

# Problem Set 2: Window-based Stereo Matching

**Due Monday, February 23rd, 2015 at 7:00 AM EST**

## Description

In class and in Forsyth and Ponce, chapter 7 we discussed window-based approaches to estimating dense stereo correspondence. In this problem set you will implement such approaches and evaluate it on some standard stereo pairs.

## What to submit

Download and unzip a template for your platform (also under: <https://www.udacity.com/wiki/ud810>):

- [ps2\\_octave\\_template.zip](#)
- [ps2\\_matlab\\_template.zip](#)
- [ps2\\_python\\_template.zip](#)

Rename it to ps2\_xxxx (i.e. ps2\_matlab, ps2\_octave, or ps2\_python) and add in your solutions:

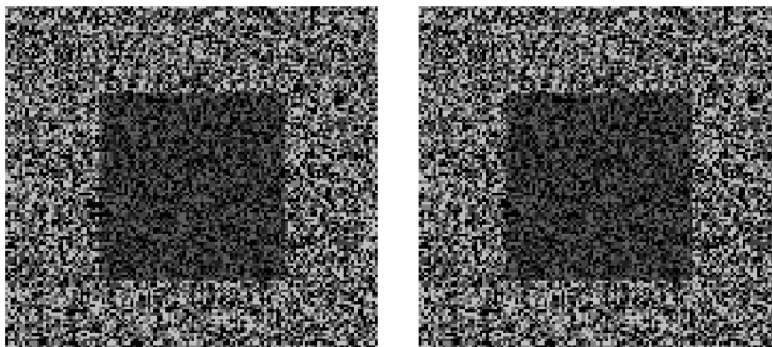
ps2\_xxxx/

- input/ - input images, videos or other data supplied with the problem set
- output/ - directory containing output images and other files your code generates
- ps2.m or ps2.py - code for completing each part, esp. function calls; all functions themselves must be defined in individual function files with filename same as function name, as indicated
- \*.m or \*.py - Matlab/Octave function files (one function per file), Python modules, any utility code
- ps2\_report.pdf - a PDF file with all output images and text responses

Zip it as ps2\_xxxx.zip, and submit on T-Square.

## Questions

1. Use the pair [pair0-L.png](#) and [pair0-R.png](#) - a central square moved 2 pixels horizontally:



Implement the basic stereo algorithm of taking a window around every pixel in one image and search for the best match along the same scan line in the other image. **You will do this both left to right and right to left.** Remember: Because of depth changes (discontinuities) some pixels visible in the left image are not in the right and vice a versa. So you will match in both directions.

For this part implement the simplest thing imaginable: Look for the smallest difference between the template window (source) and the proposed location window. Use the *sum of squared differences measure (SSD)*. We are going to take the definitions from: <https://software.intel.com/en-us/node/504333>

SSD is defined by:

$$S_{tx}(r, c) = \sum_{j=0}^{tplRows-1} \sum_{i=0}^{tplCols-1} \left[ t(j, i) - x\left(r+j-\frac{tplRows}{2}, c+i-\frac{tplCols}{2}\right) \right]^2$$

Basically you just sum up the squares. A “good” match, then, is when this value is at a minimum. That is, you are looking for the same image patch in both images.

- a. Implement the SSD match algorithm as function `disparity_ssd(L, R)` that returns a disparity image  $D(y, x)$  such that  $L(y, x) = R(y, x + D(y, x))$  when matching from left (L) to right (R).

Apply it to the two test images, matching from left to right:

```
L = im2double(imread(fullfile('input', pair0-L.png')));
R = im2double(imread(fullfile('input', pair0-R.png')));
D_L = disparity_ssd(L, R);
```

Also match from right to left:

```
D_R = disparity_ssd(R, L);
```

They should indicate a central square moved 2 pixels to the left or right, e.g.  $D_L$  should have value -2 in the approximate region of the central square, 0 elsewhere.

**Function file:** `disparity_ssd.m` containing function `disparity_ssd` (identical name)

**Output:** Save disparity images:

-  $D_L(y, x)$  [matching from left to right] as `ps2-1-a-1.png`

-  $D_R(y, x)$  [matching from right to left] as `ps2-1-a-2.png`

These disparity images may need to be scaled and shifted to display/write correctly.

2. Now we’re going to try this on a real image pair: `pair1-L.png` and `pair1-R.png`. Since these are color images, create grayscale versions. You can use **`rgb2gray`** or your own function.

- a. Again apply your SSD match function, and create a disparity image  $D(y, x)$  such that  $L(y, x) = R(y, x + D(y, x))$  when matching from left to right. Also match from right to left.

**Output:** Save disparity images, scaling/shifting as necessary:

-  $D_L(y, x)$  [matching from left to right] as `ps2-2-a-1.png`

-  $D_R(y, x)$  [matching from right to left] as `ps2-2-a-2.png`

- b. Also in the input directory are ground truth disparity images `pair1-D_dropL.png` and `pair1-D_R.png`. Compare your results.

**Output:** Text response - description of the differences between your results and ground truth.

3. SSD is not very robust to certain perturbations. We're going to try to see the effect of perturbations:
  - a. Using pair1, add some Gaussian noise, either to one image or both. Make the noise sigma big enough that you can tell some noise has been added. Run SSD match again.  
**Output:** Disparity images ( $D_L$  as ps2-3-a-1.png and  $D_R$  as ps2-3-a-2.png), text response - analysis of result compared to question 2.
  - b. Instead of the Gaussian noise, increase the contrast (multiplication) of one of the images by just 10%. Run SSD match again.  
**Output:** Disparity images ( $D_L$  as ps2-3-b-1.png and  $D_R$  as ps2-3-b-2.png), text response - analysis of result compared to question 2.
4. Now you're going to *use* (not implement yourself unless you want) an improved method, called **normalized correlation** – this is discussed in the book. The basic idea is that we think of two image patches as **vectors** and compute the angle between them – much like normalized dot products.

The explicit dot product of two image patches (treated as flat vectors) is:

$$R_{tx}(r, c) = \sum_{j=0}^{tplRows-1} \sum_{i=0}^{tplCols-1} t(j, i) \cdot x\left(r+j-\frac{tplRows}{2}, c+i-\frac{tplCols}{2}\right)$$

This result is then normalized:

$$\rho_{tx}(r, c) = \frac{R_{tx}(r, c)}{\sqrt{R_{xx}(r, c) R_{tt}\left(\frac{tplRows}{2}, \frac{tplCols}{2}\right)}}$$

- a. Implement a window matching stereo algorithm using some form of normalized correlation. Again, write this as a function `disparity_ncorr(L, R)` that returns a disparity image  $D(y, x)$  such that  $L(y, x) = R(y, x + D(y, x))$  when matching from left (L) to right (R).  
**Matlab has its own function `normxcorr2(template, A)` which implements:**

$$\gamma(u, v) = \frac{\sum_{x,y} [f(x, y) - \bar{f}_{u,v}] [t(x-u, y-v) - \bar{t}]}{\left\{ \sum_{x,y} [f(x, y) - \bar{f}_{u,v}]^2 \sum_{x,y} [t(x-u, y-v) - \bar{t}]^2 \right\}^{0.5}}$$

OpenCV has a variety of relevant functions and supported methods as well, such as `CV_TM_CCORR_NORMED`. **You MAY use these built-in normalized correlation functions.**

Test it on the original images both left to right and right to left ([pair1-L.png](#) and [pair1-R.png](#)).

**Output:** Disparity images ( $D_L$  as ps2-4-a-1.png and  $D_R$  as ps2-4-a-2.png), text response - description of how it compares to the SSD version and to the ground truth.

- b. Now test it on both the noisy and contrast-boosted versions from 2-a and 2-b.

**Output:** Disparity images (Gaussian noise:  $D_L$  as `ps2-4-b-1.png` and  $D_R$  as `ps2-4-b-2.png`; contrast-boosted:  $D_L$  as `ps2-4-b-3.png` and  $D_R$  as `ps2-4-b-4.png`), text response - analysis of results comparing original to noise and contrast-boosted images.

5. Finally, there is a second pair of images: `pair2-L.png` and `pair2-R.png`

- a. Try your algorithms on this pair. Play with the images – smooth, sharpen, etc. Keep comparing to the ground truth (`pair2-D_L.png` and `pair2-D_R.png`).

**Output:** Disparity images ( $D_L$  as `ps2-5-a-1.png` and  $D_R$  as `ps2-5-a-2.png`), text response - analysis of what it takes to make stereo work using a window based approach.