+1] = k

alist = [34,46,43,27,57,41,45,21,70]

print("Before sorting:",alist)

insertionsort(alist)

print("After sorting:",alist)

end=time.time()

print(f"Runtime of the program is {end - start}")
```

Output:

Before sorting: [34, 46, 43, 27, 57, 41, 45, 21, 70]

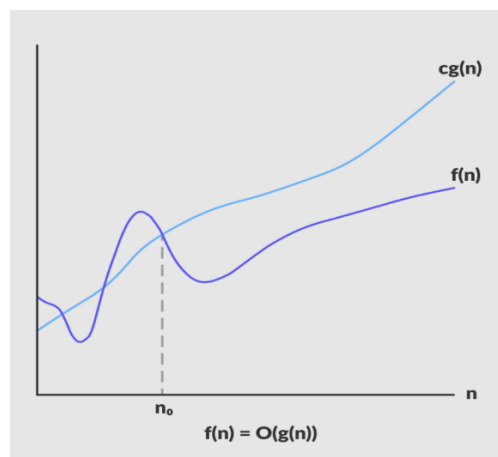
After sorting: [21, 27, 34, 41, 43, 45, 46, 57, 70]

Runtime of the program is 0.07800817489624023

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

Time Complexities:



The time complexity of the bubble sort is $O(n^2)$

- Worst Case Complexity: $O(n^2)$: If we want to sort in ascending order and the array is in descending order then the worst case occurs.
- Best Case Complexity: $O(n)$: If the array is already sorted, then there is no need for sorting.
- Average Case Complexity: $O(n^2)$: It occurs when the elements of the array are in random order.
- Space Complexity: Space complexity is $O(1)$ because an extra variable (temp) is used for swapping.

Week 4

1. Implement Binary Search using recursion Compute space and time complexities, plot graph using asymptomatic notations and compare two.

Algorithm:

Step 1: [Import Input Operation]

```
import time  
  
start=time.time()  
  
Input arr, low, high, x
```

Step 2: [Define Fuctions]

```
def binary_search(arr, low, high, x):  
    if high >= low:  
        mid = (high + low) // 2  
        if arr[mid] == x:  
            return mid  
        elif arr[mid] > x:  
            return binary_search(arr, low, mid - 1, x)  
        else:  
            return binary_search(arr, mid + 1, high, x)  
    else:  
        return -1
```

Step 3: [Output operation]

```
result = binary_search(arr, 0, len(arr)-1, x)  
if result != -1:  
    print("Element is present at index", str(result))  
else:  
    print("Element is not present in array")
```

```
end=time.time()
print(f"Runtime of the program is {end - start}")
```

Python code

```
import time

start=time.time()

def binary_search(arr, low, high, x):

    if high >= low:

        mid = (high + low) // 2

        if arr[mid] == x:

            return mid

        elif arr[mid] > x:

            return binary_search(arr, low, mid - 1, x)

        else:

            return binary_search(arr, mid + 1, high, x)

    else:

        return -1

arr = [ 2, 3, 4, 10, 40 ]

x = 10

result = binary_search(arr, 0, len(arr)-1, x)
```

```
if result != -1:
```

```
    print("Element is present at index", str(result))
```

```
else:
```

```
    print("Element is not present in array")
```

```
end=time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

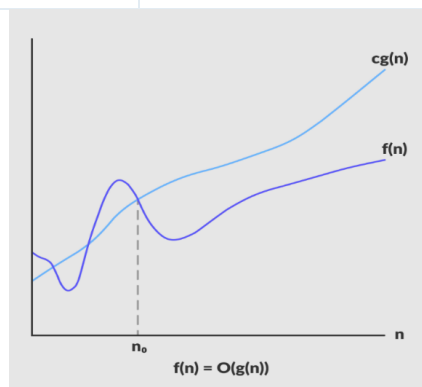
Output:

Element is present at index 3

Runtime of the program is 0.031137466430664062

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



The time complexity of the binary search algorithm is $O(\log n)$. The best-case time complexity would be $O(1)$ when the central index would directly match the desired value. The worst-case scenario could be the values at either extremity of the list or values not in the list.

2. Implement Merge and quick sorting algorithms compute space and time complexities, plot graph using asymptomatic notations and compare all solutions

Merge sort

Algorithm

Step 1: [Import time]

```
import time  
start=time.time()
```

Step 2: [Define Merage Sort]

```
def mergeSort(myList):  
    if len(myList) > 1:  
        mid = len(myList) // 2  
        left = myList[:mid]  
        right = myList[mid:]
```

Step 3: [Recursive operation on each half & Two iterators for traversing the two halves]

```
        mergeSort(left)  
        mergeSort(right)  
        i = 0  
        j = 0
```

Step 4: [Iterator for the main list]

```
        k = 0
```

```
while i < len(left) and j < len(right):
```

```
    if left[i] <= right[j]:
```

```
        myList[k] = left[i]
```

```
        i += 1
```

```
    else:
```

```
        myList[k] = right[j]
```

```
        j += 1
```

```
# For all the remaining values
```

```
while i < len(left):
```

```
    myList[k] = left[i]
```

```
    i += 1
```

```
    k += 1
```

```
while j < len(right):
```

```
    myList[k]=right[j]
```

```
    j += 1
```

```
    k += 1
```

Step 5: [Output operation]

```
myList = [54,26,93,17,77,31,44,55,20]
```

```
mergeSort(myList)
```

```
print(myList)
```

```
end=time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
```

```
start=time.time()
```

```

def mergeSort(myList):
    if len(myList) > 1:
        mid = len(myList) // 2
        left = myList[:mid]
        right = myList[mid:]
        mergeSort(left)
        mergeSort(right)
        i = 0
        j = 0
        k = 0
        while i < len(left) and j < len(right):
            if left[i] <= right[j]:
                myList[k] = left[i]
                i += 1
            else:
                myList[k] = right[j]
                j += 1
            k += 1
        while i < len(left):
            myList[k] = left[i]
            i += 1
            k += 1
        while j < len(right):
            myList[k]=right[j]
            j += 1

```



```

        k += 1
myList = [54,26,93,17,77,31,44,55,20]
mergeSort(myList)
print(myList)
end=time.time()
print(f"Runtime of the program is {end - start}")

```

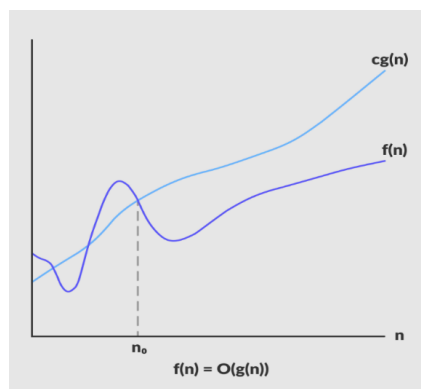
Output:

[17, 20, 26, 31, 44, 54, 55, 77, 93]

Runtime of the program is 0.015508413314819336

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Best Case Time Complexity: $O(n \cdot \log n)$

Worst Case Time Complexity: $O(n \cdot \log n)$

Average Time Complexity: $O(n \cdot \log n)$

Quick Sort

Algorithm

Step 1: [Import time]

```
import time  
start=time.time()
```

Step 2: [Define Quicksort & input an array]

```
def QuickSort(arr):  
    elements = len(arr)  
    #Base case  
    if elements < 2:  
        return arr
```

Step 3: [Position of the partitioning element & loop]

```
    current_position = 0  
    for i in range(1, elements):  
        if arr[i] <= arr[0]:  
            current_position += 1  
            temp = arr[i]  
            arr[i] = arr[current_position]  
            arr[current_position] = temp  
temp = arr[0]  
arr[0] = arr[current_position]
```

```

    arr[current_position] = temp #Brings pivot to it's appropriate
    position

    left = QuickSort(arr[0:current_position]) #Sorts the elements
    to the left of pivot

    right = QuickSort(arr[current_position+1:elements]) #sorts the
    elements to the right of pivot

    arr = left + [arr[current_position]] + right #Merging everything
    together

    return arr

```

Step 4: [Output the program]

```

    array_to_be_sorted = [4,2,7,3,1,6]

    print("Original Array: ",array_to_be_sorted)

    print("Sorted Array: ",QuickSort(array_to_be_sorted))

end=time.time()

print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time

start=time.time()

def QuickSort(arr):

    elements = len(arr)

    if elements < 2:

        return arr

    current_position = 0

    for i in range(1, elements):

        if arr[i] <= arr[0]:

```

```

        current_position += 1
        temp = arr[i]
        arr[i] = arr[current_position]
        arr[current_position] = temp
temp = arr[0]
arr[0] = arr[current_position]
arr[current_position] = temp
left = QuickSort(arr[0:current_position])
right = QuickSort(arr[current_position+1:elements])
arr = left + [arr[current_position]] + right
return arr
array_to_be_sorted = [4,2,7,3,1,6]
print("Original Array: ",array_to_be_sorted)
print("Sorted Array: ",QuickSort(array_to_be_sorted))
end=time.time()
print(f"Runtime of the program is {end - start}")

```

Output:

Original Array: [4, 2, 7, 3, 1, 6]

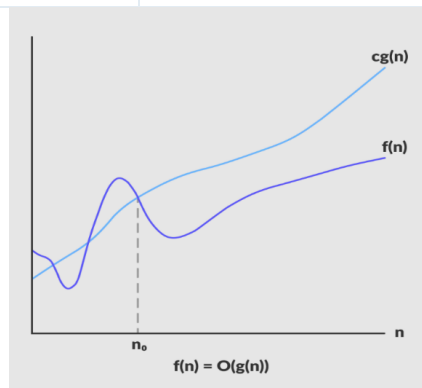
Sorted Array: [1, 2, 3, 4, 6, 7]

Runtime of the program is 0.046759843826293945

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	O(1)	O(1)	O(n)

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Best Case $O(n \cdot \log n)$

Average Case $O(n \cdot \log n)$

Worst Case $O(n^2)$

3. Implement Fibonacci sequence with dynamic programming

Algorithm:

Step 1: [Defining Fibonacci function & import time]

```
import time

start = time.time()

def fibonacci(n):
    # Taking 1st two fibonacci numbers as 0 and 1
    f = [0, 1]
    for i in range(2, n+1):
        f.append(f[i-1] + f[i-2])
    return f[n]
```

Step 2: [Output Operation]

```

print(fibonacci(9))

end = time.time()

print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time

start = time.time()

def fibonacci(n):
    f = [0, 1]
    for i in range(2, n+1):
        f.append(f[i-1] + f[i-2])
    return f[n]

print(fibonacci(9))

end = time.time()

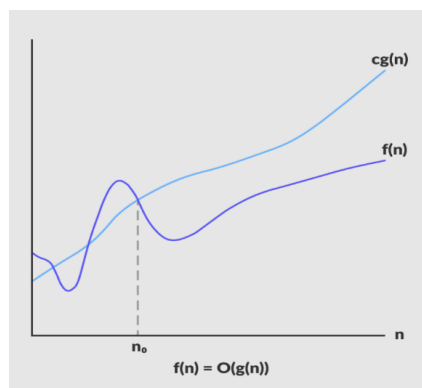
print(f"Runtime of the program is {end - start}")

```

Output:

34

Runtime of the program is 0.01562976837158203



Week 5

1. Implement Singly linked list (Traversing the Nodes, searching for a Node, Prepending Nodes, Removing Nodes)

Singly linked list

Algorithm

Step 1: [Create class node & import time]

```
import time  
  
start = time.time()  
  
class Node:  
    def __init__(self,data):  
        self.data = data  
        self.ref = None
```

Step 2: [Create another class linkedlist]

```
class Linkedlist:  
    def __init__(self):  
        self.head = None
```

Step 3: [define functions to add, print, & delete inside class linked list & Searching given value]

```
def print_LL(self):  
    if self.head is None:  
        print("linked list is empty!")  
    else:  
        n = self.head  
        while n is not None:  
            print(n.data)
```

```

        n = n.ref
def add_begin(self,data):
    new_Node = Node(data)
    new_Node.ref = self.head
    self.head = new_Node
def delete_by_value(self,x):
    if self.head is None:
        print("can't delete LL is empty !")
        return
    if x==self.head.data:
        self.head = self.head.ref
        return
    n = self.head
    while n.ref is not None:
        if x==n.ref.data:
            break
        n==n.ref
    if n.ref is None:
        print("Node is not present !")
    else:
        n.ref=n.ref.ref
def Search_value(self,x):
    if self.head is None:
        print("can't delete LL is empty !")
        return

```



```

    if x==self.head.data:
        self.head = self.head.ref
        print("Node is present at Beginning!")
        return
    n = self.head
    while n.ref is not None:
        if x==n.ref.data:
            print("Node is present!")
            break
        n==n.ref

```

Step 4: [Output operation]

```

L1 = Linkedlist ()
L1.add_begin (10)
L1.add_begin (20)
L1.add_begin (30)
L1.delete_by_value(20)
L1.print_LL()
L1.Search_value (10)
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time

start = time.time()

class Node:

```

```
def __init__(self,data):
    self.data = data
    self.ref = None
class Linkedlist:
    def __init__(self):
        self.head = None
    def print_LL(self):
        if self.head is None:
            print("linked list is empty!")
        else:
            n = self.head
            while n is not None:
                print(n.data)
                n = n.ref
    def add_begin(self,data):
        new_Node = Node(data)
        new_Node.ref = self.head
        self.head = new_Node
    def delete_by_value(self,x):
        if self.head is None:
            print("can't delete LL is empty !")
            return
        if x==self.head.data:
            self.head = self.head.ref
            return
```

```

n = self.head
while n.ref is not None:
    if x==n.ref.data:
        break
    n==n.ref
if n.ref is None:
    print("Node is not present !")
else:
    n.ref=n.ref.ref
def Search_value(self,x):
    if self.head is None:
        print("can't delete LL is empty !")
        return
    if x==self.head.data:
        self.head = self.head.ref
        print("Node is present at Beginning!")
        return
    n = self.head
    while n.ref is not None:
        if x==n.ref.data:
            print("Node is present!")
            break
        n==n.ref
L1 = Linkedlist ()
L1.add_begin (10)

```

```

L1.add_begin (20)
L1.add_begin (30)
L1.delete_by_value(20)
L1.print_LL()
L1.Search_value (10)
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Output:

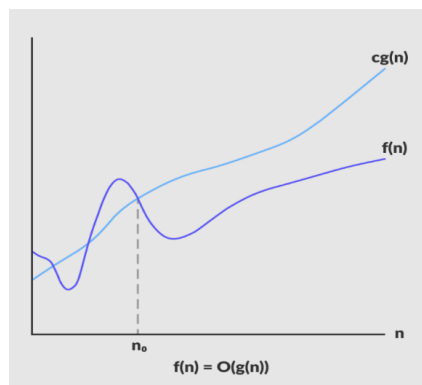
```

30
10
Node is present!
Runtime of the program is 0.046753883361816406

```

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



The summary of Time Complexity of operations in a Linked List is:

SINGLY LINKED LIST OPERATION	REAL TIME COMPLEXITY	ASSUMED TIME COMPLEXITY
Access i-th element	$O(\sqrt{N} * N)$	$O(N)$
Traverse all elements	$O(\sqrt{N} * N)$	$O(N)$
Insert element E at current point	$O(1)$	$O(1)$
Delete current element	$O(1)$	$O(1)$
Insert element E at front	$O(1)$	$O(1)$
Insert element E at end	$O(\sqrt{N} * N)$	$O(N)$

The Space Complexity of the above Linked List operations is $O(1)$.

Week 6

1. Implement linked list Iterators.

Algorithm

Step 1: [Create class Find odd & import time]

```
import time
```

```
start = time.time()
```

```
class FindOdd:
```

Step 2: [Define functions inside class]

```
def __init__(self,end):
```

```
    self.__start = 1
```

```
    self.__end = end
```

```
def __iter__(self):
```

```
    return OddsIterator(self.__end)
```

Step 3: [Define another class Odds Iterator]

```
class OddsIterator:
```

```
def __init__(self,finish):
```

```
    self.__current = 0
```

```
    self.__step = 1
```

```
    self.__end = finish
```

```
def __next__(self):
```

```

x = None
if self.__current > self.__end:
    raise StopIteration
else:
    self.__current += self.__step
    if (self.__current - self.__step + 1) % 2 != 0:
        x = self.__current - self.__step + 1
    if x != None:
        return x

```

Step 4: [Output Operation]

```

odds = FindOdd(2)
print(list(odds))
end = time.time()

print(f"Runtime of the program is {end - start}")

```

Python code

```

import time

start = time.time()

class FindOdd:
    def __init__(self, end):
        self.__start = 1
        self.__end = end
    def __iter__(self):
        return OddsIterator(self.__end)

class OddsIterator:
    def __init__(self, finish):
        self.__current = 0
        self.__step = 1
        self.__end = finish
    def __next__(self):
        x = None
        if self.__current > self.__end:
            raise StopIteration
        else:
            self.__current += self.__step

```

```

        if (self.__current - self.__step + 1) % 2 != 0:
            x = self.__current - self.__step + 1
        if x != None:
            return x
    odds = FindOdd(2)
    print(list(odds))
    end = time.time()

    print(f"Runtime of the program is {end - start}")

```

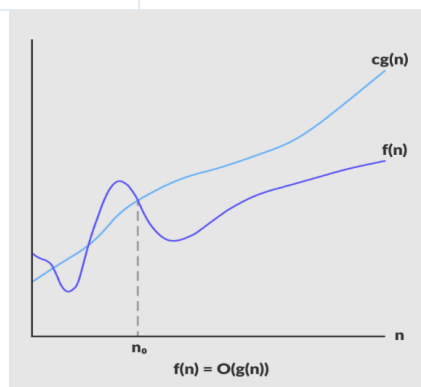
Output:

[1, None, 3]

Runtime of the program is 0.015508651733398438

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time Complexity

As we are only traversing the list to the overall time complexity will be $O(n)$.

Space complexity

Since no extra space is used the space complexity will be $O(1)$.

Week7

1. Implement DLL

Algorithm

Step 1: [Create class & Initialize the node & import time]

```
import time

start = time.time()

class Node:

    def __init__(self, data):

        self.item = data

        self.next = None

        self.prev = None
```

Step 2: [Create another class for doubly linked list]

```
class doublyLinkedList:

    def __init__(self):

        self.start_node = None
```

Step 3: [Add Insert to Empty list function inside the class]

```
def InsertToEmptyList(self, data):

    if self.start_node is None:

        new_node = Node(data)

        self.start_node = new_node

    else:

        print("The list is empty")
```

Step 4: [Add Insert to End function inside the class]

```
def InsertToEnd(self, data):
```



```

if self.start_node is None:
    new_node = Node(data)
    self.start_node = new_node
    return
n = self.start_node
while n.next is not None:
    n = n.next
new_node = Node(data)
n.next = new_node
new_node.prev = n

```

Step 5: [Define function to delete the elements from the end]

```

def DeleteAtStart(self):
    if self.start_node is None:
        print("The Linked list is empty, no element to delete")
        return
    if self.start_node.next is None:
        self.start_node = None
        return
    self.start_node = self.start_node.next
    self.start_prev = None;
def delete_at_end(self):
    if self.start_node is None:
        print("The Linked list is empty, no element to delete")
        return
    if self.start_node.next is None:

```

```
        self.start_node = None
    return
n = self.start_node
while n.next is not None:
    n = n.next
n.prev.next = None
```

Step 6: [Create function to display & traversing]

```
def Display(self):
    if self.start_node is None:
        print("The list is empty")
        return
    else:
        n = self.start_node
        while n is not None:
            print("Element is: ", n.item)
            n = n.next
        print("\n")
```

Step 7: [Function for searching element in list]

```
def search(self,x):
    if self.start_node is None:
        print("The list is empty")
        return
    else:
        n = self.start_node
        while n is not None:
```

```
if x==n.item:  
    print("item present")  
    break  
    n = n.next  
    print("\n")
```

Step 8: [Create elements to display output]

```
NewDoublyLinkedList = doublyLinkedList()  
NewDoublyLinkedList.InsertToEmptyList(10)  
NewDoublyLinkedList.InsertToEnd(20)  
NewDoublyLinkedList.InsertToEnd(30)  
NewDoublyLinkedList.InsertToEnd(40)  
NewDoublyLinkedList.InsertToEnd(50)  
NewDoublyLinkedList.InsertToEnd(60)
```

Step 9: [Output Operation]

```
NewDoublyLinkedList.Display()  
NewDoublyLinkedList.DeleteAtStart()  
NewDoublyLinkedList.DeleteAtStart()  
NewDoublyLinkedList.Display()  
NewDoublyLinkedList.search(30)  
end = time.time()  
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time  
start = time.time()
```

```
class Node:
    def __init__(self, data):
        self.item = data
        self.next = None
        self.prev = None
class doublyLinkedList:
    def __init__(self):
        self.start_node = None
    def InsertToEmptyList(self, data):
        if self.start_node is None:
            new_node = Node(data)
            self.start_node = new_node
        else:
            print("The list is empty")
    def InsertToEnd(self, data):
        if self.start_node is None:
            new_node = Node(data)
            self.start_node = new_node
            return
        n = self.start_node
        while n.next is not None:
            n = n.next
        new_node = Node(data)
        n.next = new_node
        new_node.prev = n
```

```

def DeleteAtStart(self):
    if self.start_node is None:
        print("The Linked list is empty, no element to delete")
        return
    if self.start_node.next is None:
        self.start_node = None
        return
    self.start_node = self.start_node.next
    self.start_prev = None;
def delete_at_end(self):
    if self.start_node is None:
        print("The Linked list is empty, no element to delete")
        return
    if self.start_node.next is None:
        self.start_node = None
        return
    n = self.start_node
    while n.next is not None:
        n = n.next
    n.prev.next = None
def Display(self):
    if self.start_node is None:
        print("The list is empty")
        return
    else:

```

```

        n = self.start_node
        while n is not None:
            print("Element is: ", n.item)
            n = n.next
        print("\n")
    def search(self,x):
        if self.start_node is None:
            print("The list is empty")
            return
        else:
            n = self.start_node
            while n is not None:
                if x==n.item:
                    print("item present")
                    break
                n = n.next
            print("\n")

```

```

NewDoublyLinkedList = doublyLinkedList()
NewDoublyLinkedList.InsertToEmptyList(10)
NewDoublyLinkedList.InsertToEnd(20)
NewDoublyLinkedList.InsertToEnd(30)
NewDoublyLinkedList.InsertToEnd(40)
NewDoublyLinkedList.InsertToEnd(50)
NewDoublyLinkedList.InsertToEnd(60)
NewDoublyLinkedList.Display()

```

```
NewDoublyLinkedList.DeleteAtStart()  
NewDoublyLinkedList.DeleteAtStart()  
NewDoublyLinkedList.Display()  
NewDoublyLinkedList.search(30)  
end = time.time()  
print(f"Runtime of the program is {end - start}")
```

Output:

```
Element is: 10  
Element is: 20  
Element is: 30  
Element is: 40  
Element is: 50  
Element is: 60
```

```
Element is: 30  
Element is: 40  
Element is: 50  
Element is: 60
```

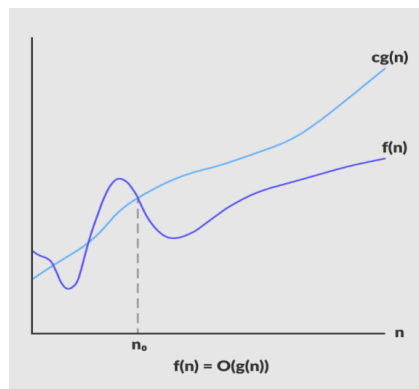
item present

Runtime of the program is 0.3124046325683594

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

Time and Space Complexity



The time complexity for searching a given element in the linked list is **$O(N)$** as we have to loop over all the nodes and check for the required one. The space complexity is **$O(1)$** as no additional memory is required to traverse through a doubly linked list and perform a search.

2. Implement CDLL

Step 1: [Create class node]

```
import time

start = time.time()

class Node:

    def __init__(self, my_data):

        self.data = my_data
```



```
self.next = None
```

Step 2: [Create another class circular linked list]

```
class circularLinkedList:
    def __init__(self):
        self.head = None
    def add_data(self, my_data):
        ptr_1 = Node(my_data)
        temp = self.head
        ptr_1.next = self.head
        if self.head is not None:
            while(temp.next != self.head):
                temp = temp.next
            temp.next = ptr_1
        else:
            ptr_1.next = ptr_1
        self.head = ptr_1
```

Step 3: [Define output function]

```
def print_it(self):
    temp = self.head
    if self.head is not None:
        while(True):
            print("%d" %(temp.data)),
            temp = temp.next
            if (temp == self.head):
                break
```

Step 4: [Output operation]

```
my_list = circularLinkedList()
print("Elements are added to the list ")
my_list.add_data (56)
my_list.add_data (78)
my_list.add_data (12)
print("The data is : ")
my_list.print_it()
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Python code

```
import time
start = time.time()
class Node:
    def __init__(self, my_data):
        self.data = my_data
        self.next = None
class circularLinkedList:
    def __init__(self):
        self.head = None
    def add_data(self, my_data):
        ptr_1 = Node(my_data)
        temp = self.head
        ptr_1.next = self.head
```

```

    if self.head is not None:
        while(temp.next != self.head):
            temp = temp.next
        temp.next = ptr_1
    else:
        ptr_1.next = ptr_1
    self.head = ptr_1
def print_it(self):
    temp = self.head
    if self.head is not None:
        while(True):
            print("%d" %(temp.data)),
            temp = temp.next
            if (temp == self.head):
                break
my_list = circularLinkedList()
print("Elements are added to the list ")
my_list.add_data (56)
my_list.add_data (78)
my_list.add_data (12)
print("The data is : ")
my_list.print_it()
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Output:

Elements are added to the list

The data is :

12

78

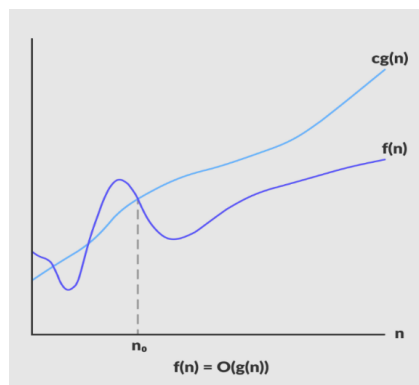
56

Runtime of the program is 0.06238698959350586

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

Time and Space Complexity



The time complexity for searching a given element in the linked list is **$O(N)$** as we have to loop over all the nodes and check for the required one. The space complexity is **$O(1)$** as no additional memory is required to traverse through a circular singly linked list and perform a search.

Week 8

1. Implement Stack Data

Step 1: [Create stack of list & import time]

```
import time  
  
start = time.time()  
  
stack = []
```

Step 2: [Function to push element in the stack]

```
stack.append('a')  
stack.append('b')  
stack.append('c')  
print('Initial stack')  
  
print(stack)
```

Step 3: [Function to pop element from stack]

```
print(stack.pop())  
print(stack.pop())  
print(stack.pop())
```

Step 4: [Output operation]

```
print('\nElements popped from stack:')  
print('\nStack after elements are popped:')  
print(stack)  
  
end = time.time()  
  
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
start = time.time()
stack = []
stack.append('a')
stack.append('b')
stack.append('c')
print('Initial stack')
print(stack)
print('\nElements popped from stack:')
print(stack.pop())
print(stack.pop())
print(stack.pop())
print('\nStack after elements are popped:')
print(stack)
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Output:

Initial stack

['a', 'b', 'c']

Elements popped from stack:

c

b

a

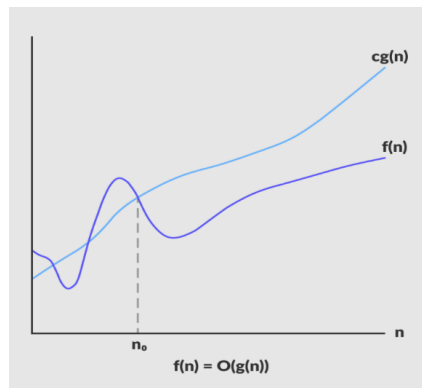
Stack after elements are popped:

[]

Runtime of the program is 0.10926008224487305

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



The time complexity of creating a Stack using a list is $O(1)$ as it takes a constant amount of time to initialize a list. The space complexity is $O(1)$ as well since no additional memory is required.

2. Implement Bracket matching using stack

Step 1: [Define function to balance Brackets & import time]

```
import time
```

```
start = time.time()
```

```
def areBracketsBalanced(expr):
```

```
    stack = []
```

Step 2: [Push the element & Traverse the expression in function]

```
    for char in expr:
```

```
        if char in ["(", "{", "["]:
```

```
            stack.append(char)
```

```
        else:
```

```
            if not stack:
```

```
                return False
```

```
            current_char = stack.pop()
```

```
            if current_char == '(':
```

```
                if char != ")":
```

```
                    return False
```

```
            if current_char == '{':
```

```
                if char != "}":
```

```
                    return False
```

```
            if current_char == '[':
```

```
                if char != "]":
```

```
                    return False
```

Step 3: [Condition to check the stack]

```
    if stack:
```

```
        return False
```

```
    return True
```

Step 4: [Source code to set the special variable]


```
if __name__ == "__main__":
    expr = "{()}{[]}"
    if areBracketsBalanced(expr):
        print("Balanced")
    else:
        print("Not Balanced")
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
start = time.time()
def areBracketsBalanced(expr):
    stack = []
    for char in expr:
        if char in ["(", "{", "["]:
            stack.append(char)
        else:
            if not stack:
                return False
            current_char = stack.pop()
            if current_char == '(':
                if char != ")":
                    return False
            if current_char == '{':
                if char != "}":
                    return False
            if current_char == '[':
```

```

        if char != "}":
            return False
    if current_char == '[':
        if char != "]":
            return False

    if stack:
        return False

    return True

if __name__ == "__main__":
    expr = "{()}{[]}"
    if areBracketsBalanced(expr):
        print("Balanced")
    else:
        print("Not Balanced")

end = time.time()

print(f"Runtime of the program is {end - start}")

```

Output:

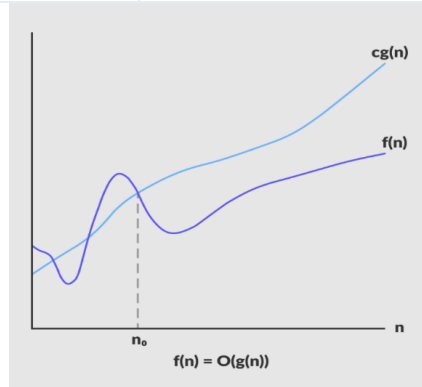
Balanced

Runtime of the program is 0.031132936477661133

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	O(1)	O(1)	O(n)
Insertion	O(1)	O(1)	O(n)

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



$O(1)$ space | $O(N^2)$ time complexity

Week 9

1. Program to demonstrate recursive operations (Factorial / Fibonacci)

Step 1: [Create function for recursive operations & import time]

```
import time

start = time.time()

def recur_fibo(n):
    if n <= 1:
        return n
    else:
        return(recur_fibo(n-1) + recur_fibo(n-2))

nterms = 10
```

Step 2: [Program to check if the number of terms is valid & output operation]

```

if nterms <= 0:
    print("Plese enter a positive integer")
else:
    print("Fibonacci sequence:")
    for i in range(nterms):
        print(recur_fibo(i))
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time
start = time.time()
def recur_fibo(n):
    if n <= 1:
        return n
    else:
        return(recur_fibo(n-1) + recur_fibo(n-2))
nterms = 10
if nterms <= 0:
    print("Plese enter a positive integer")
else:
    print("Fibonacci sequence:")
    for i in range(nterms):
        print(recur_fibo(i))
end = time.time()

```

```
print(f"Runtime of the program is {end - start}")
```

Output:

Fibonacci Sequence:

0

1

1

2

3

5

8

13

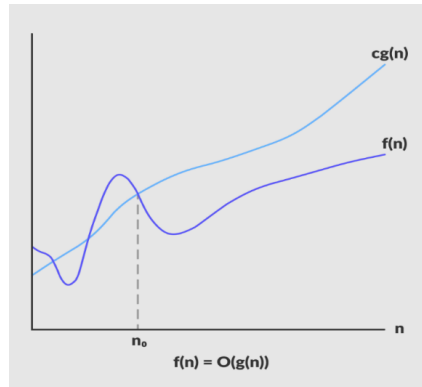
21

34

Runtime of the program is 0.10938119888305664

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Space complexity is $O(1)$ & time complexity $O(n)$

2. Implement Solution for Towers of Hanoi

Step 1: [Define function Towers of Hanoi & import time]

```
import time

start = time.time()

def TowerOfHanoi(n , source, destination, auxiliary):

    if n==1:

        print ("Move disk 1 from source",source,"to
destination",destination)

        return
```

Step 2: [Execution program]

```
TowerOfHanoi(n-1, source, auxiliary, destination)

    print ("Move disk",n,"from source",source,"to
destination",destination)

    TowerOfHanoi(n-1, auxiliary, destination, source)

end = time.time()

print(f"Runtime of the program is {end - start}")
```

Python Code

```

import time
start = time.time()
def TowerOfHanoi(n , source, destination, auxiliary):
    if n==1:
        print ("Move disk 1 from source",source,"to
destination",destination)
        return
    TowerOfHanoi(n-1, source, auxiliary, destination)
    print ("Move disk",n,"from source",source,"to
destination",destination)
    TowerOfHanoi(n-1, auxiliary, destination, source)
n = 3
TowerOfHanoi(n,'A','B','C')
end = time.time()
print(f"Runtime of the program is {end - start}")

```

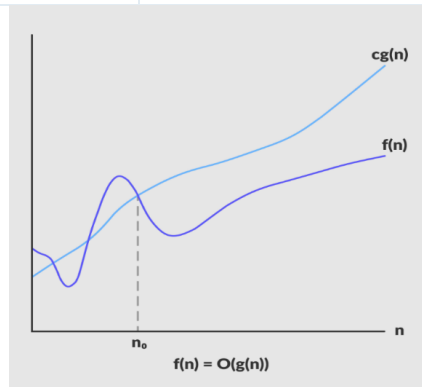
Output:

```

Move disk 1 from source A to destination B
Move disk 2 from source A to destination C
Move disk 1 from source B to destination C
Move disk 3 from source A to destination B
Move disk 1 from source C to destination A
Move disk 2 from source C to destination B
Move disk 1 from source A to destination B
Runtime of the program is 0.29689645767211914
Time Complexity For open addressing:

```

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Space complexity is $O(n)$. Here time complexity is exponential but space complexity is linear

Week 10

1. Implement Queue

Algorithm

Step 1: [Create class of Queue & import time]

```
import time
start = time.time()
class Queue:
```

Step 2: [Define functions of basic operations class queue]

```
def __init__(self):
    self.items = []
def isEmpty(self):
    return self.items == []
```



```
def enqueue(self,item):
    self.items.append(item)
    print(item)
def dequeue(self):
    return self.items.pop(0)
def front(self):
    return self.items[len(self.items)-1]
def size(self):
    return len(self.items)
```

Step 3: [Output Operation]

```
print(q.isEmpty(),"- because queue is empty")
print("Enqueue")
q.enqueue(15)
q.enqueue(16)
q.enqueue(17)
print("Front",q.front())
print("Dequeue")
print(q.dequeue())
print(q.dequeue())
print("Size",q.size())
end = time.time()
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
```

```

start = time.time()

class Queue:
    def __init__(self):
        self.items = []
    def isEmpty(self):
        return self.items == []
    def enqueue(self,item):
        self.items.append(item)
        print(item)
    def dequeue(self):
        return self.items.pop(0)
    def front(self):
        return self.items[len(self.items)-1]
    def size(self):
        return len(self.items)

q=Queue()
print(q.isEmpty(),"- because queue is empty")
print("Enqueue")
q.enqueue(15)
q.enqueue(16)
q.enqueue(17)
print("Front",q.front())
print("Dequeue")
print(q.dequeue())
print(q.dequeue())
print("Size",q.size())
end = time.time()

print(f"Runtime of the program is {end - start}")

```

Output:

```

True - because queue is empty
Enqueue
15
16
17
Front 17

```

Dequee

15

16

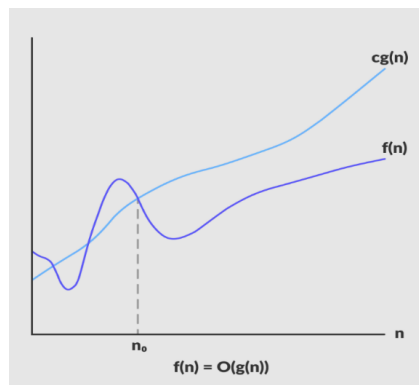
Size 1

Runtime of the program is 0.140514135360717771

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

Time and Space Complexity



The time complexity of creating a Queue using a list is **$O(1)$** as it takes a constant amount of time to initialize a list. The space complexity is **$O(1)$** as well since no additional memory is required.

2. Implement priority queue

Algorithm

Step 1: [Create class Priority queue & import time]

```
import time
```

```
start = time.time()
```

```
class PriorityQueue(object):
```

```
    def __init__(self):
```

```

        self.queue = []
    def __str__(self):
        return ' '.join([str(i) for i in self.queue])
    def isEmpty(self):
        return len(self.queue) == 0
    def insert(self, data):
        self.queue.append(data)
    def delete(self):
        try:
            max_val = 0

```

Step 2: [Checking the Condition]

```

        for i in range(len(self.queue)):
            if self.queue[i] > self.queue[max_val]:
                max_val = i
        item = self.queue[max_val]
        del self.queue[max_val]
        return item
    except IndexError:
        print()
        exit()

```

Step 3: [Inserting in Queue]

```

if __name__ == '__main__':
    myQueue = PriorityQueue()
    myQueue.insert(12)
    myQueue.insert(1)
    myQueue.insert(14)
    myQueue.insert(7)

```

Step 4: [Output Operation]

```

    print(myQueue)
    while not myQueue.isEmpty():
        print(myQueue.delete())
    end = time.time()

    print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time

```

```

start = time.time()

class PriorityQueue(object):
    def __init__(self):
        self.queue = []
    def __str__(self):
        return ' '.join([str(i) for i in self.queue])
    def isEmpty(self):
        return len(self.queue) == 0
    def insert(self, data):
        self.queue.append(data)
    def delete(self):
        try:
            max_val = 0
            for i in range(len(self.queue)):
                if self.queue[i] > self.queue[max_val]:
                    max_val = i
            item = self.queue[max_val]
            del self.queue[max_val]
            return item
        except IndexError:
            print()
            exit()

if __name__ == '__main__':
    myQueue = PriorityQueue()
    myQueue.insert(12)
    myQueue.insert(1)
    myQueue.insert(14)
    myQueue.insert(7)
    print(myQueue)
    while not myQueue.isEmpty():
        print(myQueue.delete())
end = time.time()

print(f"Runtime of the program is {end - start}")

```

Output:

12 1 14 7

14

12

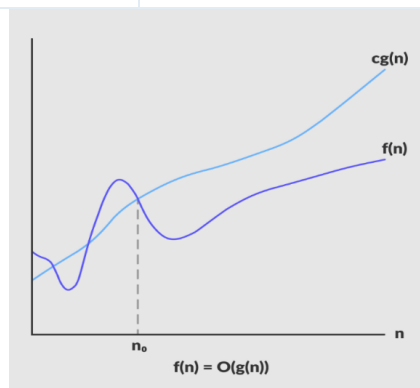
7

1

Runtime of the program is 0.07807803153991699

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time complexity: By Using heap data structure to implement Priority Queue

Insert Operation: $O(\log(n))$

Delete Operation: $O(\log(n))$

Week 11

1. Implement Binary search tree and its operations using list.

Algorithm

Step 1: [Creating a Binary tree by defining class initially & import time]

```
import time

start = time.time()

class Node:

    def __init__(self, key):

        self.key = key

        self.left = None

        self.right = None
```

Step 2: [Inorder traversal function inside node]

```
def inorder(root):

    if root is not None:

        inorder(root.left)

        print(str(root.key) + "->", end=' ')

        inorder(root.right)
```

Step 3: [Inserting a Node]

```
def insert(node, key):

    if node is None:

        return Node(key)

    if key < node.key:

        node.left = insert(node.left, key)

    else:

        node.right = insert(node.right, key)

    return node
```

Step 4: [Find the inorder Successor]

```
def minValueNode(node):  
    current = node  
    while(current.left is not None):  
        current = current.left  
    return current
```

Step 5: [Deleting a node]

```
def deleteNode(root, key):  
    if root is None:  
        return root  
    if key < root.key:  
        root.left = deleteNode(root.left, key)  
    elif(key > root.key):  
        root.right = deleteNode(root.right, key)  
    else:  
        if root.left is None:  
            temp = root.right  
            root = None  
            return temp  
        elif root.right is None:  
            temp = root.left  
            root = None  
            return temp  
        temp = minValueNode(root.right)  
        root.key = temp.key
```

Step 6: [Delete the inorder successor]


```
        root.right = deleteNode(root.right, temp.key)
    return root
```

Step 7: [Search the given node]

```
def searchNode(root, key):
    if root.left is None:
        print("The element has not found.")
        return
    elif root.key == key:
        print("The element has been found.")
    elif key < root.key:
        if root.left.key == key:
            print("The element has been found.")
        else:
            searchNode(root.left, key)
    else:
        if root.right.key == key:
            print(key, " element has been found.")
        else:
            searchNode(root.right, key)
```

Step 8: [Output operation]

```
root = None
root = insert(root, 8)
root = insert(root, 3)
root = insert(root, 1)
root = insert(root, 6)
```

```

root = insert(root, 7)
root = insert(root, 10)
root = insert(root, 14)
root = insert(root, 4)
print("Inorder traversal: ", end=' ')
inorder(root)
print("\nDelete 10")
root = deleteNode(root, 10)
print("Inorder traversal: ", end=' ')
inorder(root)
print("\n")
searchNode(root,14)
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Python Code

```

import time
start = time.time()
class Node:
    def __init__(self, key):
        self.key = key
        self.left = None
        self.right = None
def inorder(root):
    if root is not None:

```

```

    inorder(root.left)
    print(str(root.key) + "->", end=' ')
    inorder(root.right)
def insert(node, key):
    if node is None:
        return Node(key)
    if key < node.key:
        node.left = insert(node.left, key)
    else:
        node.right = insert(node.right, key)
    return node
def minValueNode(node):
    current = node
    while(current.left is not None):
        current = current.left
    return current
def deleteNode(root, key):
    if root is None:
        return root
    if key < root.key:
        root.left = deleteNode(root.left, key)
    elif(key > root.key):
        root.right = deleteNode(root.right, key)
    else:
        if root.left is None:

```

```

    temp = root.right
    root = None
    return temp
elif root.right is None:
    temp = root.left
    root = None
    return temp
temp = minValueNode(root.right)
root.key = temp.key
root.right = deleteNode(root.right, temp.key)
return root
def searchNode(root, key):
    if root.left is None:
        print("The element has not found.")
        return
    elif root.key == key:
        print("The element has been found.")
    elif key < root.key:
        if root.left.key == key:
            print("The element has been found.")
        else:
            searchNode(root.left, key)
    else:
        if root.right.key == key:
            print(key, " element has been found.")

```

```

        else:
            searchNode(root.right,key)
root = None
root = insert(root, 8)
root = insert(root, 3)
root = insert(root, 1)
root = insert(root, 6)
root = insert(root, 7)
root = insert(root, 10)
root = insert(root, 14)
root = insert(root, 4)
print("Inorder traversal: ", end=' ')
inorder(root)
print("\nDelete 10")
root = deleteNode(root, 10)
print("Inorder traversal: ", end=' ')
inorder(root)
print("\n")
searchNode(root,14)
end = time.time()
print(f"Runtime of the program is {end - start}")

```

Output:

Inorder traversal: 1-> 3-> 4-> 6-> 7-> 8-> 10-> 14->

Delete 10

Inorder traversal: 1-> 3-> 4-> 6-> 7-> 8-> 14->

14 element has been found.

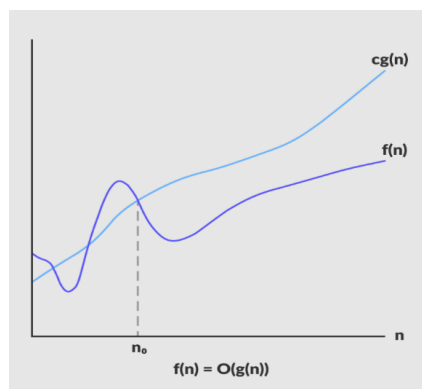
Runtime of the program is 0.29677271842956543

Binary Search Tree Complexities

Time Complexity

Operation	Best Case Complexity	Average Case Complexity	Worst Case Complexity
Search	$O(\log n)$	$O(\log n)$	$O(n)$
Insertion	$O(\log n)$	$O(\log n)$	$O(n)$
Deletion	$O(\log n)$	$O(\log n)$	$O(n)$

Here, n is the number of nodes in the tree.



Space Complexity: The space complexity for all the operations is $O(n)$.

Week 12

1. Implementation of BFS.

Algorithm

Step 1: [Import queue & import time]

import time

```

start = time.time()

from queue import Queue

graph =
{'A':['B','D','E','F'],'D':['A'],'B':['A','F','C'],'F':['B','A'],'C':['B'],'E':['A']}

print("Given Graph is : ")

print(graph)

```

Step 2: [Define BFS function]

```

def BFS(input_graph,source):

    Q = Queue()

    visited_vertices = list()

    Q.put(source)

    visited_vertices.append(source)

```

Step 3: [Checking the condition]

```

while not Q.empty():

    vertex = Q.get()

    print(vertex,end= " ")

    for u in input_graph[vertex]:

        if u not in (visited_vertices):

            Q.put(u)

            visited_vertices.append(u)

```

Step 4: [Output operation]

```

print("BFS traversal of graph with source A is:")

BFS(graph,"A")

end = time.time()

```

```
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
start = time.time()
from queue import Queue
graph =
{'A':['B','D','E','F'],'D':['A'],'B':['A','F','C'],'F':['B','A'],'C':['B'],'E':['A']}
print("Given Graph is : ")
print(graph)
def BFS(input_graph,source):
    Q = Queue()
    visited_vertices = list()
    Q.put(source)
    visited_vertices.append(source)
    while not Q.empty():
        vertex = Q.get()
        print(vertex,end= " ")
        for u in input_graph[vertex]:
            if u not in (visited_vertices):
                Q.put(u)
                visited_vertices.append(u)
print("BFS traversal of graph with source A is:")
BFS(graph,"A")
end = time.time()
```



```
print(f"Runtime of the program is {end - start}")
```

Output:

Given Graph is :

{'A': ['B', 'D', 'E', 'F'], 'D': ['A'], 'B': ['A', 'F', 'C'], 'F': ['B', 'A'], 'C': ['B'], 'E': ['A']}

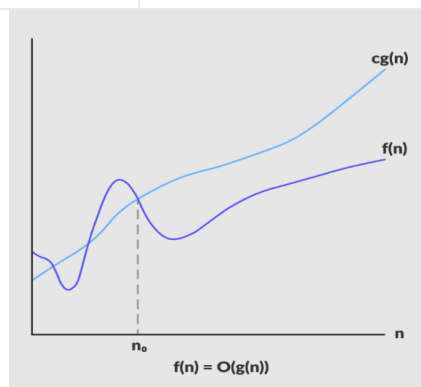
BFS traversal of graph with source A is:

A B D E F C

Runtime of the program is 0.1092679500579834

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time complexity is $O(|V|)$, where $|V|$ is the number of nodes. You need to traverse all nodes. Space complexity is $O(|V|)$ as well - since at worst case you need to hold all vertices in the queue.23-Mar-2012

2. Implementations of DFS.

Algorithm

Step 1: [Define graph & import time]

```
import time
```

```
start = time.time()
```

```
graph =
```

```
{'A':['B','D','E','F'],'D':['A'],'B':['A','F','C'],'F':['B','A'],'C':['B'],'E':['A']}
```

```
print("Given Graph is : ")
```

```
print(graph)
```

Step 2: [Create DFS_traversal function]

```
def dfs_traversal(input_graph,source):
```

```
    stack = list()
```

```
    visited_list = list()
```

```
    stack.append(source)
```

```
    visited_list.append(source)
```

```
    while stack:
```

```
        vertex = stack.pop()
```

```
        print(vertex,end = " ")
```

```
        for u in input_graph[vertex]:
```

```
            if u not in visited_list:
```

```
                stack.append(u)
```

```
                visited_list.append(u)
```

Step 3: [Output operation]

```
print("DFS traversal of graph with source A is:")
```

```
dfs_traversal(graph,"A")
```

```
end = time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Python Code

```
import time
```

```
start = time.time()
```

```
graph =
```

```
{'A':['B','D','E','F'],'D':['A'],'B':['A','F','C'],'F':['B','A'],'C':['B'],'E':['A']}
```

```

print("Given Graph is : ")
print(graph)
def dfs_traversal(input_graph,source):
    stack = list()
    visited_list = list()
    stack.append(source)
    visited_list.append(source)
    while stack:
        vertex = stack.pop()
        print(vertex,end = " ")
        for u in input_graph[vertex]:
            if u not in visited_list:
                stack.append(u)
                visited_list.append(u)
print("DFS traversal of graph with source A is:")
dfs_traversal(graph,"A")
end = time.time()

print(f"Runtime of the program is {end - start}")

```

Output:

Given Graph is :
{'A': ['B', 'D', 'E', 'F'], 'D': ['A'], 'B': ['A', 'F', 'C'], 'F': ['B', 'A'], 'C': ['B'], 'E': ['A']}

DFS traversal of graph with source A is:

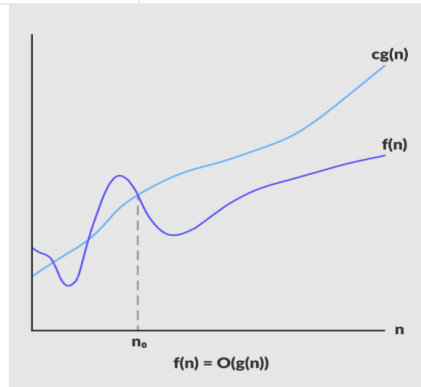
A F E D B C

Runtime of the program is 0.1561589241027832

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	O(1)	O(1)	O(n)
Insertion	O(1)	O(1)	O(n)

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$



Time complexity: $O(N)$ N is the number of nodes. · Space complexity: $O(H)$ H is the height of the tree.

Week 13

1. Implement Hash functions

Step 1: [Define variables of different datatypes & import time]

```
import time
```

```
start = time.time()
```

```
int_val = 4
```

```
str_val = 'GeeksforGeeks'
```

```
flt_val = 24.56
```

Step 2: [Print the variables]

```
print("The integer hash value is : " + str(hash(int_val)))
```

```
print("The string hash value is : " + str(hash(str_val)))
```

```
print("The float hash value is : " + str(hash(flt_val)))
```

```
end = time.time()
```

```
print(f"Runtime of the program is {end - start}")
```

Python Code

```

import time

start = time.time()

int_val = 4
str_val = 'GeeksforGeeks'
flt_val = 24.56
print("The integer hash value is : " + str(hash(int_val)))
print("The string hash value is : " + str(hash(str_val)))
print("The float hash value is : " + str(hash(flt_val)))
end = time.time()

print(f"Runtime of the program is {end - start}")

```

Output:

The integer hash value is : 4
 The string hash value is : -112777785087808093
 The float hash value is : 1291272085159665688
 Runtime of the program is 0.04675722122192383

Time Complexity For open addressing:

ACTIVITY	BEST CASE COMPLEXITY	AVERAGE CASE COMPLEXITY	WORST CASE COMPLEXITY
Searching	$O(1)$	$O(1)$	$O(n)$
Insertion	$O(1)$	$O(1)$	$O(n)$
Deletion	$O(1)$	$O(1)$	$O(n)$
Space Complexity	$O(n)$	$O(n)$	$O(n)$

