

③ Let  $I$  with  $i \in \{0, 1\}$  be the random variable.

$$\left. \begin{array}{l} \text{intruder} = 1 \\ \text{not intruder} = 0 \end{array} \right\}$$

be the alarm indicating variable.

Alarm will be raised if an intruder is identified with probability.

$$P(A=1 | I=1) = 0.98$$

and non-intruder probability  $P(A=1 | I=0) = 0.001$   
implies error factor.

Someone to be intruder  $P(I=1) = 0.00001$

Q - what is the probability that an alarm is raised when person is actually intruder?

sol-

$$P(I=1 | A=1) = \frac{P(A=1 | I=1) P(I=1)}{P(A=1)}$$

$$= \frac{P(A=1 | I=1) P(I=1)}{P(A=1 | I=1) P(I=1) + P(A=1 | I=0) P(I=0)}$$

$$= \frac{0.98 \times 0.00001}{0.98 \times 0.00001 + 0.001 \times 0.99999}$$

$$= \frac{0.98 \times 0.00001}{0.98 \times 0.00001 + 0.001 \times 0.99999}$$

i.e.

Intruder identified X Intruder  
Intruder identified X Intruder X error 0.001



$$= \frac{0.98 \times 0.00001}{0.98 \times 0.00001 + 0.001 \times (1 - 0.00001)}$$

$$\approx \frac{0.00001}{0.001} = \boxed{0.01}$$

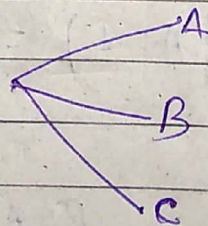
{ If he arrested as a intruder  
he is still most likely not a intruder  
with 99% of probability

formula

$$\frac{\text{Intruder} \times \text{Someone to be Intruder}}{\text{Intruder} \times \text{Someone to be Intruder} + \text{Not Intruder} \times (1 - \text{error})}$$

(5)

Question solves  
either of type



Probabilities of A ; B ~~and~~ or C  
30%, 20%, 50%.

during preparation, the student  
solved 9 of 10 problems of  
type A.



2 of 10 of type B, 6 of 10 of type C

find solve;

9 of 10  $\rightarrow$  A

2 of 10  $\rightarrow$  B

6 of 10  $\rightarrow$  C

Q probability that the student will solve the problem of exam?

$$P(\text{solved}) = P(\text{solved}|A) P(A) + P(\text{solved}|B) P(B) + P(\text{solved}|C) P(C)$$

$$= \left(\frac{9}{10} \cdot 30\%\right) + \left(\frac{2}{10} \cdot 20\%\right) + \frac{6}{10} \cdot 50\%$$

$$= \frac{27}{100} + \frac{4}{100} + \frac{30}{100}$$

$$= \frac{61}{100} = \boxed{0.61}$$

Total probability 100

Q what is the probability that it was of type A?

$$P(A|\text{solved}) = \frac{P(\text{solved}|A) P(A)}{P(\text{solved})} = \frac{\frac{9}{10} \cdot 30\%}{\frac{61}{100}}$$

$$= \frac{27/100}{61/100} = \frac{27}{61} = \boxed{0.442}$$



⑥ created bins of time frame of 5 min each.

In each time frame of 5 min, there may be a customer moving into the bank with 5% probability or there is no customer.

If a customer is detected by CCTV with probability 90%.

If no customer, camera take false photography with probability of 10%.

Q How many customers enter the bank on average day (10 hours)?

~~Q~~ consideration —  
average day = 10 hours

$$\begin{array}{l} \text{There are } 10 \times \boxed{12} = 120 \text{ five} \\ \text{minute periods} \\ \text{per day} \\ 1 \text{ hr} = 60 \text{ min} \\ 1 \text{ hr} = 12 \times \boxed{5} \text{ min} \\ \text{frame} \end{array}$$

In each period there is a probability of 5% for a customer to enter the bank.

So,

average number of person is

$$120 \times 5\% = \boxed{6}$$



Q How many false photograph (if no customer) and how many missed photograph (if customer but no photograph) are there on average per day?

— on average there is no person (~~120~~ - 6) of five-minute period false probability is 10%.

$$\text{so, } (120 - 6) \times 10\% = 11.4 \\ \text{false photograph}$$

on average there are 6 person, each of has probability of 1% of getting missed (~~99%~~ 100 - 99%)

thus number of missed photograph

$$6 \times 1\% = 6 \times 0.01 = \boxed{0.06}$$

Q If there is a photograph, probability that there is indeed a customer?

$$P(\text{person} | \text{photograph}) =$$

$$\frac{P(\text{person} | \text{photo}) P(\text{person})}{P(\text{person})}$$

$$= \frac{P(\text{person} | \text{photo}) P(\text{person})}{P(\text{person} | \text{photo}) P(\text{person}) + P(\text{person} | \text{no photo}) P(\text{no person})}$$

$$= \frac{0.99 \times 0.05}{0.99 \times 0.05 + 0.1 \times (1 - 0.05)}$$

$$= \frac{0.05}{0.05 + 0.1} = \boxed{0.333}$$



Ex-

Instance	classification	A1	A2
1	+	T	T
2	+	T	T
3	-	<del>T</del> F	F
4	+	F	F
5	-	F	T
6	-	F	T

- ① what is the entropy of this collection of training.
- ② what is the information gain (IG) of A2.

## Formulas

$$\text{Entropy}(S) = \sum_{i=1}^C -p_i \log_2 p_i$$

Sample set

Entropy( $S$ ) measures the impurity of  $S$  defined as -

- $C$  is the number of class labels
- $p$  refers to the proportion of values falling into the  $i$ th label.

$$\text{Information Gain}(S, A) = \text{Entropy}(S_{\text{be}}) - \frac{\text{Entropy}(S_{\text{as}})}{\text{Entropy}(S_{\text{as}})}$$

Individual Entropy sum

$$\text{Entropy}(S_{\text{as}}) = \sum_{i=1}^n (w_i) \text{Entropy}(p_i)$$

weight

① original dataset

<u>Scal-</u>	+	→ 3
	-	→ <u>3</u>
		count

$$p_i = 3/6 = 0.5$$

$$p_i = 3/6 = 0.5$$

$$\text{Total Entropy}(S_{\text{be}}) = -p_i \log_2 p_i$$

$$= 0.5 + 0.5 = \underline{\underline{1}}$$

② splitted dataset

<u>True</u> (AL)	+	-	Total
count	2	1	3
$p_i$	0.667	0.33	
$-p_i \log_2 p_i$	0.39	0.529	= 0.917

$$\text{Entropy}(AL) = 0.917 \times 0.992$$

<u>false</u> (AL)	+	-	Total
count	1	2	3
$p_i$	0.33	0.667	
$-p_i \log_2 p_i$	0.53	0.39	= 0.917

$$\text{Entropy}(AL) = 0.917 \times 0.992$$

0.92



split entropy

$$\text{Entropy}(S_{A1}) = \sum_{i=1}^n w_i \text{Entropy}(P_i)$$

$$= \frac{3}{6} * 0.923 + \frac{3}{6} * 0.923$$

$$= 0.923$$

Info. gain =  $1 - 0.923$   
 $\underline{\underline{= 0.077}}$

True false (a2)	+	-	Total		False (a2)	+	-	Total
count	2	2	4		count	1	1	2
Pi	0.5	0.5			Pi	0.5	0.5	
-Pi log Pi	0.5	0.5	2.1		-Pi log Pi	0.5	0.5	1

split entropy

$$\text{Entropy}(S_{A1}) = \sum_{i=1}^n w_i \text{Entropy}(P_i)$$

$$= \frac{4}{6} * 1 + \frac{2}{6} * 1$$

$$= \frac{6}{6} = 1$$

$$A_1 = 1 - 1 = 0$$

$$A_2 = 1 - 1 = 0$$

$$[A_1] \rightarrow [A_2]$$