Report and Numerical study on K-Means Algorithm

Aim- To understand the theoretical and practical concepts of K-Means Algorithms and perfom a use case.

Abstract- Clustering is a type of Unsupervised learning. This is very often used when you don't have labeled data. K-Means Clustering is one of the popular clustering algorithm. The goal of this algorithm is to find groups(clusters) in the given data.

K-Means is a very simple algorithm which clusters the data into K number of clusters.

Dataset- We have used a simple unlabelled data that contains **3000 rows and 2 columns**

Algorithm- The algorithm is stated below:-

Step 1

We randomly pick K cluster centers(centroids). Let's assume these are c1,c2,...,ck, and we can say that;

C=c1,c2,...,ck

C is the set of all centroids.

Step 2

In this step we assign each input value to closest center. This is done by calculating Euclidean(L2) distance between the point and the each centroid.

argminci∈Cdist(ci,x)2

Where dist(.) is the Euclidean distance.

Step 3

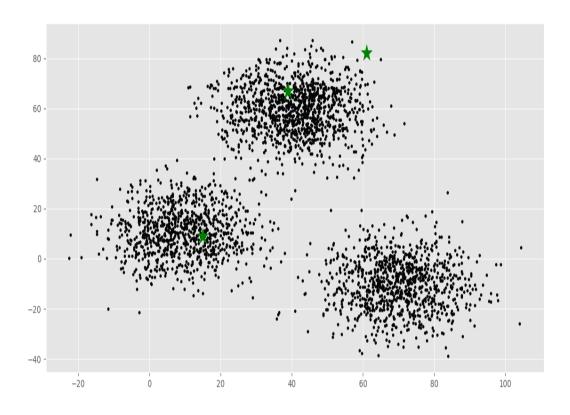
In this step, we find the new centroid by taking the average of all the points assigned to that cluster.

ci=1|Si|∑xi€Sixi

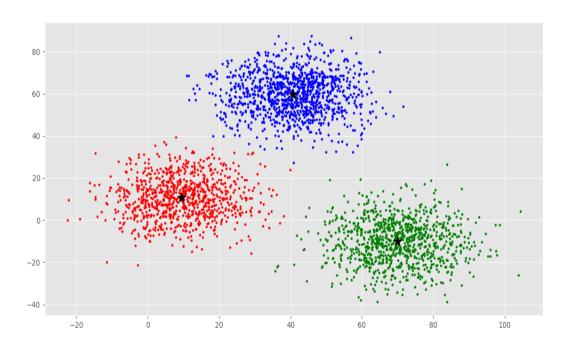
Si is the set of all points assigned to the ith cluster.

Step 4

In this step, we repeat step 2 and 3 until none of the cluster assignments change. That means until our clusters remain stable, we repeat the algorithm.

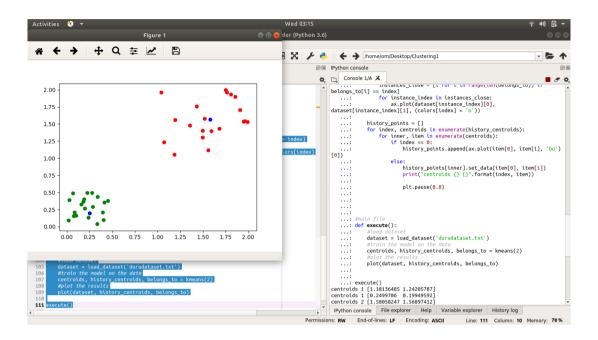


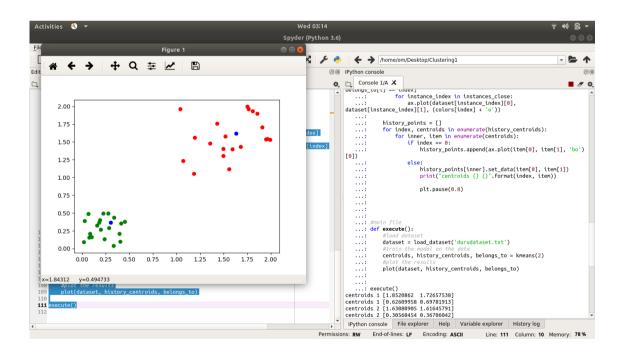
(fig 1-Shows initial centroid)



(fig2 shows updated centroid)

Example-2 The Second use case.





```
@author: om
#importing all the neccessary libraries
from copy import deepcopy
import numpy as np
import pandas as pd
from matplotlib import pyplot as plt
plt.rcParams['figure.figsize'] = (16, 9)
plt.style.use('ggplot')
# Importing the dataset
data = pd.read_csv('xclara.csv')
print("Input Data and Shape")
print(data.shape)
data.head()
# Getting the values and plotting it
f1 = data['V1'].values
f2 = data['V2'].values
X = np.array(list(zip(f1, f2)))
plt.scatter(f1, f2, c='black', s=7)
# Euclidean Distance Caculator
#it will give us sum of squarred errors across all the data points
#If axis is an integer, it specifies the axis of x along which to compute the vector norms.
# If axis is a 2-tuple, it specifies the axes that hold 2-D matrices, and the matrix norms of
these matrices are computed. If axis is None then either a vector norm (when x is 1-D) or a
matrix norm (when x is 2-D) is returned.
def dist(a, b, ax=1):
  return np.linalg.norm(a - b, axis=ax)
#Step-1 Randomly picking up the centroids
# Number of clusters
k = 3
# X coordinates of random centroids
C x = np.random.randint(0, np.max(X)-20, size=k)
#Y coordinates of random centroids
C_y = \text{np.random.randint}(0, \text{np.max}(X)-20, \text{size}=k)
#Desired dtype of the result
C = np.array(list(zip(C_x, C_y)), dtype=np.float32)
print("Initial Centroids")
print(C)
```

Code :- Created on Sat May 19 02:17:42 2018

```
# Plotting along with the Centroids
plt.scatter(f1, f2, c='#050505', s=7)
plt.scatter(C_x, C_y, marker='*', s=300, c='g')
# To store the value of centroids when it updates
C old = np.zeros(C.shape)
\# Cluster Lables(0, 1, 2)
clusters = np.zeros(len(X))
# Error func. - Distance between new centroids and old centroids
error = dist(C, C_old, None)
# Loop will run till the error becomes zero
while error != 0:
  #Step-2 Assign each data point with the closest centroid
  # Assigning each value to its closest cluster
  for i in range(len(X)):
     distances = dist(X[i], C)
     cluster = np.argmin(distances) #returns minimum values along axis
     clusters[i] = cluster
  # Storing the old centroid values
  #deep copy concept
  C_{old} = deepcopy(C)
  #Step-3 Finding new centroids by taking average
  # Finding the new centroids by taking the average value
  for i in range(k):
     points = [X[i]] for i in range(len(X)) if clusters[i] == i]
     C[i] = np.mean(points, axis=0)
  error = dist(C, C_old, None)
colors = ['r', 'g', 'b', 'y', 'c', 'm']
fig, ax = plt.subplots()
for i in range(k):
     points = np.array([X[i]] for i in range(len(X)) if clusters[i] == i])
     ax.scatter(points[:, 0], points[:, 1], s=7, c=colors[i])
ax.scatter(C[:, 0], C[:, 1], marker='*', s=200, c='#050505')
```