

# PERCENTAGES

## BASIC DEFINITION OF PERCENTAGE

The word per cent means per hundred or for every hundred. The symbol ‘%’ is used for the term percent. Thus, 20 per cent is written as 20% and it means 20 out of 100.

This is written in ratio form as  $\frac{20}{100}$ .

The percentage value of a ratio is obtained when we multiplying the ratio by 100.

Thus percentage value of the ratio  $\frac{3}{5}$  will be  $\frac{3}{5} \times 100\% = 60\%$ .

**Illustration 1:** A person saves ₹ 5,000 per month from his monthly salary ₹ 30,000. Find the percentage monthly saving of the person.

**Solution:** Out of monthly salary ₹ 30,000, saving is ₹ 5,000

$$\Rightarrow \text{Out of monthly salary ₹ 1, saving is } \frac{5,000}{30,000}$$

$$\Rightarrow \text{Out of monthly salary ₹ 100, saving is } \frac{5,000}{30,000} \times 100 \\ = ₹ \frac{50}{3} = ₹ 16.67 \text{ (approx.)}$$

Hence percentage monthly saving = 16.67% (approx.)

**Illustration 2:** 250 students of ABC school and 350 students of XYZ school appeared in secondary board examination conducted by CBSE in 2013. 20 students of ABC school and 25 students of XYZ school did not pass in this board examination. Students of which of the two schools ABC and XYZ have shown poor performance?

**Solution:** We cannot compare the performance of the students of the two schools in secondary board examination by just looking the number of students 20 of ABC school and 25 of XYZ school who did not pass in secondary board examination.

To compare the performance, you have to find the percentage of the students who did not pass the secondary board examination of each school out of those students of each school who appeared in the secondary board examination.

Percentage of the students of ABC school who did not pass

$$= \frac{20}{250} \times 100\% = 8\%$$

Percentage of the student of XYZ school who did not pass

$$= \frac{25}{350} \times 100\% = 7.1\% \text{ (approximately)}$$

Hence students of the XYZ school have shown poor performance.

**Illustration 3:** In a survey, voters of a national party A are increase by 2.5 lakhs and voters of national party B are increase by 4 lakhs in 2012. Which party A or B has grown more in 2012?

**Solution:** In first shot the answer to the question seems to be national party B. But actually the question can not be answered, because we don't know the just previous year's voters of each of the national party A and B.

If we had further information that in 2011, voters of national party A were 5 lakhs and voters of national party B were 10 lakhs, we can compare growth rates of two national parties.

Percentage growth rate of national party A in 2012

$$= \frac{250000}{500000} \times 100\% = 50\%$$

Percentage growth rate of national party B in 2012

$$= \frac{400000}{1000000} \times 100\% = 40\%$$

Hence, national party A has higher growth rate in 2012. Thus national party A has grown more than B in 2012.

In the illustrations 2 and 3, you have seen that percentage is the most powerful tool for comparing the data. 500000 and 1000000 in illustration 3 are called base values of percentage growth rate of party A and party B respectively.

Without knowing these base values, percentage growth rate of party A and party B could not be determined.

Thus percentage of anything (let X) =  $\frac{\text{Value of } X}{\text{Base value of } X} \times 100$

In illustration 1, ₹ 30000 is the base value of percentage monthly saving. In illustration 2, 250 is the base value of the percentage of students of ABC school who did not pass and 350 is the base value of the percentage of student of XYZ school who did not pass.

**Illustration 4:** Express the following as fraction

(a) 25%

(b)  $33\frac{1}{3}\%$

**Solution :**

$$(a) 25\% = \frac{25}{100} \left( \text{Since \% means } \frac{1}{100} \right) = \frac{1}{4}$$

$$(b) 33\frac{1}{3}\% = \frac{100}{3}\% = \frac{100}{3 \times 100} = \frac{1}{3}$$

**Illustration 5:** 25% of a number is 80. What is the number ?

**Solution:**

Let the number be  $X$ . According to the given condition

$$\frac{25}{100} \times X = 80 \Rightarrow X = \frac{80 \times 100}{25} = 320.$$

**Illustration 6:** Express  $\frac{1}{8}$  as a percentage.

$$\text{Solution: } \frac{1}{8} = \frac{1}{8} \times 100\% = 12.5\%$$

$$= \frac{100}{8}\% = \frac{25}{2}\% = 12\frac{1}{2}\%$$

**Illustration 7:** Two third of three fifth of one eighth of a certain number is 268.50. What is 30% of the number?

(a) 1611

(b) 1616

(c) 1343

(d) 594.60

**Solution:** (a) Let the number be  $x$ .

According to the question  $\frac{2}{3}$  of  $\frac{3}{5}$  of  $\frac{1}{8}$  of  $x = 268.50$

$$\Rightarrow \frac{2}{3} \times \frac{3}{5} \times \frac{1}{8} \times x = 268.50$$

$$x = \frac{268.50 \times 3 \times 5 \times 8}{2 \times 3} = 5370$$

$$30\% \text{ of } x = \frac{30}{100} \times 5370 = 1611.00$$

**Illustration 8:** 4598 is 95% of ?

(a) 4800

(b) 4840

(c) 4850

(d) 4880

**Solution:** (b) Let 95% of  $x = 4598$ .

$$\text{Then, } \frac{95}{100} \times x = 4598 \Rightarrow x = \left( 4598 \times \frac{100}{95} \right) = 4840.$$

## PERCENTAGE INCREASE, PERCENTAGE DECREASE AND PERCENTAGE CHANGE

$$\text{Percentage increase} = \frac{\text{Increase}}{\text{Initial value (i.e., Base value)}} \times 100$$

$$\text{Percentage decrease} = \frac{\text{Decrease}}{\text{Initial value (i.e., Base value)}} \times 100$$

$$\text{Percentage change} = \frac{\text{Change}}{\text{Initial value (i.e., Base value)}} \times 100$$

Let income of a family in the years 2010, 2011 and 2012 are ₹ 50000, ₹ 80000 and ₹ 60000 respectively.

Here income of the family increases in 2011 but decreases in 2012.

Increase in family income in 2011 from 2010

$$\begin{aligned} &= (\text{Higher Income}) - (\text{Lower Income}) \\ &= (\text{Income in 2011}) - (\text{Income in 2010}) \\ &= ₹ 80000 - ₹ 50000 = ₹ 30000 \end{aligned}$$

Decrease in family income in 2012 from 2011

$$\begin{aligned} &= (\text{Higher Income}) - (\text{Lower Income}) \\ &= (\text{Income in 2011}) - (\text{Income in 2012}) \\ &= ₹ 80000 - ₹ 60000 = ₹ 20000 \end{aligned}$$

Percentage increase in family income in 2011 from 2010

$$\begin{aligned} &= \frac{(\text{Increase in income})}{(\text{Income in 2010})} \times 100 \\ &= \frac{30000}{50000} \times 100 = 60\% \end{aligned}$$

Percentage decrease in family income in 2012 from 2011

$$\begin{aligned} &= \frac{(\text{Decrease in income})}{(\text{Income in 2011})} \times 100 \\ &= \frac{20000}{80000} \times 100 = 25\% \end{aligned}$$

**Illustration 9:** Rent of the house is increased from ₹ 7000 to ₹ 7700. Express the increase in price as a percentage of the original rent.

**Solution:**

$$\text{Increase value} = ₹ 7700 - ₹ 7000 = ₹ 700$$

$$\begin{aligned} \text{Increase \%} &= \frac{\text{Increase value}}{\text{Base value}} \times 100 = \frac{700}{7000} \times 100 \\ &= 10 \end{aligned}$$

∴ Percentage rise = 10 %.

**Illustration 10:** The cost of a bike last year was ₹ 19000. Its cost this year is ₹ 17000. Find the percent decrease in its cost.

**Solution:**

$$\% \text{ decrease} = \frac{19000 - 17000}{19000} \times 100$$

$$= \frac{2000}{19000} \times 100 = 10.5\%$$

∴ Percent decrease = 10.5 %.

If the value of any thing increases, then percentage change is the percentage increase and if the value of any thing decreases, then percentage change is the percentage decrease. Thus,

Percentage change = Percentage increase, if value of any thing increases

and Percentage change = Percentage decrease, if value of anything decreases.

# Practice Exercise

## Level - I

1. In a public library there are 110,000 books, 40% of which are science books. It was decided to add 20,000 new books to the library. How many of the new books should be science books in order to bring the percentage of science books in the library up to 45%?  
 (a) 15000 (b) 1500 (c) 1450 (d) 14500
2. A batsman scored 110 runs which included 3 boundaries and 8 sixes. What percent of his total score did he make by running between the wickets ?  
 (a) 45% (b)  $45\frac{5}{11}\%$   
 (c)  $54\frac{6}{11}\%$  (d) 55%
3. A student secures 90%, 60% and 54% marks in test papers with 100, 150 and 200 respectively as maximum marks. The percentage of his aggregate is:  
 (a) 64 (b) 68  
 (c) 70 (d) None of these
4. If two numbers are respectively 20% and 50% of a third number, what is the percentage of the first number to the second ?  
 (a) 10 (b) 20 (c) 30 (d) 40
5. In an examination, 5% of the applicants were found ineligible and 85% of the eligible candidates belonged to the general category. If 4275 eligible candidates belonged to other categories, then how many candidates applied for the examination ?  
 (a) 30,000 (b) 35,000  
 (c) 37,000 (d) None of these
6. Deepa decided to donate 8% of her salary to an orphanage. On the day of donation she changed her mind and donated ₹ 2240 which was 80% of what she had decided earlier. How much is Deepa's salary?  
 (a) ₹ 36000 (b) ₹ 42000  
 (c) ₹ 35000 (d) ₹ 45000
7. When the price of a radio was reduced by 20%, its sale increased by 80%. What was the net effect on the sale?  
 (a) 44% increase (b) 44% decrease  
 (c) 66% increase (d) 75% increase
8. If the price of sugar is increased by 7%, then by how much per cent should a housewife reduce her consumption of sugar, to have no extra expenditure?  
 (a) 7 over 107% (b) 107 over 100%  
 (c) 100 over 107% (d) 7%
9. A salesman's terms were changed from a flat commission of 5% on all his sales to a fixed salary of ₹ 1,000 plus 2.5% commission on all sales exceeding ₹ 4,000. If his remuneration as per the new scheme was ₹ 600 more than by the first scheme, what were his sales worth?  
 (a) 10,000/- (b) 11,000/- (c) 12,000/- (d) 14,000/-
10. An inspector rejects 0.08% of the metres as defective. How many metres will he examine to reject 2 metres?  
 (a) 200m (b) 250m  
 (c) 2500m (d) 3000m
11. A invested 10% more than B. B invested 10% less than C. If the total sum of their investment is ₹ 14450. how much did C get?  
 (a) ₹ 5000 (b) ₹ 4800  
 (c) ₹ 5100 (d) None of these
12. A sum of ₹ 4558 is divided among A, B and C such that A receives 20% more than C, and C receives 25% less than B. What is A's share in the amount ?  
 (a) ₹ 1548 (b) ₹ 1720  
 (c) ₹ 1290 (d) ₹ 1345
13. In an election between two candidates, 75% of the voters cast their votes, out of which 2% of the votes were declared invalid. A candidate got 9261 votes which were 75% of total valid votes. Find the total number of votes enrolled in that election.  
 (a) 16080 (b) 16800  
 (c) 18600 (d) 16008
14. A spider climbed  $62\frac{1}{2}\%$  of the height of the pole in one hour and in the next hour it covered  $12\frac{1}{2}\%$  of the remaining height. If the height of the pole is 192 m, then distance climbed in second hour is:  
 (a) 3 m (b) 5 m  
 (c) 7 m (d) 9 m
15. A number is increased by 10% and then reduced by 10%. After these operations, the number:  
 (a) does not change (b) decreases by 1%  
 (c) increases by 1% (d) increases by 0.1%
16. The difference between the value of a number increased by 25% and the value of the original number decreased by 30% is 22. What is the original number ?  
 (a) 70 (b) 65  
 (c) 40 (d) 90
17. A salesman is allowed  $5\frac{1}{2}\%$  discount on the total sales made by him plus a bonus of  $\frac{1}{2}\%$  on the sales over ₹ 10,000. If his total earnings were ₹ 1990, then his total sales (in ₹) were:  
 (a) 30,000 (b) 32,000  
 (c) 34,000 (d) 35,000
18. If 12% of 75% is greater than 5% of a number by 75, the number is  
 (a) 1875 (b) 1890  
 (c) 1845 (d) 1860



37. A city had a population of 30,00,000 in the beginning of 1999. Its average growth rate is 4% per year, but due to a massive earthquake in 2001, its population is reduced by 8% in that year. But it again maintained the same growth rate of 4% in following years. What will be the approx. population of the city at the end of 2003?
- (a) 32,06,460      (b) 34,68,420  
 (c) 31,52,360      (d) 32,28,810
38. In a factory there are three types of machines  $M_1$ ,  $M_2$  and  $M_3$  which produces 25%, 35% and 40% of the total products respectively.  $M_1$ ,  $M_2$  and  $M_3$  produces 2%, 4% and 5% defective products, respectively. What is the percentage of non-defective products?
- (a) 89%      (b) 97.1%      (c) 96.1%      (d) 86.1%
39. A person saves 6% of his income. Two years later, his income shoots up by 15% but his savings remain the same. Find the hike in his expenditure.
- (a) 15.95%      (b) 15%      (c) 14.8%      (d) 15.5%
40. In the half yearly exam only 70% of the students were passed. Out of these (passed in half yearly) only 60% student are passed in annual exam. Out of those who did not pass the half yearly exam, 80% passed in annual exam. What percent of the students passed the annual exam?
- (a) 42%      (b) 56%  
 (c) 66%      (d) None of these
41. Two vessels contain equal quantities of 40% alcohol. Anil changed the concentration of the first vessels to 50% by adding extra quantity of pure alcohol. Balu changed the concentration of the second vessels to 50% replacing a certain quantity of the solution with pure alcohol. By what percentage is the quantity of alcohol added by Anil more than that replaced by Balu?
- (a) 20%      (b) 25%  
 (c) 40%      (d) Cannot be determined
42. Lagaan is levied on the 60% of the cultivated land. The revenue department collected total ₹ 3,84,4000 through the lagaan from the village of Sukhiya. Sukhiya, a very rich farmer, paid only ₹ 480 as lagaan. The percentage of total land of Sukhiya over the total taxable land of the village is:
- (a) 0.15%      (b) 15%  
 (c) 0.125%      (d) None of these
43. In an election between 2 candidates, Bhiku gets 65% of the total valid votes. If the total votes were 6000, what is the number of valid votes that the other candidate Mhatre gets if 25% of the total votes were declared invalid?
- (a) 1625      (b) 1575  
 (c) 1675      (d) 1525
44. A machine depreciates in value each year at the rate of 10% of its previous value. However, every second year there is some maintenance work so that in that particular year, depreciation is only 5% of its previous value. If at the end of the fourth year, the value of the machine stands at ₹ 1,46,205, then find the value of machine at the start of the first year.
- (a) ₹ 1,90,000      (b) ₹ 2,00,000  
 (c) ₹ 1,95,000      (d) ₹ 2,10,000
45. After three successive equal percentage rise in the salary the sum of 100 rupees turned into 140 rupees and 49 paise. Find the percentage rise in the salary.
- (a) 12%      (b) 22%  
 (c) 66%      (d) 82%
46. The salary of Anil and Vinit is 20% and 30% less than the salary of Dheeraj respectively. By what percentage is the salary of Anil more than the salary of Vinit?
- (a) 33.33%      (b) 50%  
 (c) 10%      (d) 14.28%
47. In a certain town, at least 50% of the people read a newspaper. Among those who read a newspaper, at most 25% read more than one paper. Only one of the following statements follows from the statements given below. Which one is it?
- (a) At the most 25% read exactly one newspaper  
 (b) At least 25% read all the newspaper  
 (c) At the most 37½% read exactly one newspaper  
 (d) At least 37½% read exactly one newspaper
48. Kajal spends 55% of her monthly income on grocery, clothes and education in the ratio of 4 : 2 : 5 respectively. If the amount spent on clothes is ₹ 5540/-, what is Kajal's monthly income? [SBI Clerk-2012]
- (a) ₹ 55,400/-      (b) ₹ 54,500/-  
 (c) ₹ 55,450/-      (d) ₹ 55,650/-  
 (e) None of these
49. 35 percent of a number is two times 75 percent of another number. What is the ratio between the first and the second number respectively? [SBI Clerk-2012]
- (a) 35 : 6      (b) 31 : 7  
 (c) 23 : 7      (d) 32 : 9  
 (e) None of these
50. Last year there were 610 boys in a school. The number decreased by 20 percent this year. How many girls are there in the school if the number of girls is 175 percent of the total number of boys in the school this year? [SBI Clerk-2012]
- (a) 854      (b) 848  
 (c) 798      (d) 782  
 (e) None of these
51. Aryan got 350 marks and Vidya scored 76 percent marks in the same test. If Vidya scored 296 marks more than Aryan, what were the maximum marks of the test? [SBI Clerk-2012]
- (a) 650      (b) 900  
 (c) 850      (d) 950  
 (e) None of these
52. A student was awarded certain marks in an examination. However, after re-evaluation, his marks were reduced by 40% of the marks that were originally awarded to him so that the new score now became 96. How many marks did the student lose after re-evaluation? [SBI Clerk-2012]
- (a) 58      (b) 68  
 (c) 63      (d) 56  
 (e) 64
53. 855 candidates applied for a job, out of which 80% of the candidates were rejected. How many candidates were selected for the job? [SBI Clerk-2012]
- (a) 684      (b) 151  
 (c) 676      (d) 179  
 (e) None of these

**84** ● **Percentages**

54. A shopkeeper purchased 200 bulbs for ₹ 10 each. However, 5 bulbs were fused and had to be thrown away. The remaining were sold at ₹ 12 each. What will be the percentage profit ? [SBI Clerk-2014]  
 (a) 25 (b) 15  
 (c) 13 (d) 17  
 (e) None of these
55. Ajay spends 25 per cent of his salary on house rent, 5 per cent on food, 15 per cent on travel, 10 per cent on clothes and the remaining amount of ₹ 27,000 is saved. What is Ajay's income ? [SBI Clerk-2014]  
 (a) ₹ 60,000 (b) ₹ 80,500  
 (c) ₹ 60,700 (d) ₹ 70,500  
 (e) None of these
56. The salary of an employee increases every year in the month of July by 10%. If his salary in May 2000 was ₹ 15,000, his salary in October 2001 was [SSC-Sub. Ins.-2012]  
 (a) ₹ 16,500 (b) ₹ 18,000  
 (c) ₹ 18,150 (d) ₹ 19,965
57. 72% of the students of a certain class took Biology and 44% took Mathematics. If each student took Biology or Mathematics and 40 took both, the total number of students in the class was [SSC-Sub. Ins.-2012]  
 (a) 200 (b) 230  
 (c) 250 (d) 320
58. In a big garden 60% of the trees are coconut trees, 25% of the number of coconut trees are mango trees and 20% of the number of mango trees are apple trees. If the number of apple trees are 1500, then the number of trees in the garden is : [SSC-Sub. Ins.-2013]  
 (a) 48000 (b) 50000  
 (c) 51000 (d) 45000
59. If  $50\% \text{ of } (P - Q) = 30\% \text{ of } (P + Q)$  and  $Q = x\% \text{ of } P$ , then the value of  $x$  is: [SSC-Sub. Ins.-2013]  
 (a) 30 (b) 25  
 (c) 20 (d) 50
61. In an examination 75% candidates passed in English and 60% passed in Mathematics. 25% failed in both and 240 passed the examination. Find the total number of candidates. [SSC-Sub. Ins.-2014]  
 (a) 492 (b) 300  
 (c) 500 (d) 400
62. If  $40\% \text{ of } \frac{4}{5} \text{ of } \frac{3}{4}$  of a number is 48, then what is 1% of the same number ? [SSC-Sub. Ins.-2014]  
 (a) 20 (b) 2  
 (c) 10 (d) 1
63. Two persons contested an election of Parliament. The winning candidate secured 57% of the total votes polled and won by a majority of 42,000 votes. The number of total votes polled is [SSC-MT-2013]  
 (a) 4,00,000 (b) 5,00,000  
 (c) 6,00,000 (d) 3,00,000
64. A number when reduced by 10% gives 30. The number is [SSC-MT-2013]  
 (a) 35 (b)  $33\frac{1}{2}$   
 (c)  $33\frac{1}{3}$  (d) 40
65. A team played 40 games in a season and won in 24 of them. What percent of games played did the team win ? [SSC 10+2-2012]  
 (a) 70% (b) 40%  
 (c) 60% (d) 35%
66. If  $125\% \text{ of } x$  is 100, then  $x$  is : [SSC 10+2-2012]  
 (a) 80 (b) 150  
 (c) 400 (d) 125
67. In the annual examination Mahuya got 10% less marks than Supriyo in Mathematics. Mahuya got 81 marks. The marks of Supriyo is [SSC 10+2-2013]  
 (a) 89 (b) 90  
 (c) 87 (d) 88
68. Ram's income is greater than Shyam's income by 20%. Then the percent by which Shyam's income is less than Ram's income is [SSC 10+2-2013]  
 (a)  $16\frac{2}{3}$  (b)  $18\frac{2}{5}$   
 (c)  $10\frac{1}{5}$  (d)  $12\frac{1}{3}$
69. 1% of 1% of 25% of 1000 is [SSC 10+2-2014]  
 (a) .025 (b) .0025  
 (c) 25 (d) .000025





38. Recently I had gone to a locality called Shadigarh for conducting a survey about the number of married persons in the locality. The population of the locality is 7,200 and  $\frac{1}{18}$  th of those are males and the rest females. If 40% of the males are married, find percentage of married females in the locality  
 (a)  $48\frac{1}{7}\%$       (b)  $52\frac{4}{7}\%$   
 (c)  $62\frac{6}{7}\%$       (d)  $71\frac{1}{7}\%$
39. Chintu is given a quadratic equation  $ax^2 + bx + c = 0$  and is asked to make another quadratic equation from this with  $a = 1$ . Also one root of the second quadratic equation is same as one of the roots of the first equation but opposite in sign and the other root of the second equation is two times the second root of the first equation. Find the percentage change in the constant term of the second equation as compared to the first equation?  
 (a) 200% increase      (b) 300% decrease  
 (c) 400% increase      (d) 100% decrease
40. A salesgirl's terms were changed from a flat commission of 5% on all her sales to a fixed salary of ₹ 1000 plus 2.5% commission on all sales exceeding ₹ 4000. If her remuneration as per the new scheme was ₹ 600 more than that by the previous scheme, her total sales was [SBI PO-2011]  
 (a) ₹10000      (b) ₹5000  
 (c) ₹2000      (d) ₹12000  
 (e) None of these
41. Six-eleventh of a number is equal to twenty-two percent of second number. Second number is equal to the one-fourth of third number. The value of the third number is 2400. What is the 45% of first number? [IBPS-PO-2011]  
 (a) 109.8      (b) 111.7  
 (c) 117.6      (d) 123.4  
 (e) None of these
42. An HR Company employs 4800 people, out of which 45 percent are males and 60 percent of the males are either 25 years or older. How many males are employed in that HR Company who are younger than 25 years ? [IBPS-PO-2011]  
 (a) 2640      (b) 2160  
 (c) 1296      (d) 864  
 (e) None of these
43. In a test, a candidate secured 468 marks out of maximum marks 'A'. If the maximum marks 'A' were converted to 700 marks, he would have secured 336 marks. What were the maximum marks of the test? [IBPS-PO-2011]  
 (a) 775      (b) 875  
 (c) 975      (d) 1075  
 (e) None of these
44. Sum of three consecutive numbers is 2262. What is 41 % of the highest number ? [IBPS-PO-2012]  
 (a) 301.51      (b) 303.14  
 (c) 308.73      (d) 306.35  
 (e) 309.55
45. Akash scored 73 marks in subject A. He scored 56% marks in subject B and X marks in subject C. Maximum marks in each subject were 150. The overall percentage marks obtained by Akash in all the three subjects together were 54%. How many marks did he score in subject C ? [IBPS-PO-2012]  
 (a) 84      (b) 86  
 (c) 79      (d) 73  
 (e) None of these
46. In an examination, Raman scored 25 marks less than Rohit. Rohit scored 45 more marks than Sonia. Rohan scored 75 marks which is 10 more than Sonia. Ravi's score is 50 less than, maximum marks of the test. What approximate percentage of marks did Ravi score in the examination, if he gets 34 marks more than Raman? [IBPS-PO-2013]  
 (a) 90      (b) 70  
 (c) 80      (d) 60  
 (e) 85
47. Mr Giridhar spends 50% of his monthly income on household items and out of the remaining he spends 50% on transport, 25% on entertainment, 10% on sports and the remaining amount of ₹ 900 is saved. What is Mr Giridhar's monthly income? [IBPS-PO-2013]  
 (a) ₹6000      (b) ₹12000  
 (c) ₹9000      (d) Cannot be determined  
 (e) None of these
48. Rakesh got 273 marks in an examination and scored 5% more than the pass %. If Lokesh got 312 marks, then by what % above the pass mark did he pass the examination? [SSC CGL-2013]  
 (a) 20%      (b) 27%  
 (c) 25%      (d) 15%
49. The monthly salaries of A and B together amount to ₹ 40,000. A spends 85% of his salary and B, 95% of his salary. If now their savings are the same, then the salary (in ₹) of A is [SSC CGL-2014]  
 (a) 10,000      (b) 12,000  
 (c) 16,000      (d) 18,000
50. One litre of water is evaporated from 6 litres of a solution containing 5% salt. The percentage of salt in the remaining solution is [SSC CGL-2014]  
 (a)  $4\frac{4}{9}\%$       (b)  $5\frac{5}{7}\%$   
 (c) 5%      (d) 6%

# Hints & Solutions



## Level-I

1. (d) Let  $X$  be the number of new science books. Then,  
Total Science books / Total books = 45%.

$$\Rightarrow \frac{\left( X + 110000 \times \frac{40}{100} \right)}{(20000 + 10000)} = \frac{45}{100} \Rightarrow X = 14500.$$

2. (b) Number of runs made by running  
 $= 110 - (3 \times 4 + 8 \times 6) = 50.$

$$\therefore \text{Required percentage} = \left( \frac{50}{110} \times 100 \right)\% \\ = 45 \frac{5}{11}\%$$

3. (a) Total marks secured = (90% of 100 + 60% of 150 + 54% of 200)  
 $= \left( \frac{90}{100} \times 100 + \frac{60}{100} \times 150 + \frac{54}{100} \times 200 \right)$   
 $= (90 + 90 + 108) = 288.$   
Total maximum marks = (100 + 150 + 200) = 450.

$$\therefore \text{Aggregate Percentage} = \left( \frac{288}{450} \times 100 \right)\% = 64\%$$

4. (d) Let the third number be 100. Then, the first and second numbers will be 20 and 50, respectively.

$$\text{Required \%} = \frac{20}{50} \times 100 = 40\%$$

5. (a) Let the total number of applicants be  $x$ . Number of eligible candidates = 95% of  $x$ . Eligible candidates of other categories = 15% of (95% of  $x$ )

$$= \left( \frac{15}{100} \times \frac{95}{100} \right) \times x = \frac{57}{400} x$$

$$\therefore \frac{57}{400} x = 4275 \Leftrightarrow x = \left( \frac{4275 \times 400}{57} \right) = 30000$$

6. (c) Let the salary of Deepa be ₹  $x$ .  
Then, 80% of 8% of  $x$  = 2240

$$\Rightarrow \frac{80}{100} \times \frac{8}{100} \times x = 2240$$

$$\Rightarrow x = \frac{2240 \times 100 \times 100}{80 \times 8} = 35000$$

Hence, the salary of Deepa = ₹ 35000

7. (a) Let the original price be  $x$  and sale be of  $y$  units.  
Then, the revenue collected initially =  $x \times y$

Now, new price = 0.8  $x$ , new sale = 1.8  $y$   
Then, new revenue collected = 1.44  $xy$

$$\% \text{ increase in revenue} = \frac{0.44xy}{xy} \times 100 \\ = 44\% \text{ increase}$$

8. (a) % reduction in consumption

$$= \frac{\% \text{ change in price}}{100 + \% \text{ change in price}} \times 100 \\ = \frac{7}{100 + 7}\% = \frac{7}{107}\%$$

9. (c) Let his sales be worth ₹  $x$ . Then,  
1000 + 2.5% of ( $x - 4000$ ) = 5% of  $x + 600$

$$\Rightarrow \frac{5x}{100} - \frac{2.5(x - 4000)}{100} = 1000 - 600 \\ \Rightarrow 2.5x + 10000 = 40,000 \\ \Rightarrow x = \frac{30,000}{2.5} = 12,000$$

10. (c) Let the inspector examined  $x$  metres,  
then 0.08% of  $x$  = 2

$$\Rightarrow \frac{x \times 0.08}{100} = 2$$

$$\text{or } x = \frac{200}{0.08} = 2500 \text{ metres}$$

11. (a) Let the investment of  $C$  = ₹ 100  
Then  $B$ 's investment = ₹ 90 and  $A$ 's investment = ₹ 99  
Sum of investment = ₹ (100 + 90 + 99) = ₹ 289

$$\text{Hence, } C\text{'s actual investment} = \text{₹} \left( \frac{14450 \times 100}{289} \right) \\ = ₹ 5000$$

12. (a) Let  $B$  get ₹  $x$ . Then  $C$  gets = 75% of  $x = \frac{3x}{4}$

$$\text{and } A \text{ gets} = 120\% \text{ of } \frac{3x}{4} = \frac{120}{100} \times \frac{3x}{4} = \frac{9x}{10}$$

$$\text{Now, } \frac{9x}{10} + \frac{3x}{4} + x = 4558$$

$$\Rightarrow \frac{53x}{20} = 4558 \Rightarrow x = \frac{4558 \times 20}{53} = 1720$$

$$\text{Hence, } A\text{'s share} = \frac{9x}{10} = ₹ \frac{9 \times 1720}{10} = ₹ 1548$$

## Percentages • 89

13. (b) Let the total number of votes enrolled be  $x$ . Then,  
Number of votes cast = 75% of  $x$ . Valid votes = 98% of (75% of  $x$ ).  
 $\therefore 75\% \text{ of } [98\% \text{ of } (75\% \text{ of } x)] = 9261$

$$\Rightarrow \left( \frac{75}{100} \times \frac{98}{100} \times \frac{75}{100} \times x \right) = 9261$$

$$\Rightarrow x = \left( \frac{9261 \times 100 \times 100 \times 100}{75 \times 98 \times 75} \right) = 16800.$$

14. (d) Height climbed in second hour

$$= 12 \frac{1}{2}\% \text{ of } \left( 100 - 62 \frac{1}{2}\% \text{ of } 192 \text{ m} \right)$$

$$= \left( \frac{25}{2} \times \frac{1}{100} \times \frac{75}{2} \times \frac{1}{100} \times 192 \right) \text{ m} = 9 \text{ m.}$$

15. (b) Let the original number be 100.  
Then, the new number =  $100 \times 1.1 \times 0.9 = 99$

$\therefore$  Reqd. ratio of population of males and females

$$= \frac{4000}{9000 - 4000} = \frac{4000}{5000} = 4 : 5$$

21. (d) Let salary of Saroj be ₹  $x$ .

$$\therefore \text{Salary of Raju} = \frac{80}{100} x$$

$$\text{Salary of Ram} = \frac{70}{100} x$$

$$\text{Required percentage} = \left( \frac{\frac{80x}{100} - \frac{70x}{100}}{\frac{70x}{100}} \right) \times 100$$

$$= \frac{10x}{76x} \times 100 = \frac{100}{7} = 14.28\%$$

13. (b) Let the total number of votes enrolled be  $x$ . Then,  
 Number of votes cast = 75% of  $x$ . Valid votes = 98% of  
 (75% of  $x$ ).  
 $\therefore 75\% \text{ of } [98\% \text{ of } (75\% \text{ of } x)] = 9261$
- $$\Rightarrow \left( \frac{75}{100} \times \frac{98}{100} \times \frac{75}{100} \times x \right) = 9261$$
- $$\Rightarrow x = \left( \frac{9261 \times 100 \times 100 \times 100}{75 \times 98 \times 75} \right) = 16800.$$
14. (d) Height climbed in second hour  
 $= 12 \frac{1}{2}\% \text{ of } \left( 100 - 62 \frac{1}{2}\% \text{ of } 192 \text{ m} \right)$   
 $= \left( \frac{25}{2} \times \frac{1}{100} \times \frac{75}{2} \times \frac{1}{100} \times 192 \right) \text{ m} = 9 \text{ m.}$
15. (b) Let the original number be 100.  
 Then, the new number =  $100 \times 1.1 \times 0.9 = 99$   
 i.e. the number decreases by 1%.
16. (c) Work with option,  $\left( \frac{5}{4} \right) x - \left( \frac{7}{10} \right) x = 22$   
 Only  $x = 40$  fulfil the above equation.
17. (c) Let the total sales be ₹  $x$ . Then,  $5 \frac{1}{2}\% \text{ of } x + \frac{1}{2}\%$   
 of  $(x - 10000) = 1990$
- $$\Leftrightarrow \frac{11}{2} \times \frac{1}{100} \times x + \frac{1}{2} \times \frac{1}{100} \times (x - 10000) = 1990$$
- $$\Leftrightarrow 12x - 10000 = 398000 \Leftrightarrow 12x = 408000$$
- $$\Leftrightarrow x = 34000$$
18. (a) Let the number be  $x$ ,  
 Then,  $\frac{12}{100} \times \frac{75}{100} \times x - \frac{5}{100} \times x = 75$   
 $\Rightarrow \frac{9x}{100} - \frac{5x}{100} = 75 \Rightarrow \frac{4x}{100} = 75$   
 $\Rightarrow x = \frac{75 \times 100}{4} = 1875$
19. (a)  $\because$  Amount he have spent in 1 month on clothes  
 transport = Amount spent on saving per month  
 $\therefore$  Amount spent on clothes and transport  
 $= \frac{48456}{12} = ₹ 4038$
20. (a) Let the population of males =  $x$ ; then the population of  
 females =  $9000 - x$   
 Now, 5% of  $x + 8\% \text{ of } (9000 - x)$   
 $= (9600 - 9000) = 600$   
 or  $0.05x + 720 - 0.08x = 600$   
 or  $720 - 600 = 0.08x - 0.05x$   
 or,  $120 = 0.03x$   
 $\therefore x = 4000$
21. (d) Let salary of Saroj be ₹  $x$ .  
 $\therefore$  Salary of Raju =  $\frac{80}{100}x$   
 Salary of Ram =  $\frac{70}{100}x$   
 $\text{Required percentage} = \left( \frac{\frac{80x}{100} - \frac{70x}{100}}{\frac{70x}{100}} \right) \times 100$   
 $= \frac{10x}{76x} \times 100 = \frac{100}{7} = 14.28\%$
22. (d) Let the family consumes 1 kg wheat  
 To keep expenditure at Rs. 24, its new consumption  
 should be  $\frac{24}{27} = \frac{8}{9}$  kg  
 $\therefore$  Percentage decrease in consumption  
 $= \frac{\left( 1 - \frac{8}{9} \right)}{1} \times 100 = 11.1\%$
- Alternative method :**  
 $\text{Required \%} = \frac{27 - 24}{27} \times 100 = 11.1\%$
23. (d) Let the first man's output be  $x$ .  
 Then,  $33 \frac{1}{3}\% \text{ of } x = 50\% \text{ of } 1500 \Leftrightarrow \left( \frac{100}{3} \times \frac{1}{100} \times x \right)$   
 $= 750 \Leftrightarrow x = 750 \times 3 = 2250.$
24. (b) Solve using options. 2/25 fits the requirement.
25. (c)  $10 \times 100 = 1000$ , 100 = no. of visitors  
 Now,  $7.5 \times \text{No. of visitors} = 1200$   
 No. of visitors = 160  
 $\text{Increase \%} = \frac{160 - 100}{100} \times 100 = 60\%$
26. (c) Let the inspector examined  $x$  metres,  
 then 0.08% of  $x = 2$   
 $\Rightarrow \frac{x \times 0.08}{100} = 2$   
 or  $x = \frac{200}{0.08} = 2500$  metres
27. (d) Let the original fraction be  $\frac{x}{y}$

## 90 • Percentages

- Then,  $\frac{115\% \text{ of } x}{92\% \text{ of } y} = \frac{15}{16} \Rightarrow \frac{115x}{92y} = \frac{15}{16}$
- $$\Rightarrow \frac{x}{y} = \left( \frac{15}{16} \times \frac{92}{115} \right) = \frac{3}{4}$$
28. (d) Let the class has 100 students.  
 $\Rightarrow$  Number of girls = 35 and number of boys = 65.  
 Since total number of present students = 70 and  
 number of girls present = 80% of 35 = 28, so number of  
 boys present =  $70 - 28 = 42$ .  
 $\Rightarrow$  Required fraction = 42/65.
29. (b) Let 100 units be B's income and  $X$  units be B's  
 expenditure  
 $\Rightarrow A$ 's income = 60 units.  
 $A$ 's expenditure =  $70X/100$  units.  
 But  $60 = 75/100 \times X \Rightarrow X = 80$ .  
 $\therefore B$ 's saving =  $(100 - 80)$  units = 20 units.
33. (d) Weight of water in the mixture of 60 g water  
 $= 60 \times \frac{75}{100} = 45\text{g}$   
 weight of water in the mixture of 45 g water  
 $= 45 + 15 = 60\text{g}$   
 $\therefore$  Percentage of water =  $\frac{60 \times 100}{75} = 80\%$
34. (a) Servant's commission amount  
 $= 6000 - 1500 = ₹ 4500$   
 i.e.,  $15\% = 4500$   
 or,  $100\% = \frac{4500}{15} \times 100 = ₹ 30000$
35. (d) Let the total number of children =  $x$   
 Then,  $\frac{720}{x} = 20\% \text{ of } x = \frac{20}{100} \times \frac{x}{x}$   
 $\Rightarrow x^2 = 720 \times 5 = 3600$   
 $\Rightarrow x = 60$

$$\text{Then, } \frac{115\% \text{ of } x}{92\% \text{ of } y} = \frac{15}{16} \Rightarrow \frac{115x}{92y} = \frac{15}{16}$$

$$\Rightarrow \frac{x}{y} = \left( \frac{15}{16} \times \frac{92}{115} \right) = \frac{3}{4}$$

28. (d) Let the class has 100 students.

$\Rightarrow$  Number of girls = 35 and number of boys = 65.

Since total number of present students = 70 and number of girls present = 80% of 35 = 28, so number of boys present =  $70 - 28 = 42$ .

$\Rightarrow$  Required fraction = 42/65.

29. (b) Let 100 units be B's income and X units be B's expenditure

$\Rightarrow$  A's income = 60 units.

A's expenditure =  $70X/100$  units.

But  $60 = 75/100 \times X \Rightarrow X = 80$ .

i.e., B's saving =  $(100 - 80)$  units = 20 units.

$$\text{Hence A's saving} = 60 - \frac{70}{100} \times 80 = 4 \text{ units.}$$

i.e., A's saving : B's saving = 4 : 20 = 1 : 5.

30. (a) Decrease in production is only due to decrease in manpower. Hence, manpower is decreased by 25% Now, suppose that to restore the same production, working hours are increased by  $x\%$

$$\begin{aligned} \text{Production} &= \text{Manpower} \times \text{Working hours} \\ &= M \times W \text{ (say)} \end{aligned}$$

$$\text{Now, } M \times W = (M - 25\% \text{ of } M) \times (W + x\% \text{ of } W)$$

$$\text{or, } M \times W = \frac{75}{100} M \times \frac{100+x}{100} W$$

$$\text{or, } 100 \times 100 = 75 (100 + x)$$

$$\text{or, } \frac{400}{3} = 100 + x \quad \therefore x = \frac{100}{3} = 33\frac{1}{3}\%$$

31. (b) Let original number = 100

New number = 120% of 120% of 100

$$= \left( \frac{120}{100} \times \frac{120}{100} \times 100 \right) = 144.$$

Decrease on 144 = 44. Decrease on 100

$$= \left( \frac{44}{144} \times 100 \right)\% = 30\frac{5}{9}\%$$

32. (d) Number of ticketless travellers in April

$$= 4000 \times \left( 1 + \frac{5}{100} \right) \left( 1 - \frac{5}{100} \right) \left( 1 - \frac{10}{100} \right)$$

$$= \left( 4000 \times \frac{21}{20} \times \frac{19}{20} \times \frac{9}{10} \right) = 3591.$$

33. (d) Weight of water in the mixture of 60 g water

$$= 60 \times \frac{75}{100} = 45\text{g}$$

weight of water in the mixture of 45 g water

$$= 45 + 15 = 60\text{g}$$

$$\therefore \text{Percentage of water} = \frac{60 \times 100}{75} = 80\%$$

34. (a) Servant's commission amount

$$= 6000 - 1500 = ₹ 4500$$

$$\text{i.e., } 15\% = 4500$$

$$\text{or, } 100\% = \frac{4500}{15} \times 100 = ₹ 30000$$

35. (d) Let the total number of children =  $x$

$$\text{Then, } \frac{720}{x} = 20\% \text{ of } x = \frac{20}{100} \times x = \frac{x}{5}$$

$$\Rightarrow x^2 = 720 \times 5 = 3600$$

$$\Rightarrow x = 60$$

$$\therefore \text{Each child receive} = \frac{720}{60} = 12 \text{ sweets}$$

36. (a) Suppose price of the printer =  $P$

$$\therefore \text{Price of a computer} = 3P$$

$$\text{Total cost of 60 computers} = 180P$$

$$\text{Total cost of 20 printers} = 20P$$

$$\therefore \text{Total cost of the purchase} = 200P$$

Thus total cost of the printers is 10% of the total cost.

37. (d) Population after 2000 = 3244800

$$\text{Population after 2001} = 2985216$$

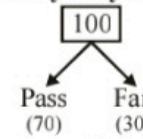
$$\text{Population at the end of 2003} = 3228810$$

38. (e) Non-defective products

$$\frac{25 \times 0.98 + 35 \times 0.96 + 40 \times 0.95}{100} \times 100 = 96.1\%$$

39. (a) On ₹ 100 he saves ₹ 6. On 115 he still saves ₹ 6. percentage increase of 15 on 94 = 15.95%

40. (e) Half yearly exam



Annual exam

$$\frac{70 \times 0.6}{42} + \frac{30 \times 0.8}{24}$$

$\therefore$  Total pass in annual exam = 42 + 24 = 66

41. (a) Solution = 100 ml and Alcohol = 40 ml

For first vessel

$$\frac{40+x}{100+x} = \frac{1}{2},$$

$$\text{so, } x = 20\text{ml}$$

For second vessel

$$\frac{40 + \frac{3}{5}y}{100 + \frac{2}{5}y} = \frac{1}{2},$$

so,  $y = 25\text{ml}$

$$\text{Required percentage} = \frac{5}{25} \times 100 = 20\%$$

42. (d) Total land of Sukhiya =  $\frac{480x}{0.6} = 800x$

$\therefore$  Cultivated land of village =  $384000x$

$$\therefore \text{Required percentage} = \frac{800x}{384000} \times 100 = 0.20833.$$

43. (b) Total votes = 6000. Valid votes = 75% of 6000 = 4500. Bhiku gets 65% of 4500 votes and Mhatre gets 35% of 4500. Hence, Mhatre gets:  $0.35 \times 4500 = 1575$  votes.

44. (b) Solve using options. Checking for option (b), gives us:

$200000 \rightarrow 180000 \rightarrow 171000 \rightarrow 153900 \rightarrow 146205$   
(by consecutively decreasing 200000 by 10% and 5% alternately)

45. (a) Solve through trial and error using the options. 12% (option (a)) is the only value that fits the situation.

46. (d) Salary of Dheeraj = ₹ 100

Salary of Anil = ₹ 80

Salary of Vinit = ₹ 70

$$\text{Required percent} = \frac{10}{70} \times 100 = 14.28\%$$

47. (d) Let population = 100

At least 50 people read a newspaper

At most 12.5 people read more than a newspaper

Hence, at least 37.5 people read only one newspaper.

48. (a) Let monthly income be  $y$

Let money spent on grocery, clothes and education be  $4x, 2x, 5x$

Money spent of clothes = ₹ 5540 =  $2x$

$$x = 2770$$

$$\text{Now } 4x + 2x + 5x = 11x = 11 \times 2770$$

$$= 30470 = 55\% \text{ of } y$$

$$y = \frac{30470 \times 100}{55}$$

$$y = ₹ 55,400$$

49. (e) Let the two number be  $x$  and  $y$ .

$$35\% x = 2 \times 75\% y$$

$$35\% x = 150\% y$$

$$\frac{35}{100} \times x = \frac{150}{100} \times y$$

$$35x = 150y$$

$$\frac{x}{y} = \frac{150}{35} = \frac{30}{7}, x:y = 30:7$$

50. (a) No. of boys, last year = 610

$$20\% \text{ of } 610 = 122$$

No. of boys, current year =  $610 - 122 = 488$

No. of girls = 175% of 488

$$= \frac{175 \times 488}{100} = 854 \text{ girls}$$

51. (c) Let maximum marks of test =  $x$

$$\text{Vidya marks} = 350 + 296 = 646 = 76\% \text{ of } x$$

$$x = \frac{646 \times 100}{76} = 850$$

52. (e) Let initial marks of student =  $x$

After Re-evaluation marks reduced by 40% of  $x$

New score = 60% of  $x = 96$

$$= \frac{60}{100} \times x = 96$$

$$x = \frac{96 \times 100}{60}$$

$$x = 160$$

Marks lose =  $160 - 96 = 64$ .

53. (e) No. of candidates selected for job = 20% of 855

$$= \frac{20 \times 855}{100} = 171$$

54. (d) Total cost price =  $200 \times 10 = ₹ 2000$

Total selling price =  $12 \times 195 = ₹ 2340$

$$\therefore \text{Profit per cent} = \frac{2340 - 2000}{2000} \times 100 = 17\%$$

55. (a) Saving percentage =  $(100 - 55)\% = 45\%$

If the income of Ajay be ₹  $x$ , then,

$$\frac{45 \times x}{100} = 27000$$

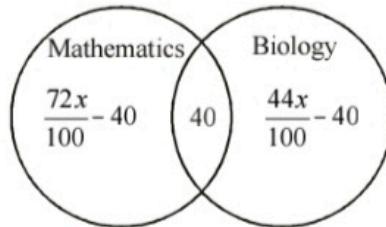
$$\Rightarrow x = \frac{27000 \times 100}{45} = ₹ 60000$$

56. (c) Salary in May 2000 = ₹ 15000

Salary in July 2000  $\Rightarrow 15000 + 10\% \text{ of } 15000 = ₹ 16500$

Salary in October 2001 =  $16500 + 10\% \text{ of } 16500 = ₹ 18150$

57. (c) Let the total number of students in the class be  $x$ .



$$\therefore \frac{72x}{100} - 40 + 40 + \frac{44x}{100} - 40 = x$$

$$\Rightarrow \frac{72x}{100} x + \frac{44x}{100} - x = 40$$

$$\Rightarrow \frac{16x}{100} = 40 \Rightarrow x = \frac{40 \times 100}{16}$$

$$\Rightarrow x = 250$$

58. (c) If the number of trees in the garden be  $x$ , then

$$x \times \frac{60}{100} \times \frac{25}{100} \times \frac{20}{100} = 1500$$

$$\Rightarrow x \times \frac{3}{5} \times \frac{1}{4} \times \frac{1}{5} = 1500$$

$$\Rightarrow x = \frac{1500 \times 5 \times 4 \times 5}{3} = 50000$$

$$59. (b) \frac{P-Q}{2} = (P+Q) \times \frac{30}{100}$$

$$\Rightarrow 5(P-Q) = (P+Q) \times 3$$

$$\Rightarrow 5P - 3P = 5Q + 3Q$$

$$\Rightarrow 2P = 8Q \Rightarrow P = 4Q$$

$$Q = \frac{x}{100} \times P$$

$$Q = \frac{x}{100} \times 4Q$$

$$\Rightarrow \frac{4x}{100} \Rightarrow x = 25$$

60. (d) Let the total number of students be  $x$ .

Let A and B represent the sets of students who passed in English and Mathematics respectively.

Then, number of students passed in one or both the subjects

$$= n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$= 75\% \text{ of } x + 60\% \text{ of } x - (x - 25\% \text{ of } x)$$

$$= \frac{3}{4}x + \frac{3}{5}x - \frac{3}{4}x = \frac{3}{5}x$$

$$\text{So, } \frac{3}{5}x = 240$$

$$x = \frac{240 \times 5}{3} = 400$$

$$61. (b) \frac{40}{100} \times \frac{4}{5} \times \frac{3}{4} \times x = 48$$

$$\frac{6}{25}x = 48$$

$$x = \frac{48 \times 25}{6} = 200$$

1% of 200 is 2.

62. (d) % of votes secured by second candidate  
=(100 - 57) = 43%

Let total votes polled be  $x$ .

According to question,

$$(57 - 43)\% \text{ of } x = 42000$$

$$14\% \text{ of } x = 42000 \Rightarrow x = 3,00,000$$

63. (e) Let the number is  $x$ .

According to question

$$x - 10\% \text{ of } x = 30$$

$$x - \frac{10}{100}x = 30$$

$$\left( \frac{100-10}{100} \right) x = 30$$

$$x = \frac{30 \times 100}{90} = 33\frac{1}{3}$$

Hence, the number is  $33\frac{1}{3}$

64. (c) Required percentage =  $\frac{24}{40} \times 100 = 60\%$

$$65. (a) \frac{125}{100} \times x = 100$$

$$\Rightarrow x = \frac{100 \times 100}{125} = 80$$

66. (b) Marks of Supriyo =  $x$  marks

According to question

Mahuya marks = Supriyo marks - 10% of Supriyo marks

$$81 = x - 10\% \text{ of } x \Rightarrow x \left( 1 - \frac{10}{100} \right)$$

$$81 = \frac{9}{10}x \Rightarrow \frac{810}{9} = x$$

$\therefore x = 90$  marks

67. (a)  $R = S + 0.2S = 1.2S$

$$\left( \frac{R-S}{R} \right) \times 100 = \left( 1 - \frac{S}{R} \right) \times 100$$

$$= \left( 1 - \frac{1}{1.2} \right) \times 100$$

$$= \frac{100}{6} = \frac{50}{3} = 16\frac{2}{3}$$

68. (a)  $\frac{1}{100} \times \frac{1}{100} \times \frac{25}{100} \times 1000 = 0.025$

**Level-II**

1. (b) We have 5.5% of 100000  
= Rent – 12.5% of Rent – 325.

$$\Rightarrow \frac{5500}{12} = \text{Rent} - \frac{\text{Rent}}{8} - \frac{325}{12}$$

$$\Rightarrow \frac{5500}{12} + \frac{325}{12} = \frac{7}{8} \times \text{Rent}$$

$$\Rightarrow \text{Rent} = \frac{5500}{12} \times \frac{8}{7} = ₹ 554.76 \text{ per month.}$$

2. (c) **First expenditure:** Suppose 100 litres of petroleum at 100 units of money per litre, then total expenditure =  $100 \times 100$  units of money = 10000 units of money.  
**Second expenditure:** Now 80 litres of petroleum at 140 units of money per litre, total expenditure =  $80 \times 140$  units of money = 11200 units.

$\Rightarrow$  Expenditure increases by

$$\frac{11200 - 10000}{10000} \times 100 = 12\%$$

**Short-cut:**  $\text{Exp}_1 = \text{P}X$ ,  $\text{Exp}_2 = 1.4P(0.8X) = 1.12PX$ .  
 $\Rightarrow$  Directly we see, answer = 12%.

3. (a) A's marks =  $300 \times \frac{3}{100} = 90$ .

$$\text{B's marks} = 100 \times (1 + 40/100) = 140.$$

$\Rightarrow$  C is ahead of B by  $2/9$  of his own marks i.e.

$$7/9 \text{ of C's marks} = 140$$

$$\Rightarrow \text{C's marks} = 140 \times 9/7 = 180.$$

4. (d) Migrants = 35% of 728400 =  $\left(\frac{35x}{100} \times 728400\right)$   
 $= 254940$ .  
Local population =  $(728400 - 254940) = 473460$   
Rural population = 20% of 473460 = 94692.  
Urban population =  $(254940 - 94692) = 160248$ .  
 $\therefore$  Female population = 48% of 473460 + 30% of 94692 + 40% of 160248

$$= \left(\frac{48}{100} \times 473460 + \frac{30}{100} \times 94692 + \frac{40}{100} \times 160248\right)$$

$$= 227260.8 + 28407.6 + 64099.2 = 896660.$$

5. (b) Let Madan's income be ₹ x.  
Then, Net income =  $(100 - 10)\%$  of ₹ x

$$= 90\% \text{ of } ₹ x = ₹ \frac{9x}{10}$$

New net income = 85% of 110% of ₹ x

$$= ₹ \left(\frac{85}{100} \times \frac{110}{100} \times x\right) = ₹ \frac{187}{200} x$$

$$\therefore \frac{187x}{200} - \frac{9x}{10} = 350 \Rightarrow \frac{7x}{200} = 350$$

$$\Rightarrow x = \left(\frac{350 \times 200}{7}\right) = 10000.$$

6. (d) Working with options, we have

	Original number	New number	Difference
(a)	22	34	12
(b)	63	96	33
(c)	24	38	14

Obviously, (d) is the correct option.

7. (d) Let he had originally ₹ x. Then  
65% of x + 20% of x + 1305 = x  
 $0.65x + 0.2x + 1305 = x$   
 $\Rightarrow 0.15x = 1305 \Rightarrow x = ₹ 8700$   
 $\therefore$  His total investment = 65% of 8700 + 20% of 8700 = 85% of 8700 = ₹ 7395

8. (c) Let original consumption be 1 unit costing ₹ 100  
New cost = ₹ 125. New consumption

$$= \left(\frac{1}{125} \times 100\right) = \frac{4}{5} \text{ unit.}$$

$$\therefore \frac{\text{Reduction in consumption}}{\text{Original consumption}} = \frac{\left(1 - \frac{4}{5}\right)}{1} = \frac{1}{5}$$

i.e., 1 : 5.

9. (c) After first year, the value of the scooter = ₹ 20,000  
After second year, the value of scooter = ₹ 16,000  
After third year, the value of scooter = ₹ 12,800

10. (b) Let original consumption = 100 kg  
and new consumption = x kg  
So,  $100 \times 6 = x \times 7.50 \Leftrightarrow x = 80 \text{ kg}$   
 $\therefore$  Reduction in consumption = 20%

11. (a) Let the numbers be x and y. Then,

$$x + y = \frac{28}{25}x \Rightarrow y = \frac{28}{25}x - x \Rightarrow y = \frac{3}{25}x$$

$$\Rightarrow \frac{y}{x} = \left(\frac{3}{25} \times 100\right)\% = 12\%$$

12. (b) Let the number be x. Then,

$$\% \text{ error} = \frac{6x - x/6}{6x} \times 100 = \frac{35}{36} \times 100 = 97.2\%$$

13. (c)  $p = 6q$ . So, q is less than p by  $5q$ .

$$\therefore \text{Required percentage} = \left(\frac{5q}{p} \times 100\right)\%$$

$$= \left(\frac{5q}{6q} \times 100\right)\% = 83\frac{1}{3}\%$$

14. (c)  $\frac{5}{100}A = \frac{15}{100}B$  and  $\frac{10}{100}B = \frac{20}{100}C \Rightarrow A = 3B$  and  $B = 2C = 2 \times 2000 = 4000$ .  
 $\therefore A = 3 \times 4000 = 12000$ .

Hence,  $A + B + C = (12000 + 4000 + 2000) = 18000$ .

15. (d) Let original price be ₹  $x$  per orange. Then,  
Reduced rate  $= (1 - 0.2)x = ₹ 0.8x$

$$\therefore \frac{2.50}{0.8x} - \frac{2.50}{x} = 5$$

$$\Rightarrow \frac{25}{8x} - \frac{2.5}{x} = 5 \Rightarrow x = \frac{1}{8}$$

$\therefore$  Original price of oranges per dozen  $\frac{1}{8} \times 12 = ₹ 1.5$

and Reduced price  $= ₹ (0.8)(1.5) = ₹ 1.2$

16. (d) Let the total no. of parts produced at initial stage be 100. Then after three successive percentage rejections of 10%, 5% and 2%, we have  
 $100 \times 0.9 \times 0.95 \times 0.98 = 83.79$   
Therefore, a single effective rejection  
 $= 100 - 83.79 = 16.21$

17. (a) Let the original quantity be  $x$  kg. Vanaspati ghee in

$$x \text{ kg} = \left( \frac{40}{100}x \right) \text{ kg} = \left( \frac{2x}{5} \right) \text{ kg.}$$

$$\text{Now, } \frac{\frac{2x}{5}}{x+10} = \frac{20}{100} \Leftrightarrow \frac{2x}{5x+50} = \frac{1}{5} \Leftrightarrow 5x = 50 \\ \Leftrightarrow x = 10$$

18. (a) Let the strength of school was  $x$  in 1998  
 $\therefore$  strength in 2001 will be

$$= x \frac{110}{100} \times \frac{90}{100} \times \frac{110}{100} \times \frac{90}{100} \times \frac{110}{100} = 1.07811x$$

$\therefore$  increment  $= 1.07811x - x = 0.07811x$

$\therefore$  % increase  $= 7.811 \approx 8\%$

19. (d) The given information gives no indication regarding the comparison of  $x$  and  $y$ .  
20. (d) Since the weightage of eighth examination is not known, hence can not be determined.  
21. (c) Let the original price per egg be ₹  $x$ . Then, increased

$$\text{price} = ₹ \left( \frac{130}{100}x \right)$$

$$\therefore \frac{7.80}{x} - \frac{7.80}{\frac{130}{100}x} = 3 \Leftrightarrow \frac{7.80}{x} - \frac{7.80}{130x} = 3$$

$$\Leftrightarrow 1014 - 780 = 3 \times 130x \Leftrightarrow 390x = 234$$

$$\Leftrightarrow x = 0.6$$

So, present price per dozen  $= ₹ \left( 12 \times \frac{130}{100} \times 0.6 \right) = ₹ 9.36$ .

22. (a) Let the truth spoken by  $A$  and  $B$  be  $p_1$  and  $p_2$

$$\text{respectively, i.e., } p_1 = \frac{3}{4} \text{ and } p_2 = \frac{4}{5}$$

They will contradict each other only when one speaks truth and the other is lying.

$$\text{i.e., } \frac{3}{4} \times \frac{1}{5} + \frac{4}{5} \times \frac{1}{4} = \frac{3}{20} + \frac{4}{20} = \frac{7}{20} = \frac{35}{100} \text{ i.e., } 35\%$$

23. (b) Let B's Income = ₹  $x$

$$A's \text{ Income} = ₹ \frac{3}{5}x$$

And B's expenditure = ₹  $y$

$$A's \text{ expenditure} = ₹ \frac{7}{10}y$$

$$\text{Also, } \frac{3}{5}x = \frac{3}{4} \cdot \frac{7}{10}y$$

$$\frac{A's \text{ savings}}{B's \text{ savings}} = \frac{x-y}{\frac{3}{5}x - \frac{7}{10}y} = \frac{\frac{7}{8}y - y}{\frac{3}{5}\cdot\frac{7}{8}y - \frac{7}{10}y} = \frac{-y/8}{\frac{21y}{40} - \frac{7}{10}y}$$

$$= \frac{5}{25} \approx 1:5$$

24. (b) Percentage of uncertain individuals

$$= [100 - (20 + 60)] \% = 20\%$$

$\therefore 60\% \text{ of } x - 20\% \text{ of } x = 720 \Leftrightarrow 40\% \text{ of } x = 720$

$$\Leftrightarrow \frac{40}{100}x = 720 \Leftrightarrow x = \left( \frac{720 \times 100}{40} \right) = 1800.$$

25. (d) Suppose Income of  $B$  = ₹  $x$

$$\text{Income of } A = \frac{150}{100} \times x = ₹ \frac{3x}{2}$$

$$\text{Income of } C = \frac{120}{100} \times \frac{3x}{2}$$

$$\frac{6}{5} \times \frac{3x}{2} = \frac{9x}{5}$$

$$\therefore x + \frac{3x}{2} + \frac{9x}{5} = 86000$$

$$\frac{10x + 15x + 18x}{10} = 86000$$

$$43x = 86000$$

$$x = 20000$$

$$\text{So, income of } C = \frac{9}{5} \times 20000 = ₹ 36000$$

26. (e) Number of males = 60% of 1000 = 600.

Number of females =  $(1000 - 600) = 400$ .

Number of literates = 25% of 1000 = 250.

Number of literate males = 20% of 600 = 120

Number of literate females =  $(250 - 120) = 130$

$$\therefore \text{Required percentage} = \left( \frac{130}{400} \times 100 \right) \% = 32.5\%$$

27. (d)  $B + 60\% \text{ of } A = 175\% \text{ of } B \rightarrow 60\% \text{ of } A = 75\% \text{ of } B.$   
i.e.  $0.6A = 0.75B$   
 $A/B = 5/4$

Apparently it seems that A is bigger, but if you consider A and B to be negative the opposite would be true.

Hence, option (d) is correct

28. (d) Number of ticketless travellers in April

$$\begin{aligned} &= 4000 \times \left(1 + \frac{5}{100}\right) \left(1 - \frac{5}{100}\right) \left(1 - \frac{10}{100}\right) \\ &= \left(4000 \times \frac{21}{20} \times \frac{19}{20} \times \frac{9}{10}\right) = 3591. \end{aligned}$$

29. (d) October : November : December = 9 : 8 : 10.666  
since, he got ₹40 more in December than October, we can conclude that  $1.666 = 40 \rightarrow 1 = 24$ .  
Thus, total Bonus for the three months is:  
 $0.4 \times 27.666 \times 24 = 265.6$

30. (b) The total wealth given would be  $50\% + 25\%$  (which is got by  $50\%$  of the remaining  $50\%$ ) +  $12.5\%$  (which is got by  $50\%$  of the remaining  $25\%$ ). Thus, the total wealth given by him would be equivalent to  $87.5\%$  of the total. Since, this is equal to 130900 kilograms of gold, the total gold would be:  
 $130900 \times 8/7 = 149600$ .

31. (c)  $\frac{378}{125} = 3 + \frac{3}{125} = 302.4\%$

Let original salary be ₹ 100

And now going through option, we get (c) as answer.

32. (d) Out of a total of 100% votes; 80% voted. 16% were invalid and 20% went to the second placed candidate. This means that the maximum the winner can get is 44%. Options a, b and c are greater than 44% and hence cannot be correct. Hence, none of these.

33. (d) Rajesh's scores in each area is 65 and 82 respectively out of 100 each. Since, the exam is of a total of 250 marks ( $100 + 100 + 50$ ) he needs a total of 195 marks in order to get his target of 78% overall. Thus, he should score  $195 - 65 - 82 = 195 - 147 = 48$  marks in Sociology which would mean 96%

34. (d) The only values that fit this situation are C 25%, B 30%, and A 45%. These are the percentage of votes polled. (Note: these values can be got either through trial and error or through solving  $c + c + 5 + 1.5(c + 5) = 100\%$ )

Then, 20% is 18000 (the difference between A & C.)  
Hence, 90000 people must have voted and 100000 people must have been on the voter's list.

35. (a) Let the number be N. Then, 5N should be the correct outcome. But instead the value got is  $0.2N$ . Change in value =  $5N - 0.2N = 4.8N$ . The percentage change in the value =  $4.8N \times 100/5N = 96\%$

36. (e)  $100 \rightarrow 150 \rightarrow 75 \text{ (yr. 1)} \rightarrow 112.5 \rightarrow 56.25 \text{ (yr. 2)}$   
 $\rightarrow 84.375 \rightarrow 42.1875$

Now,  $42.1875 = ₹ 16,875$

Hence,  $1 \rightarrow 400$

Also year 2 donation is  $56.25 \times 400 = 22500$

37. (e) Total characters in her report =  $25 \times 60 \times 75$   
Let the new no. of pages be  $n$

Then:  $n \times 55 \times 90 = 25 \times 60 \times 75$

$$n = 22.72$$

This means that her report would require 23 pages. A drop of 8% in terms of the pages.

38. (c) No. of males =  $\frac{11}{18} \times 7200 = 4400$

$$\text{No. of males married} = \frac{40}{100} \times 4400 = 1760$$

No. of females married = 1760

$$\text{Required percentage} = \frac{1760}{2800} \times 100 = 62\frac{6}{7}\%$$

39. (b) Let the equation be

$$x^2 - 2x + 1 = 0 \quad \dots(1)$$

$$\text{and } x^2 - x - 2 = 0 \quad \dots(2)$$

$$\text{Required percentage} = \frac{1 - (-2)}{1} \times 100 = 300\%$$

40. (d)  $\frac{5x}{100} + 600 = 1000 + \frac{5}{200}(x - 4000)$

$$\frac{5x}{100} - \frac{5x}{200} = 300$$

$$5x = 200 \times 300$$

$$\Rightarrow x = 12000$$

41. (e) According to question

Third number = 2400

$$\therefore \text{Second number} = 2400 \times \frac{1}{4} = 600$$

Again,

$$\text{First number} \times \frac{6}{11} = \text{Second number} \times \frac{22}{100}$$

$$\therefore \text{First number} = 600 \times \frac{22}{100} \times \frac{11}{6} = 242$$

$$\therefore 45\% \text{ of the first number} = 242 \times \frac{45}{100} = 108.9$$

42. (d) Required number =  $4800 \times \frac{45}{100} \times \frac{40}{100} = 864$

32. (d) Out of a total of 100% votes; 80% voted. 16% were invalid and 20% went to the second placed candidate. This means that the maximum the winner can get is 44%. Options a, b and c are greater than 44% and hence cannot be correct. Hence, none of these.
33. (d) Rajesh's scores in each area is 65 and 82 respectively out of 100 each. Since, the exam is of a total of 250 marks ( $100 + 100 + 50$ ) he needs a total of 195 marks in order to get his target of 78% overall. Thus, he should score  $195 - 65 - 82 = 195 - 147 = 48$  marks in Sociology which would mean 96%.
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Then, 20% is 18000 (the difference between A & C.) Hence, 90000 people must have voted and 100000 people must have been on the voter's list.

$\Rightarrow x = 12000$

41. (e) According to question  
Third number = 2400  
 $\therefore$  Second number =  $2400 \times \frac{1}{4} = 600$   
Again,  
 $\text{First number} \times \frac{6}{11} = \text{Second number} \times \frac{22}{100}$   
 $\therefore \text{First number} = 600 \times \frac{22}{100} \times \frac{11}{6} = 242$   
 $\therefore 45\% \text{ of the first number} = 242 \times \frac{45}{100} = 108.9$

42. (d) Required number =  $4800 \times \frac{45}{100} \times \frac{40}{100} = 864$

## 96 ● Percentages

43. (c) Suppose the maximum mark of the test be  $x$ .

$$\text{Then, } \frac{468 \times 100}{x} = \frac{336 \times 100}{700}$$

$$\therefore x = \frac{468 \times 100 \times 700}{336 \times 100} = 975$$

44. (e) Let the numbers are  $x, x+1, x+2$   
sum of three consecutive numbers = 2262  
 $x + x + 1 + x + 2 = 2262$   
 $3x + 3 = 2262$   
 $3x = 2259$   
 $x = 753$   
Number are 753, 754, 755  
 $\therefore 41\% \text{ of } 755 = 309.55$

45. (b) Marks in subject B = 56% of 150 = 84  
Total marks obtained = 54 % of Total marks

$$= \frac{54}{100} \times 450 \quad [\because \text{Maximum marks in each subject is 150}]$$

$$= 243$$

$$\text{Total marks obtained} = A + B + C$$

$$243 = 73 + 84 + X$$

$$X = 86$$

46. (b) Rohan's marks = 75

$$\begin{aligned} \text{Sonia's marks} &= 65 \\ \text{Rohit's marks} &= 65 + 45 = 110 \\ \text{Raman's marks} &= 110 - 25 = 85 \\ \text{Ravi got marks} &= 85 + 34 = 119 \\ \text{Total maximum marks} &= 119 + 50 = 169 \end{aligned}$$

$$\text{Percentage of Ravi's mark} = \frac{119}{169} \times 100\% = 70.4\% = 70\%$$

47. (b) Let total monthly income of Mr. Giridhar be ₹  $x$ .

According to question,

$$\therefore x \times \frac{50}{100} \times \frac{15}{100} = 900$$

$$x = ₹ 12000$$

Hence, monthly income of Mr. Giridhar = ₹ 12000.

48. (a) Let passing marks be represented by  $p$ .

$$p \times 1.05 = 273$$

$$p = 260$$

$$\text{Lokesh passing \%} = \frac{312 - 260}{260} \times 100 = 20\%$$

49. (a) Let the monthly salary of A be  $x$ , monthly salary of B is  $(40000 - x)$ .

$$\text{Savings of A} = (100 - 85)\% \text{ of } x = 0.15x$$

$$\begin{aligned} \text{Savings of B} &= (100 - 95)\% \text{ of } (40000 - x) \\ &= 0.05(40000 - x) \end{aligned}$$

$$0.15x = 0.05(40000 - x)$$

$$\Rightarrow 0.15x + 0.05x = 40000 \times 0.05$$

$$\Rightarrow 0.2x = 2000$$

$$\Rightarrow x = 10000$$

50. (d) Quantity of salt = 5% of  $6l = 300 \text{ ml}$   
Quantity of water =  $6000 \text{ ml} - 300 \text{ ml} = 5700 \text{ ml}$   
Quantity of water left after evaporation  
 $= (5700 - 100) \text{ ml} = 4700 \text{ ml}$

$$\% \text{ of salt} = \frac{300 \text{ ml}}{(4700 + 300) \text{ ml}} \times 100 = 6\%$$