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A review on dark channel prior based image dehazing algorithms

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Abstract

The presence of haze in the atmosphere degrades the quality of images captured by visible camera sensors. The removal of haze, called dehazing, is typically performed under the physical degradation model, which necessitates a solution of an ill-posed inverse problem. To relieve the difficulty of the inverse problem, a novel prior called dark channel prior (DCP) was recently proposed and has received a great deal of attention. The DCP is derived from the characteristic of natural outdoor images that the intensity value of at least one color channel within a local window is close to zero. Based on the DCP, the dehazing is accomplished through four major steps: atmospheric light estimation, transmission map estimation, transmission map refinement, and image reconstruction. This four-step dehazing process makes it possible to provide a step-by-step approach to the complex solution of the ill-posed inverse problem. This also enables us to shed light on the systematic contributions of recent researches related to the DCP for each step of the dehazing process. Our detailed survey and experimental analysis on DCP-based methods will help readers understand the effectiveness of the individual step of the dehazing process and will facilitate development of advanced dehazing algorithms.

Keywords: Dark channel prior, Dehazing, Image degradation, Image restoration

1 Review

1.1 Introduction

Due to absorption and scattering by atmospheric particles in haze, outdoor images have poor visibility under inclement weather. Poor visibility negatively impacts not only consumer photography but also computer vision applications for outdoor environments, such as object detection [1] and video surveillance [2]. Haze removal, which is referred to as dehazing, is considered an important process because haze-free images are visually pleasing and can significantly improve the performance of computer vision tasks.

Methods presented in earlier studies had required multiple images to perform dehazing. For example, polarization-based methods [3–5] use the polarization property of scattered light to restore the scene depth information from two or more images taken with different degrees of polarization. Similarly, in [6, 7], multiple images of the same scene are captured under different weather conditions to be used as reference images with clear weather

conditions. However, these methods with multiple reference images have limitation in online image dehazing applications [6, 7] and may need a special imaging sensor [1–3]. This leads the researchers to focus the dehazing method with a single reference image. Single image based methods rely on the typical characteristics of haze-free images. Tan [8] proposed a method that takes into account the characteristic that a haze-free image has a higher contrast than a hazy image. By maximizing the local contrast of the input hazy image, it enhances the visibility but introduces blocking artifacts around depth discontinuities. Fattal [9] proposed a method that infers the medium transmission by estimating the albedo of the scene. The underlying assumption is that the transmission and surface shading are locally uncorrected, which does not hold under a dense haze.

Observing the property of haze-free outdoor images, He [10] proposed a novel prior—*dark channel prior* (DCP). The DCP is based on the property of “dark pixels,” which have a very low intensity in at least one color channel, except for the sky region. Owing to its effectiveness in dehazing, the majority of recent dehazing techniques [10–36] have adopted the DCP. The DCP-based dehazing techniques are composed of four major steps: atmospheric

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light estimation, transmission map estimation, transmission map refinement, and image reconstruction. In this paper, we perform an in-depth analysis of the DCP-based methods in the four-step point of view.

We note that there are several review papers on image dehazing or defogging [37–42]. In [37], five physical model-based dehazing algorithms are compared. In [38, 39], several enhancement-based and restoration-based defogging methods are investigated. In [40], fog removal algorithms that use depth and prior information are analyzed. In [41], a comparative study on the four representative dehazing methods [4, 9, 10, 43] are performed. In [42], many visibility enhancement techniques developed for homogeneous and heterogeneous fog are discussed. To the best of our knowledge, our paper is the first one dedicated to DCP-based methods. This survey is expected to ascertain researchers' endeavors toward improving the original DCP method.

The rest of the paper is organized as follows. In Section 1.2, the original DCP-based dehazing method is first reviewed. Section 1.3 provides an in-depth survey of conventional DCP-based methods. Section 1.4 discusses the performance evaluation methods for image dehazing, and Section 1.5 concludes the paper.

1.2 Dark channel prior based image dehazing

1.2.1 Degradation model

A hazy image formed as shown in Fig. 1 can be mathematically modeled as follows [44, 45]

$$I(x) = J(x)e^{-\beta d(x)} + A(1 - e^{-\beta d(x)}), \quad (1)$$

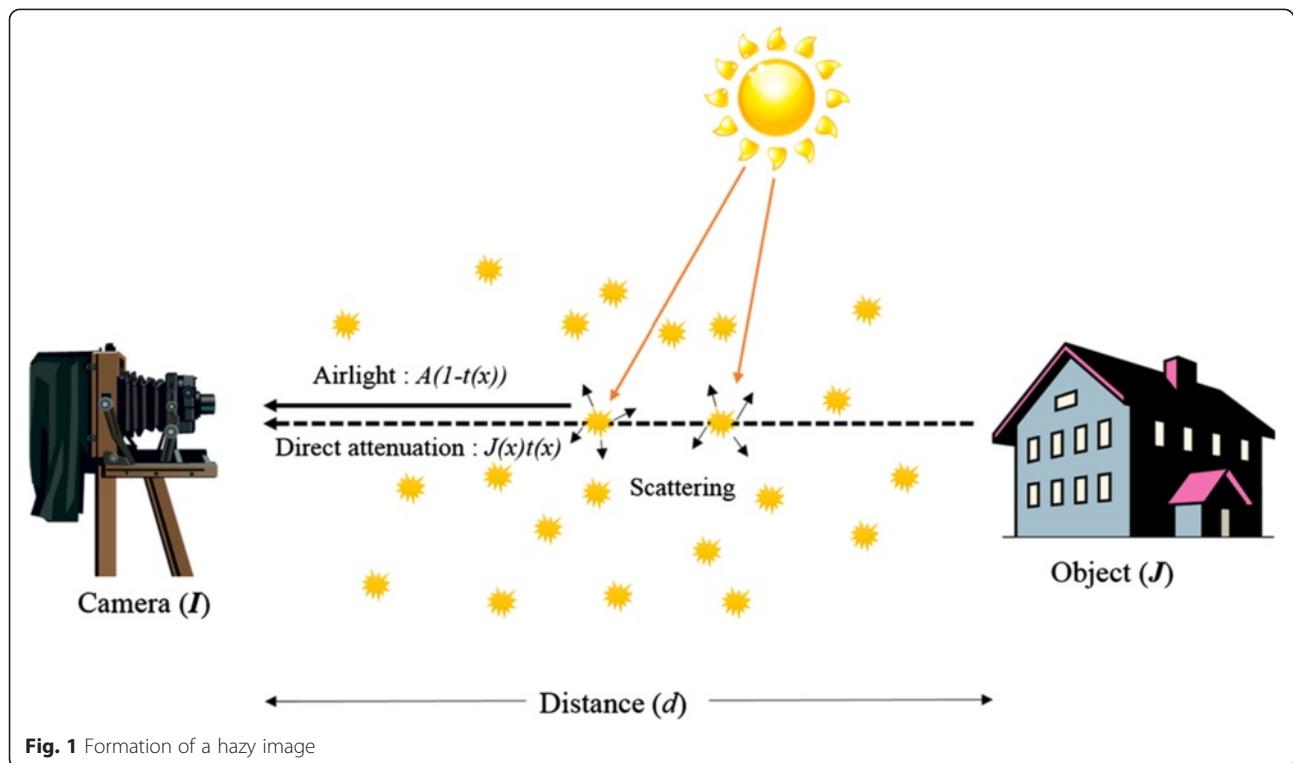
where x represents the image coordinates, I is the observed hazy image, J is the haze-free image, A is the global atmospheric light, β is the scattering coefficient of the atmosphere, and d is the scene depth. Here, $e^{-\beta d}$ is often represented as the transmission map and is given by

$$t(x) = e^{-\beta d(x)}. \quad (2)$$

In clear weather conditions, we have $\beta \approx 0$, and thus $I \approx J$. However, β becomes non-negligible for hazy images. The first term of Eq. (1), $J(x)t(x)$ (*the direct attenuation*), decreases as the scene depth increases. In contrast, the second term of Eq. (1), $A(1 - t(x))$ (*the airlight*), increases as the scene depth increases. Since the goal of image dehazing is to recover J from I , once A and t are estimated from I , J can be arithmetically obtained as

$$J(x) = \frac{I(x) - A}{t(x)} + A. \quad (3)$$

However, the estimation of A and t is non-trivial. In particular, since t varies spatially according to the scene depth, the number of unknowns is equivalent to the number of image pixels. Thus, a direct estimation of t from I is prohibitive without any prior knowledge or assumptions.



1.2.2 Dark channel prior (DCP)

He *et al.* [10] performed an empirical investigation of the characteristic of haze-free outdoor images. They found that there are dark pixels whose intensity values are very close to zero for at least one color channel within an image patch. Based on this observation, a dark channel is defined as follows:

$$J^{\text{dark}}(x) = \min_{y \in \Omega(x)} \left(\min_{c \in \{r, g, b\}} J^c(y) \right), \quad (4)$$

where J^c is an intensity for a color channel $c \in \{r, g, b\}$ of the RGB image and $\Omega(x)$ is a local patch centered at pixel x . According to Eq. (4), the minimum value among the three color channels and all pixels in $\Omega(x)$ is chosen as the dark channel $J^{\text{dark}}(x)$.

From 5000 dark channels of outdoor haze-free images, it was demonstrated that about 75 percent of the pixels in the dark channels have zero values and 90 percent of the pixels have values below 35 when the pixels in the sky region are excluded [10]. The low intensities in the dark channel are due to the following three main features: (i) shadows, e.g., shadows from cars and buildings in an urban scene or shadows from trees, leaves, and rocks in a landscape (Fig. 2a); (ii) colorful objects or surfaces, e.g., red or yellow flowers and leaves (Fig. 2b); and (iii) dark objects or surfaces, e.g., dark tree trunks and stones (Fig. 2c). Based on the above observation, the pixel value at the dark channel can be approximated as follows:

$$J^{\text{dark}} \approx 0. \quad (5)$$



Fig. 2 Dark channels of outdoor images [53], where the size of Ω is 15×15 . The pixel values for the dark channels are close to zero at (a) the shadows of buildings and rocks, (b) colorful flowers and scenes, and (c) tree trunks and stones

This approximation to zero for the pixel value of the dark channel is called the DCP.

On the contrary, the dark channels from hazy images produce pixels that have values far above zero as shown in Fig. 3. Global atmospheric light tends to be achromatic and bright, and a mixture of airlight and direct attenuation significantly increases the minimum value of the three color channels in the local patch. This implies that the pixel values of the dark channel can serve as an important clue to estimate the haze density. Successful dehazing results of various DCP-based dehazing algorithms [10–28] support the effectiveness of the DCP in image dehazing.

1.2.3 DCP-based image dehazing

In the DCP-based dehazing algorithm [10], the dark channel is first constructed from the input image as in Eq. (4). The atmospheric light and the transmission map are then obtained from the dark channel. The transmission map is further refined, and the haze-free image is finally reconstructed as Eq. (3).

More specifically, given the degradation model of

$$I(x) = J(x)t(x) + A(1-t(x)), \quad (6)$$

the minimum intensity in the local patch of each color channel is taken after dividing both sides of Eq. (6) by A^c as follows:

$$\min_{y \in \Omega(x)} \frac{I^c(y)}{A^c} = \tilde{t}(x) \min_{y \in \Omega(x)} \frac{J^c(y)}{A^c} + (1-\tilde{t}(x)). \quad (7)$$

Here the transmission in the local patch $\Omega(x)$ is assumed to be constant and is represented as $\tilde{t}(x)$ [10]. Then, the min operator of the three color channels can be applied to Eq. (7) as follows:

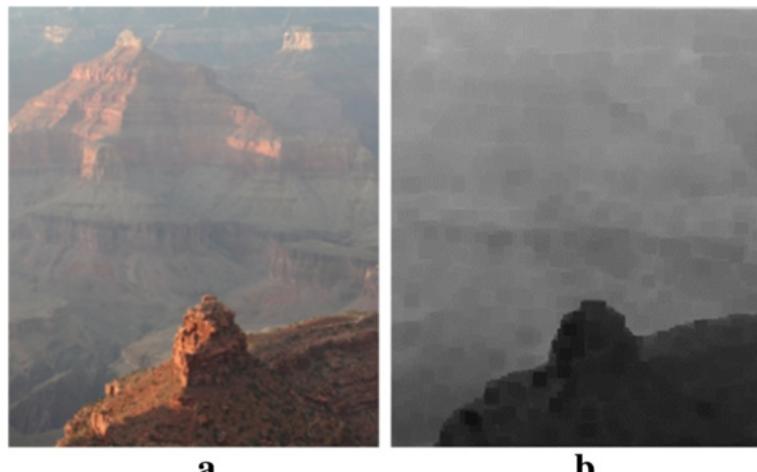


Fig. 3 Dark channel for a hazy image. **a** Hazy image. **b** Dark channel of (a)

$$\begin{aligned} \min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right) &= \tilde{t}(x) \min_{y \in \Omega(x)} \left(\min_c \frac{J^c(y)}{A^c} \right) \\ &\quad + (1-\tilde{t}(x)). \end{aligned} \quad (8)$$

According to the DCP approximation of Eq. (5), $\tilde{t}(x)$ can be represented as

$$\tilde{t}(x) = 1 - \min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right). \quad (9)$$

Here, the atmospheric light A needs to be estimated in order to obtain the transmission map \tilde{t} . Most of the previous single image based dehazing methods estimate A from the most haze-opaque pixels. As discussed in Section 1.2.2, the pixel value of the dark channel is highly correlated with haze density. Therefore, the top 0.1 % of the brightest pixels in the dark channel is first selected, and the color with the highest intensity value among the selected pixels is then used as the value for A [10].

Figure 4 illustrates the process used to obtain A . If the pixel with the highest intensity value is used to estimate A , the pixels in the patches as shown in Fig. 4d, e would be selected, yielding significant estimation errors. Instead, by finding the candidate pixels from the dark channel as shown in Fig. 4b, the pixel that accurately estimates A can be found as shown in Fig. 4c.

It is noted in [10] that the DCP is not reliable in the sky region. Fortunately, the color of the sky is close to A in hazy images, and thus, we have

$$\min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right) \approx 1 \text{ and } \tilde{t}(x) \approx 0. \quad (10)$$

This corresponds to the definition of $t(x)$ because $d(x)$ approaches infinity for the sky region. Therefore, the sky does not need special treatment for estimating the

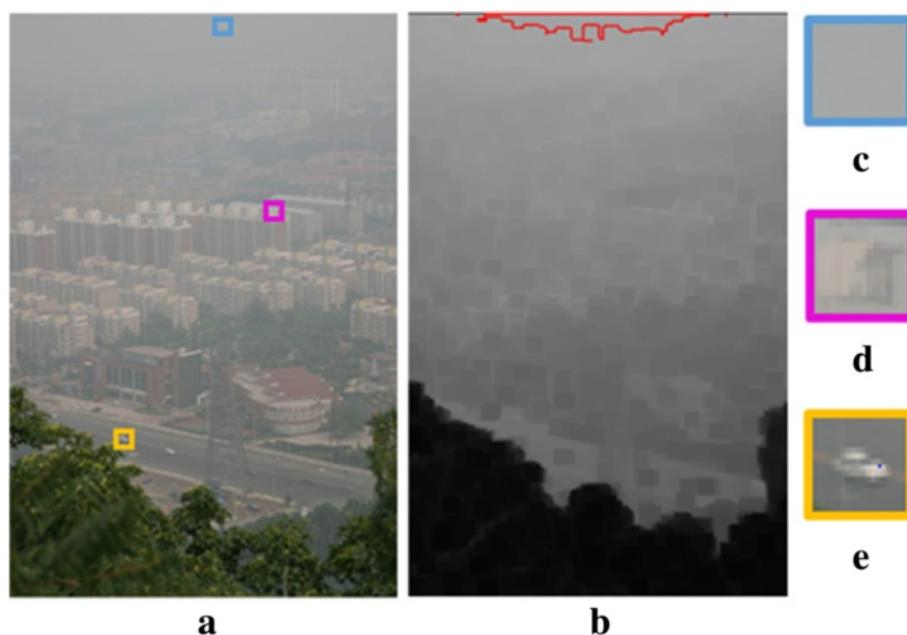


Fig. 4 Estimation of the atmospheric light [10]. **a** Hazy image. **b** Dark channel, where the size of Ω is 15×15 and the region inside the red boundary lines corresponds to the most haze-opaque region. **c** Patch used to determine the atmospheric light. **d, e** Patches that contain intensity values higher than that of the atmospheric light

transmission map if we obtain $\tilde{t}(x)$ as Eq. (9). Given A , \tilde{t} , and I , the dehazed image is obtained as

$$J(x) = \frac{I(x)-A}{\max(\tilde{t}(x), t_0)} + A, \quad (11)$$

where t_0 is used as a lower bound for the transmission map.

1.3 Analysis of DCP-based dehazing algorithms

In Section 1.2, we reviewed the original DCP-based dehazing algorithm [10]. The follow-up methods are based on the basic structure presented in [10] but differ in each step of the dehazing procedure. Table 1 shows the DCP-based dehazing algorithms from [10–24] that are investigated in this paper. Instead of analyzing each method individually, we classify all the methods in accordance with the four steps of image dehazing and then perform a step-by-step analysis. Each of the following subsections describes and compares the various methods used for each step.

1.3.1 Dark channel construction

Most conventional DCP-based dehazing methods estimate the dark channel from the input hazy image I . In Eq. (4), the size of the local patch $\Omega(x)$ is the only parameter that needs to be determined. Although the effect of the size of the local patch is significant, most conventional methods simply use a local patch with a fixed size

or do not specify the size of the local patch. Table 2 shows typical patch sizes used in the previous methods.

Figure 5a shows two hazy images. The top row in Fig. 5 corresponds to a remote aerial photograph with less local texture and heavy haze. Therefore, a small local

Table 1 Comparison of DCP-based dehazing algorithms

Step	Method	Reference
Dark channel construction	Min filter (Eq. (4))	[10–22, 24]
	Median filter (Eq. (12))	[23]
Atmospheric light estimation	Candidate	DCP top 0.1 % [10–15, 17, 18, 21, 23]
		DCP top 0.2 % [16]
		DCP maximum [19, 20, 22]
		DCP top 5 % and edge [24]
	Selection criterion	Intensity [10–20, 22–24]
		Entropy [21]
Transmission map construction	Eq. (17)	[10–13, 15–20, 22–24]
	Eq. (18)	[14]
	(i)	[21]
Transmission map refinement	Gaussian filter	[17–19]
	Bilateral filter	[11, 14, 24]
	Soft matting	[10, 11]
	Cross-bilateral filter	[16, 20]
	Guided filter	[13, 18, 22]

$$(i) t(x) = 1 - w \left(\log \left(\min_{c \in \{r, g, b\}} \frac{f_c(x)}{A^c} \right) \right)$$

Table 2 Local patch sizes used for previous methods

Patch size	Reference
3 × 3	[26]
11 × 11	[20]
15 × 15	[10, 21, 25]

patch is sufficient in order to estimate the dark channel, resulting in a reduction in the DCP calculation time. However, an image that has complicated local textures, as shown in the second row of Fig. 5, needs a larger local patch size to exclude false textures from the dark channel. Note that the block-min process of Eq. (4) inevitably decreases the apparent resolution of the dark channel as the size of the patch increases. Therefore, the minimum possible patch size that does not produce false textures in the dark channel needs to be found for every hazy image by considering application-dependent image local details.

Apart from the aforementioned general method for the dark channel estimation, Zhang [23] replaced the minimum operator by the median operator as follows:

$$I^{\text{dark}}(x) = \text{median}_{y \in \Omega(x)} \left(\min_{c \in \{r,g,b\}} I^c(y) \right). \quad (12)$$

As a result of the median operation, the dark channels become less blurry, as shown in Fig. 6. However, the median operator is computationally more complex than the minimum operator. Moreover, the median-based method is less physically meaningful because the assumption of the DCP becomes deteriorated. As shown in the second row of Fig. 6, dense image textures remain visible for the dark channel, even when a large patch size of 15 × 15 is used. For the sake of the visibility enhancement of hazy images, however, the median filter is somewhat effective because it does not require complicated post-processing, which is necessary for smooth and

blurry dark channels that are obtained by the minimum operator.

1.3.2 Atmospheric light estimation

The majority of conventional DCP-based dehazing methods estimate A as described in Section 1.2.3. In [19, 20], the pixel with the highest dark channel value is used directly as follows:

$$A = I(\text{argmax}_x(I^{\text{dark}}(x))). \quad (13)$$

However, the above method can incorrectly select the pixel when the scene contains bright objects. Instead, pixels with a top $p\%$ dark channel values are selected as the most haze-opaque pixels, and the one with the highest intensity is used to estimate A . This remains one parameter p in the estimation of A , which is empirically set as 0.1 [10–15] or 0.2 [16].

In [21], to explicitly exclude bright objects from the estimation of A , the local entropy is measured as

$$E(x) = \sum_{i=0}^N (p_x(i) \times \log_2(p_x(i))), \quad (14)$$

where $p_x(i)$ represents the probability of a pixel value i in the local patch centered at x , and N represents the maximum pixel value. The local entropy value is low for regions with smooth variations, which highly likely correspond to haze-opaque regions. Therefore, the pixel with the lowest entropy value is used to obtain A among the highest $p\%$ pixels in the dark channel ($p = 0.1$ [21]).

Table 3 lists the conventional methods that are used to estimate atmospheric light. To quantitatively evaluate atmospheric light estimation methods, we used the foggy road image database (FRIDA) [38] which consists of pairs of synthetic color and depth images. For a given depth image and β , the ground-truth transmission map can be constructed as $t(x) = e^{-\beta d(x)}$. The hazy image I is

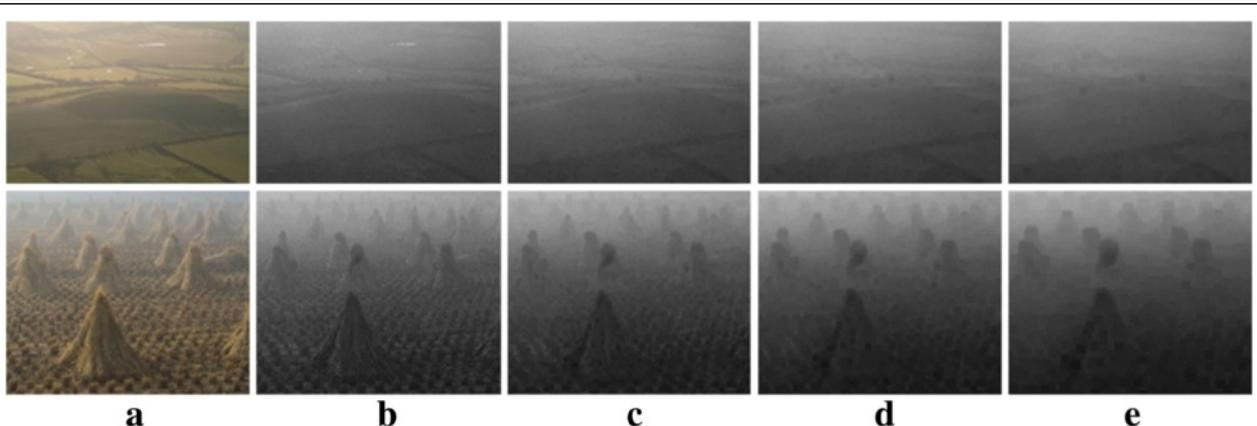


Fig. 5 Dark channels of various patch size obtained by Eq. (4). **a** Hazy image. Dark channels obtained by Eq. (4) with the patch size of **(b)** 3 × 3, **(c)** 7 × 7, **(d)** 11 × 11, and **(e)** 15 × 15

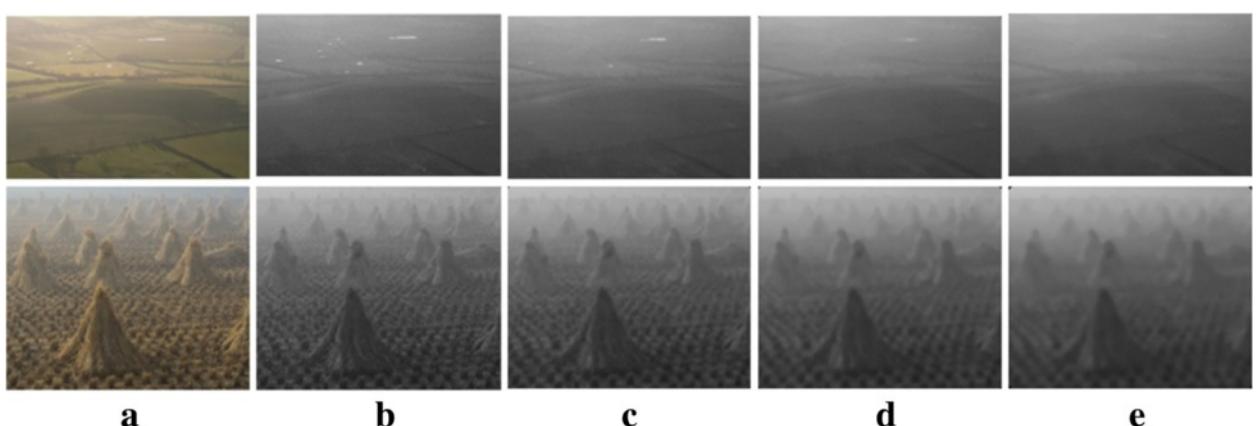


Fig. 6 Dark channels of various patch size obtained by Eq. (12). **a** Hazy images. Dark channels obtained by Eq. (12) with the patch size of **(b)** 3×3 , **(c)** 7×7 , **(d)** 11×11 , and **(e)** 15×15

then obtained as Eq. (6) by using the atmospheric light A . Therefore, a variety of hazy images can be generated by changing β (haze density) and A (global lightness).

Figure 7 shows the average root-mean-square error (RMSE) between the ground-truth and estimated atmospheric lights for the 66 test images in the FRIDA. The RMSE is obtained as

$$RMSE = \sqrt{\frac{1}{3} \left((\hat{A}_R - A_R^*)^2 + (\hat{A}_G - A_G^*)^2 + (\hat{A}_B - A_B^*)^2 \right)}, \quad (15)$$

where $A^* = (A_R^* A_G^* A_B^*)$ and $\hat{A} = [\hat{A}_R \hat{A}_G \hat{A}_B]$ represent the ground-truth and estimated atmospheric lights, respectively. Since the candidate pixels for the atmospheric light estimation are obtained from the dark channel, the local patch size also plays an important role in the accuracy of the estimation. When a small patch size is used, as shown in Fig. 8b, the pixels for bright objects are considered as candidate pixels, yielding inaccurate A estimates. The use of a large patch size can prevent selecting such pixels, as shown in Fig. 8c. The quantitative evaluation result as shown in Fig. 7a also supports our observation. The accuracy is rather insensitive to p when a large 32×32 patch is used. Therefore, a large patch size (e.g., 32×32) with $p = 0\text{--}0.4\%$ is effective only when the accuracy of the atmospheric light estimation is considered. One practical solution that takes into

account the accuracy of both the dark channel and the atmospheric light involves using different patch sizes to estimate the dark channel estimation and atmospheric light [26]. When the local entropy, as in Eq. (15), is used to prevent pixels of small bright objects from being selected, the estimation accuracy of the atmospheric light improves, as shown in Fig. 7b [21]. The estimation accuracy is still best for the largest patch size of 32×32 and is less sensitive to the p value due to the robustness of candidate pixel selection.

1.3.3 Transmission map estimation

The transmission map $\tilde{t}(x)$ fined in Eq. (9) is obtained from the DCP. If the DCP is not exploited, Eq. (9) can be rewritten as

$$\tilde{t}(x) = 1 - \min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right) + \tilde{t}(x) \cdot \min_{y \in \Omega(x)} \left(\min_c \frac{J^c(y)}{A^c} \right). \quad (16)$$

As we observed in Section 1.2.2, the pixel value of the dark channel, $J^{\text{dark}}(x)$, is highly likely zero, and so is $(J/A)^{\text{dark}}(x)$. However, if $(J/A)^{\text{dark}}(x)$ is not close to zero, the transmission map obtained as Eq. (9) can be under-estimated since the positive offset in Eq. (16) is always neglected [28].

In the original DCP-based dehazing method, it is mentioned that the image may look unnatural if the haze is removed thoroughly [10]. A constant ω ($0 < \omega < 1$) is thus used to retain a small amount of haze:

$$\tilde{t}(x) = 1 - \omega \min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right). \quad (17)$$

However, we consider that a better visibility in the dehazed image can be achieved with Eq. (17) because we inadvertently compensate for the under-estimation of $\tilde{t}(x)$ by multiplying ω .

Table 3 Conventional methods used to estimate atmospheric light

Input	Parameter	Selection criterion	Reference
Dark channel	$p = 0$	Highest intensity	[19, 20]
	$p = 0.1$	Highest intensity	[10–15]
	$p = 0.2$	Highest intensity	[16]
	$p = 0.1$	Minimum entropy	[21]

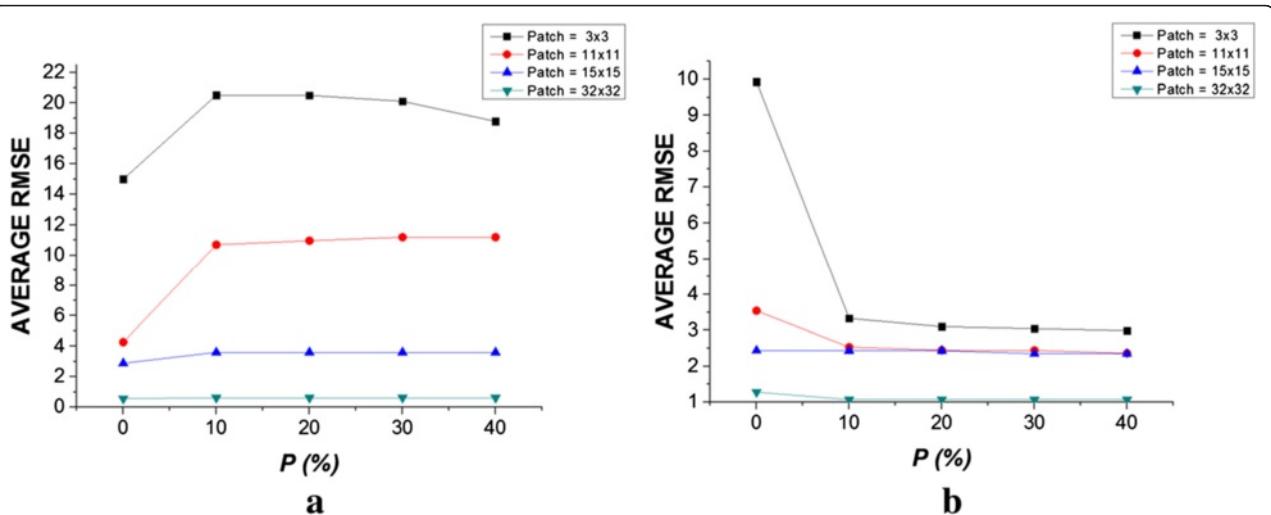


Figure 9 shows that the transmission map is indeed under-estimated when \tilde{t} is obtained as Eq. (9). The mean values of the ground-truth transmission maps, as shown in Fig. 9b, are 0.5616 and 0.6365, respectively. However, the mean values for the estimated transmission maps, as shown in Fig. 9c, are obtained as 0.5125 and 0.6086, respectively. When

the transmission map is obtained as Eq. (17) by using $\omega = 0.9$, the under-estimation of the transmission map is considerably decreased, as shown in Fig. 10a, c, where the mean values are obtained as 0.5225 and 0.6058, respectively.

Xu et al. [14] explicitly addressed the aforementioned under-estimation problem of the transmission map and

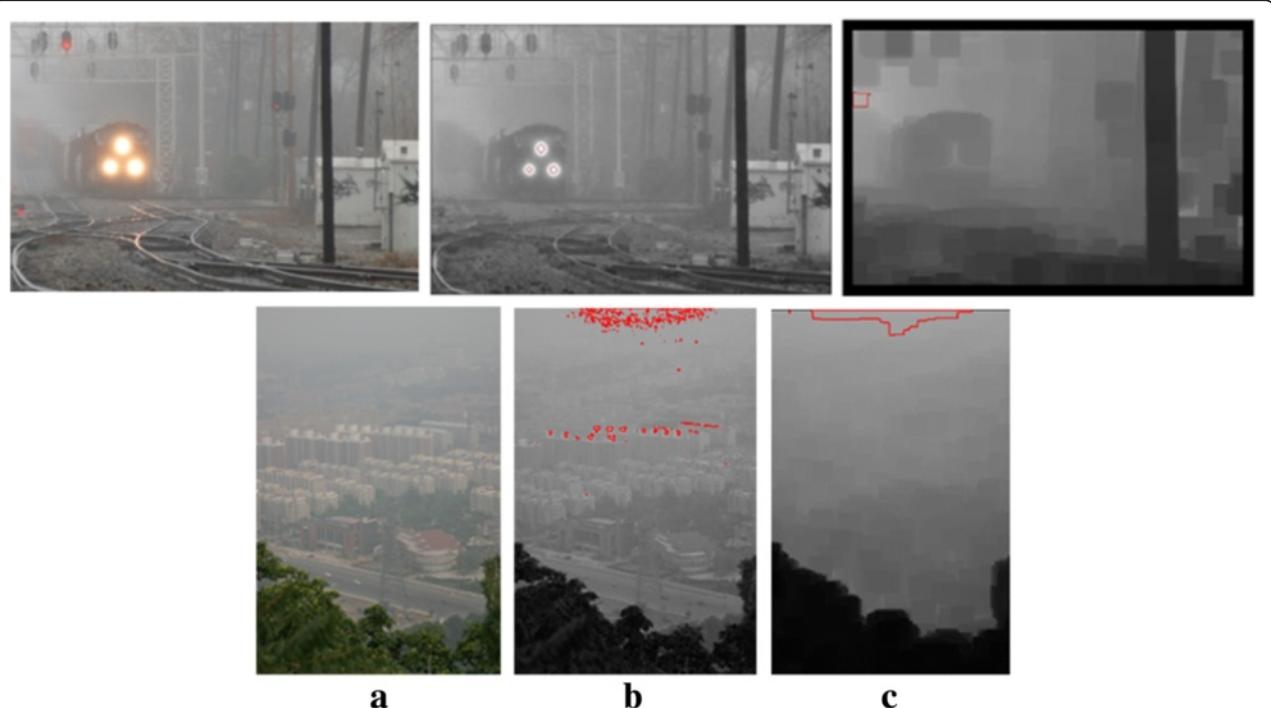


Fig. 8 Atmospheric light estimation. **a** Hazy image. The pixels in the dark channel that are used to estimate the atmospheric light when the size of Ω is (b) 3×3 and (c) 32×32

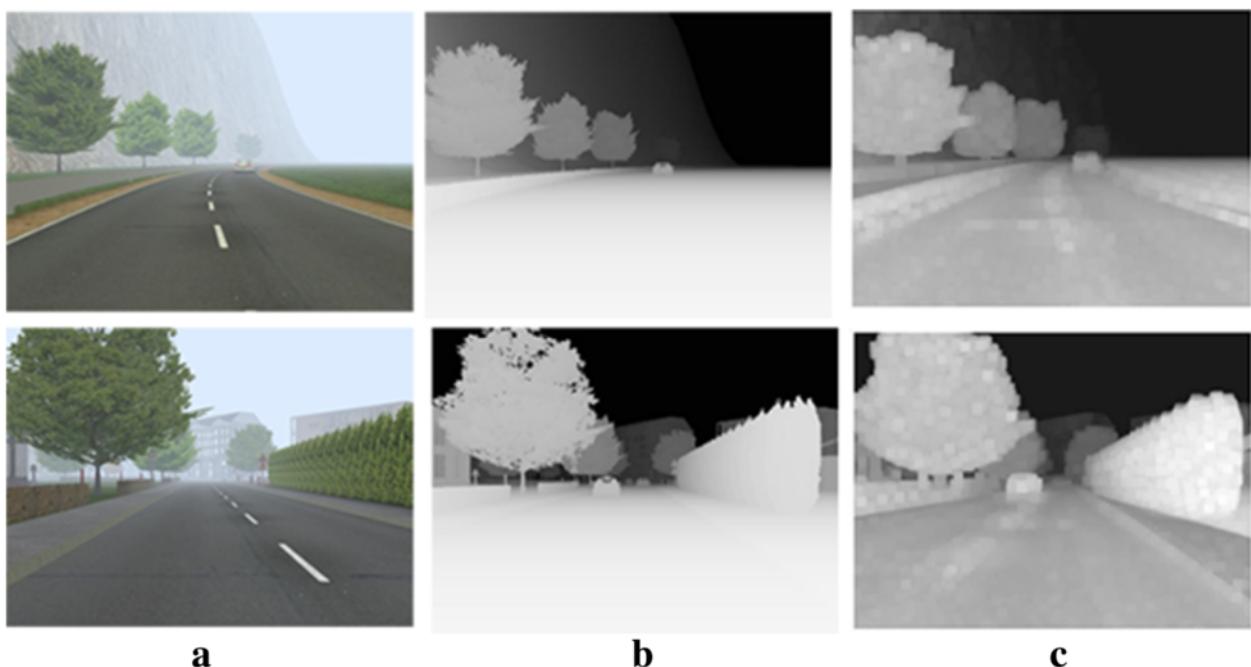


Fig. 9 Hazy images and ground-truth and estimated transmission maps from the FRIDA [46]. **a** Hazy images. **b** Ground-truth transmission maps, where $A = [220, 235, 254]$ and $\beta = 0.01$. **c** Transmission maps obtained as Eq. (9). For visualization, transmission values are multiplied by 255

simply added a positive value $\rho \in [0.08, 0.25]$ to the transmission map:

$$\tilde{t}(x) = 1 - \min_{y \in \Omega(x)} \left(\min_c \frac{I^c(y)}{A^c} \right) + \rho. \quad (18)$$

Figure 10b, d shows the estimated transmission maps when $\rho = 0.08$ is added, where the mean values are obtained as 0.5494 and 0.6431, respectively. The addition of ρ also plays a similar role of t_0 in Eq. (11), making the minimum value of the transmission map be ρ . The under-estimation can be partly solved by using Eq. (17) or (18); however, the values of ω and ρ need to be carefully chosen. To this end, we measured the RMSE values between the ground-truth and estimated transmission maps for different ω and ρ values by using 66 synthetic

test images from the FRIDA. Figure 11a, b indicates that ω around 0.9 and ρ around 0.12 are effective. An adaptive scheme also needs to be developed for a better compensation of the under-estimation.

1.3.4 Transmission map refinement

Incorrect estimation for the transmission map can lead to some problems such as false textures and blocking artifacts. In particular, the block-min process of Eq. (4) decreases the apparent resolution of the dark channel, resulting in blurry transmission maps. For this reason, many methods have been developed to further sharpen the transmission map [10, 11, 13, 14, 16–20, 22, 24].

In [42], it is especially mentioned that many dehazing methods differ in the way of smoothing the transmission map. Table 4 lists post-filtering methods used to

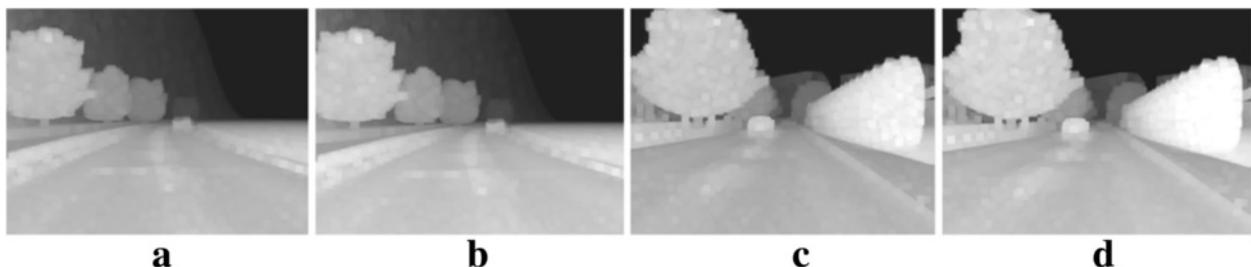
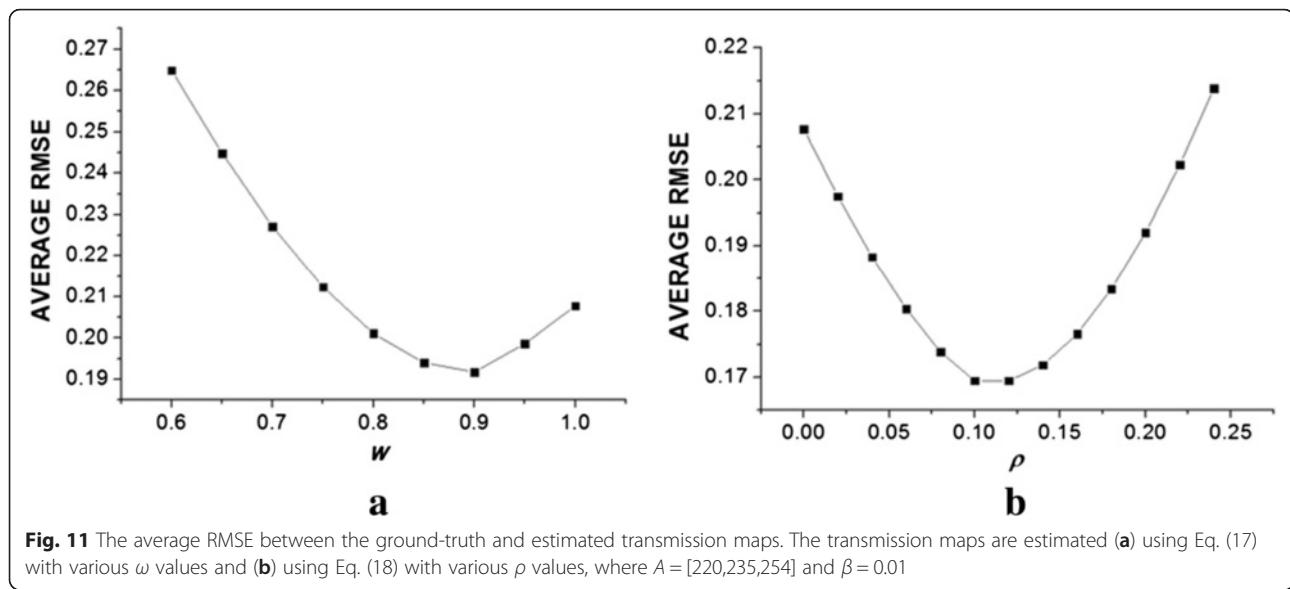


Fig. 10 Comparison of the estimated transmission maps using the FRIDA [46]. **a, c** Transmission maps obtained as Eq. (17) using $\omega = 0.9$. **b, d** The transmission map obtained as Eq. (18) using $\rho = 0.08$, where $A = [220, 235, 254]$ and $\beta = 0.01$



improve the accuracy of the transmission map. Some filtering methods, such as the Gaussian and bilateral filters, use only transmission maps, whereas the other methods, such as soft matting, cross-bilateral filter, and guided filter, exploit a hazy color image as a guidance signal. Each method and its performance are analyzed in the following subsections.

1.3.4.1 Gaussian filter

Denoting the transmission map to be refined as \tilde{t} , the Gaussian filtered transmission map \hat{t} is given as

$$\hat{t}(x) = \frac{1}{\sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|)} \cdot \sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|) \tilde{t}(y), \quad (19)$$

where G_{σ_s} is the 2-D Gaussian function with the standard deviation σ_s . The Gaussian filter is not very effective in sharpening a blurry transmission map due to its low-pass characteristic, but it is often useful in removing color textures remaining in the transmission map [19]. As discussed in Section 1.3.1, transmission maps obtained using a small local patch tend to have color textures, and thus, the Gaussian filter can improve the

accuracy of the transmission maps. Figure 12 shows some examples before and after Gaussian filtering. As can be seen in Figs. 12b, c, the Gaussian filter is effective in removing false color textures in the transmission map. However, the Gaussian filter can unnecessarily blur the transmission map when there is no annoying false color textures in the transmission map as shown in Fig. 12d, e.

Figure 13 shows the quantitative quality evaluation results. Here, the transmission maps are obtained as Eq. (17) with different sizes of the local patch. The Gaussian filter is then applied and the filtered result is compared with the ground-truth transmission map, which can be reconstructed using the FRIDA [46]. As can be seen in Fig. 13, the Gaussian filter is effective when a proper size of the patch size is used, but the RMSE starts increasing when the Gaussian blur becomes excessive. Therefore, the refinement by the Gaussian filter needs careful treatment with the consideration of the color textures in the hazy image.

1.3.4.2 Bilateral filter

The bilateral filter is a widely used edge-preserving smoothing filter. It uses weighted neighboring pixel values with the spatial and range distances as follows:

$$\hat{t}(x) = \frac{1}{\sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|) G_{\sigma_r}(\|I(x)-I(y)\|)} \cdot \sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|) G_{\sigma_r}(\|I(x)-I(y)\|) \tilde{t}(y), \quad (20)$$

where G_{σ_s} and G_{σ_r} represent the spatial and range kernels with the standard deviations σ_s and σ_r , respectively. Since the neighboring pixels that have the similar pixel

Table 4 Conventional methods used to refine the transmission map

Input	Method	Reference
Transmission map	Gaussian filter	[17, 19]
	Bilateral filter	[14, 24]
Transmission map and hazy image	Soft matting	[10, 11]
	Cross-bilateral filter	[16, 20]
	Guided filter	[13, 18, 22]

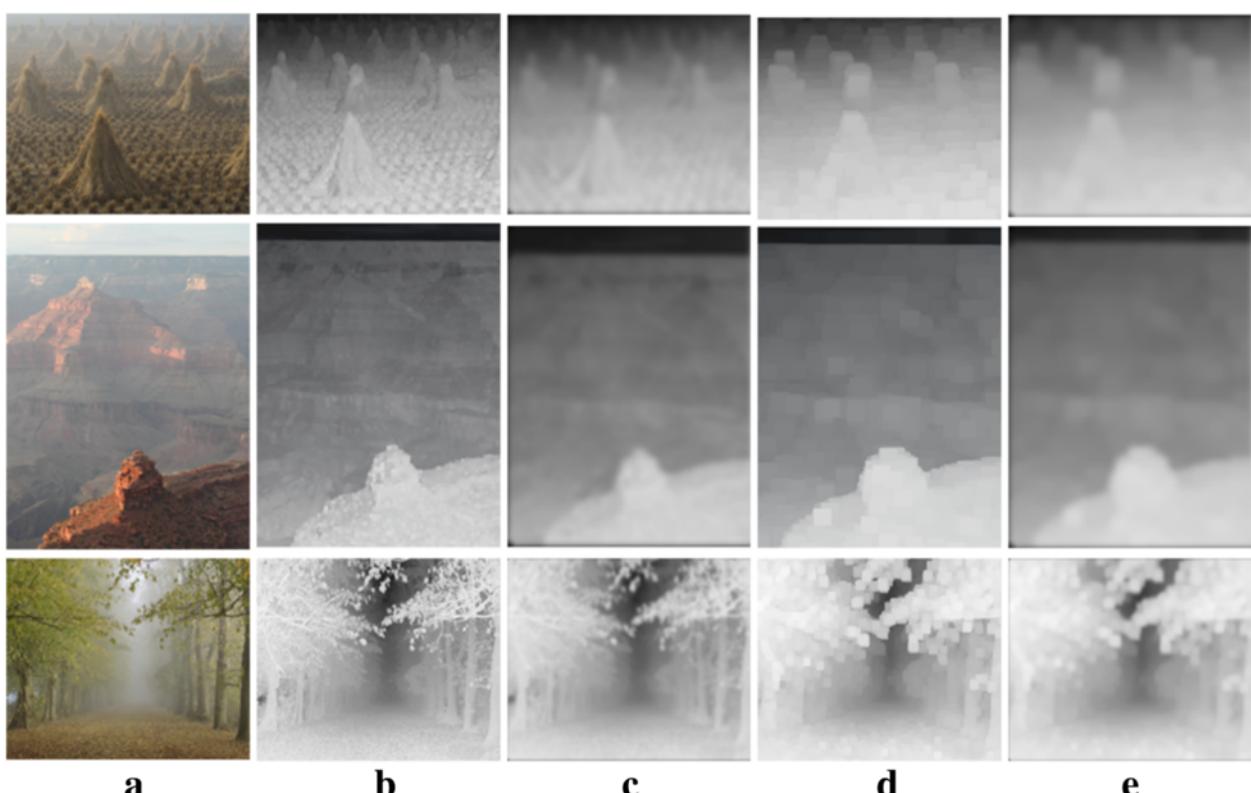


Fig. 12 The result of the Gaussian filter. **a** Hazy images. **b** Transmission map obtained using the local patch with the size 3×3 . **c** Gaussian filtered transmission map using $\sigma_s = 5$. **d** Transmission map obtained using the local patch with the size 15×15 . **e** Gaussian filtered transmission map using $\sigma_s = 5$

value with the center pixel are highly weighted, edges in \tilde{t} can be preserved while smoothing noisy regions in \tilde{t} . The bilateral-filtered transmission maps as shown in Fig. 14 tend to exhibit sharper details than the Gaussian filtered transmission maps as shown in Fig. 12.

We also evaluated the quantitative performance of the bilateral filter as shown in Fig. 15 using the same experimental condition of Fig. 14. σ_s is set as 15 and

the performance dependency on σ_r is only investigated. The results illustrate that the bilateral filter is not very effective in terms of the quantitative performance and tends to increase the RMSE when the standard deviation of the range kernel increases.

1.3.4.3 Soft matting We found that the Gaussian and bilateral filters are effective for removing false color

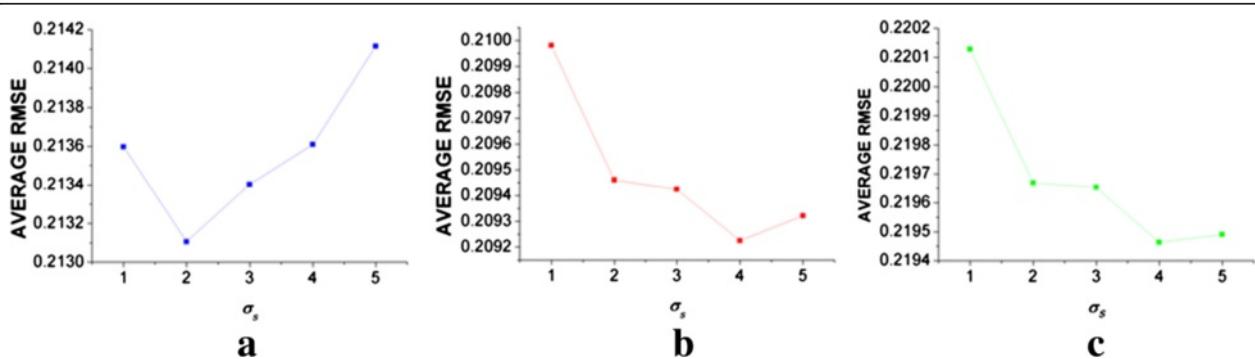


Fig. 13 The average RMSE between ground-truth and Gaussian filtered transmission maps using the FRIDA [46]. The RMSE results with respect to σ_s when the local patch size is **(a)** 3×3 , **(b)** 11×11 , and **(c)** 15×15

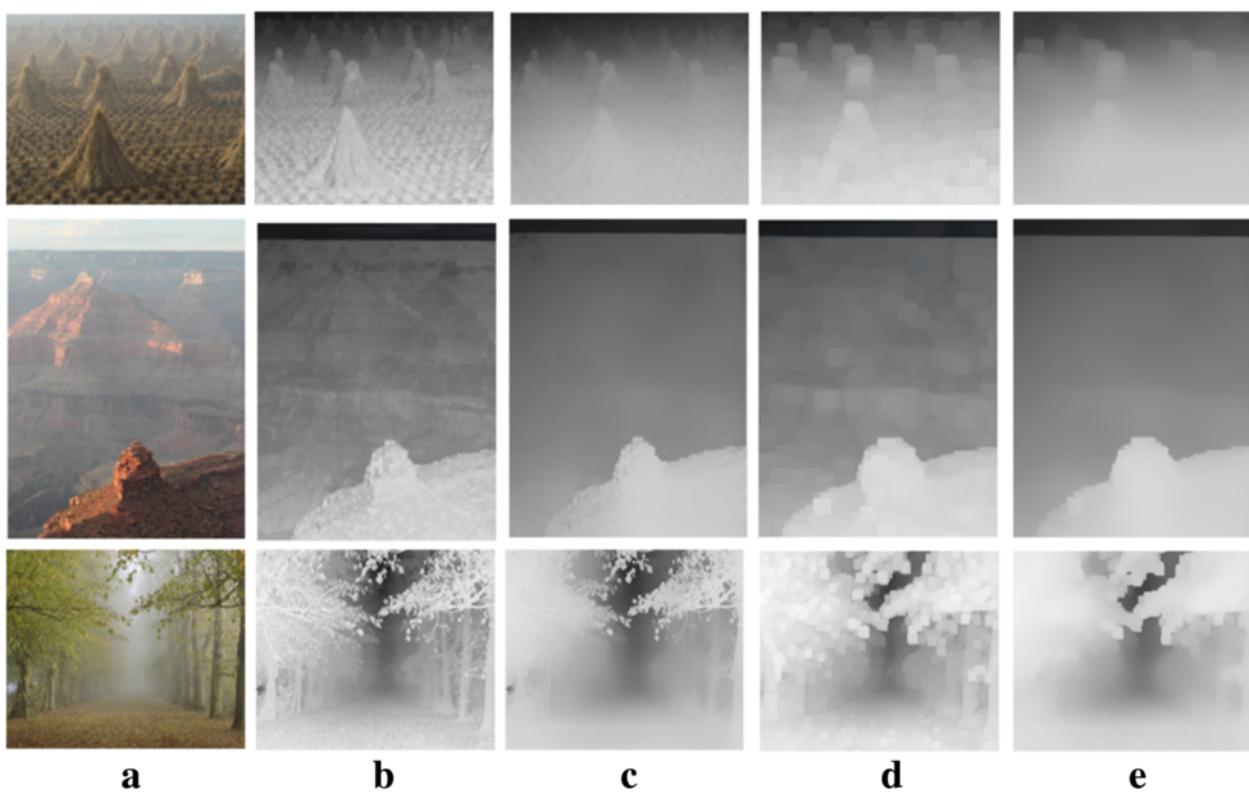


Fig. 14 The result of the bilateral filter. **a** Hazy images. **b** Transmission maps obtained using the local patch with the size 3×3 . **c** Bilateral filtered transmission maps using $\sigma_s = 15$ and $\sigma_r = 0.3$. **d** Transmission maps obtained using the local patch with the size 15×15 . **e** Bilateral filtered transmission maps using $\sigma_s = 15$ and $\sigma_r = 0.1$

textures in the transmission map. However, the transmission map should have a similar level of sharpness to the color image for dehazing, which is impossible if the color image is not used in the transmission map refinement. To this end, the original DCP-based dehazing algorithm [10] adopted the soft matting to refine the transmission map. From the observation that the degradation model in Eq. (6) is similar to the

matting equation [47], the refined transmission map \tilde{t} is obtained by minimizing the following energy function:

$$\hat{t} = \arg \min_t \left\{ t^T L t + \lambda (t - \tilde{t})^T (t - \tilde{t}) \right\}, \quad (21)$$

where \tilde{t} is the transmission map to be refined and a weight λ controls the importance of the data term. It

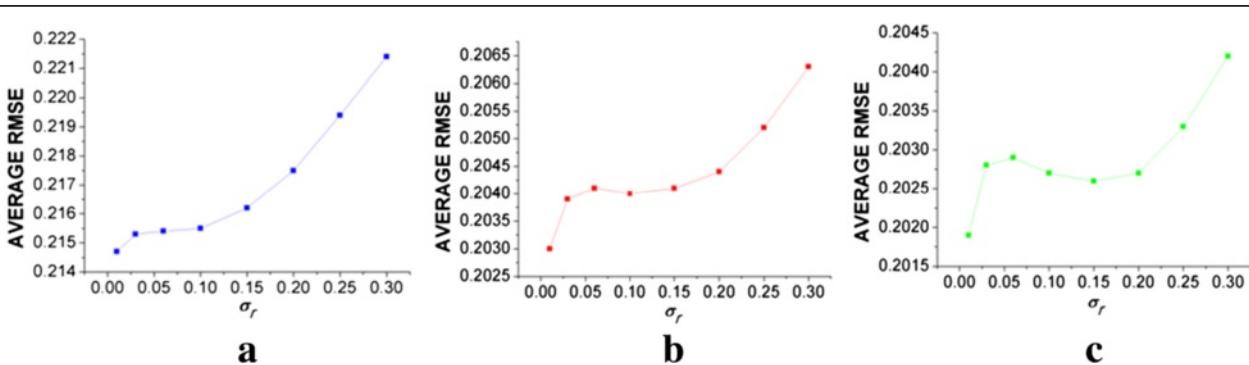


Fig. 15 The average RMSE between ground-truth and bilateral-filtered transmission maps using the FRIDA [46]. The RMSE values with respect to σ_r , when the local patch size is **(a)** 3×3 , **(b)** 11×11 , and **(c)** 15×15 , where $\sigma_s = 15$ and $\sigma_r \in \{0.01, 0.03, 0.06, 0.1, 0.15, 0.2, 0.25, 0.3\}$

is demonstrated in [11] that the solution of Eq. (21) is equivalent to that of the following sparse linear equation:

$$(L + \lambda U)\hat{t} = \lambda\tilde{t}, \quad (22)$$

where U represents an identity matrix. Note that in order to exploit sharp details in the hazy image, the Laplacian matrix L is determined from the hazy image. We refer the readers for more details about image matting to [11, 47]. Figure 16 shows the refined transmission maps obtained by the soft matting. As can be seen, blurry edges in the transmission maps have been sharpened due to the use of color images. It should be noted here that the bilateral filter was also applied to the result of the soft matting to further refine the transmission map [10]. To evaluate the performance of the soft matting only, the bilateral filter is not applied.

Figure 17 shows the quantitative performance of the soft matting. Different values of λ and patch sizes were used to find out the dependency of the performance of the soft matting on the parameters. A large value of λ was preferred when a small local patch was used because the transmission map before the refinement

tended to be inherently similar to the hazy image. When the local patch of the size 15×15 was used, a proper value of λ ($=2 \times 10^{-4}$ in our experiment) showed the best performance.

1.3.4.4 Cross-bilateral filter The cross-bilateral filter (aka joint-bilateral filter) is a variant of the classic bilateral filter. Unlike the bilateral filter, the cross-bilateral filter computes the range kernel from a cross (guidance) channel as follows:

$$\hat{t}(x) = \frac{1}{\sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|)G_{\sigma_r}(\|I(x)-I(y)\|)} \cdot \sum_{y \in \Omega(x)} G_{\sigma_s}(\|x-y\|)G_{\sigma_r}(\|I(x)-I(y)\|)\tilde{t}(y), \quad (23)$$

where the guidance channel I corresponds to the hazy image as in Eq. (1). Therefore, the sharpness of I can be inherited to the transmission map \hat{t} . Figure 18 shows the result of the cross-bilateral filter, and Fig. 19 shows the quantitative performance evaluation result using a fixed value of $\sigma_s=15$ and various σ_r values. Owing to the use of the cross channel, the resultant transmission map can

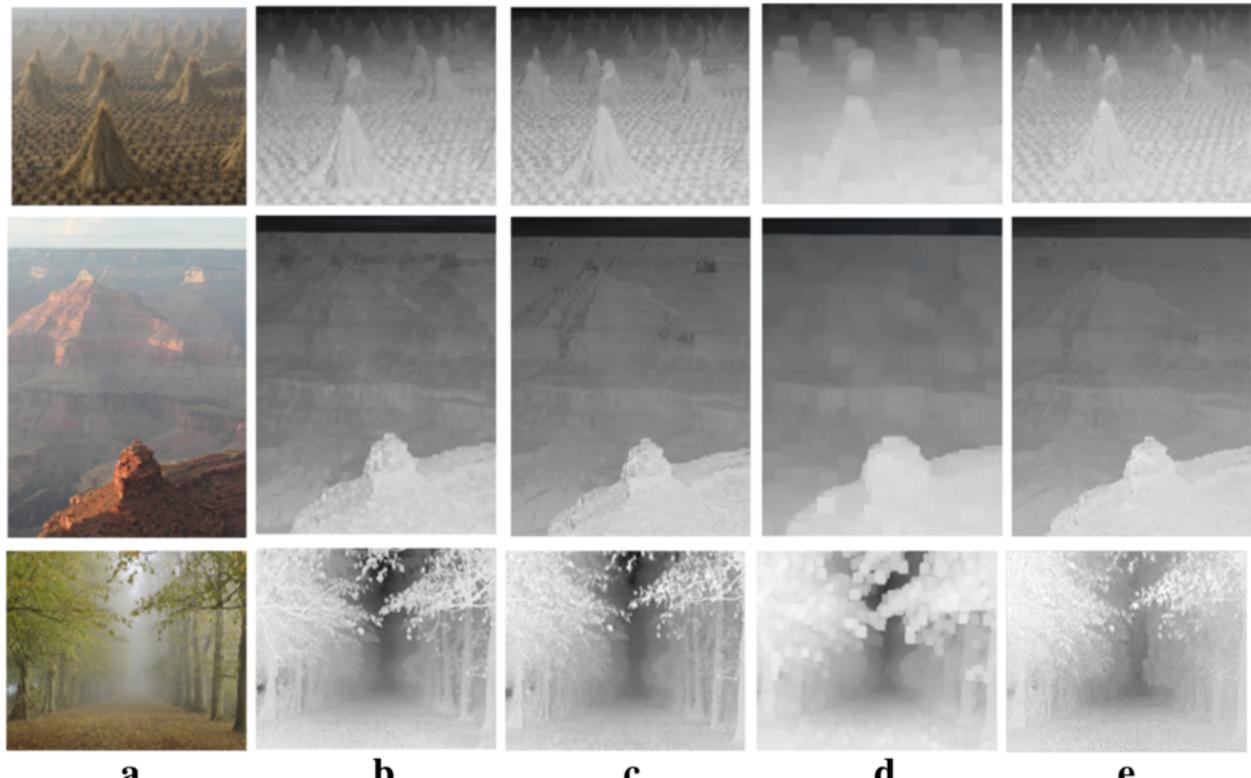


Fig. 16 The result of the soft matting using $\lambda=10^{-4}$. **a** Hazy images. **b** Transmission maps obtained using the local patch with the size 3×3 . **c** Soft matting results of (b). **d** Transmission maps obtained using the local patch with the size 15×15 . **e** Soft matting results of (d)

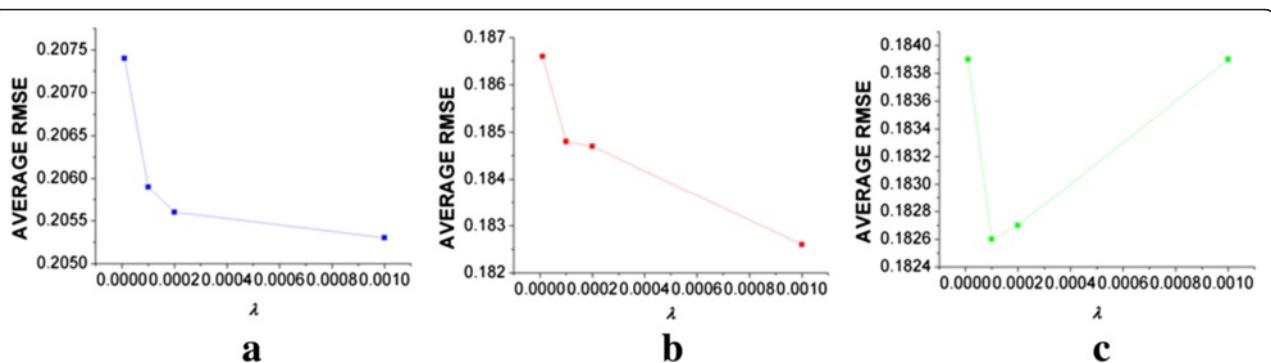


Fig. 17 The average RMSE between ground-truth and soft matting filtered transmission maps using the FRIDA [46]. The RMSE values with respect to σ_r when the local patch size is (a) 3×3 , (b) 11×11 , and (c) 15×15 , where $\lambda \in \{10^{-5}, 10^{-4}, 2 \times 10^{-4}, 10^{-3}\}$

exhibit sharper edges than those obtained by the Gaussian and bilateral filters. The selection of σ_r was also found to be important for the accuracy of the transmission map, and the best value of σ_r was found around 0.1 regardless of the size of the local patch. Unlike the computationally expensive soft matting method (which takes 10–20 s on average for images

with the size 600×400 [11]), it was shown in [20] that the cross-bilateral filter can be implemented in real-time using the GPU.

1.3.4.5 Guided filter To speed up the transmission map refinement, the authors of the original DCP-based dehazing method [10] replaced the soft

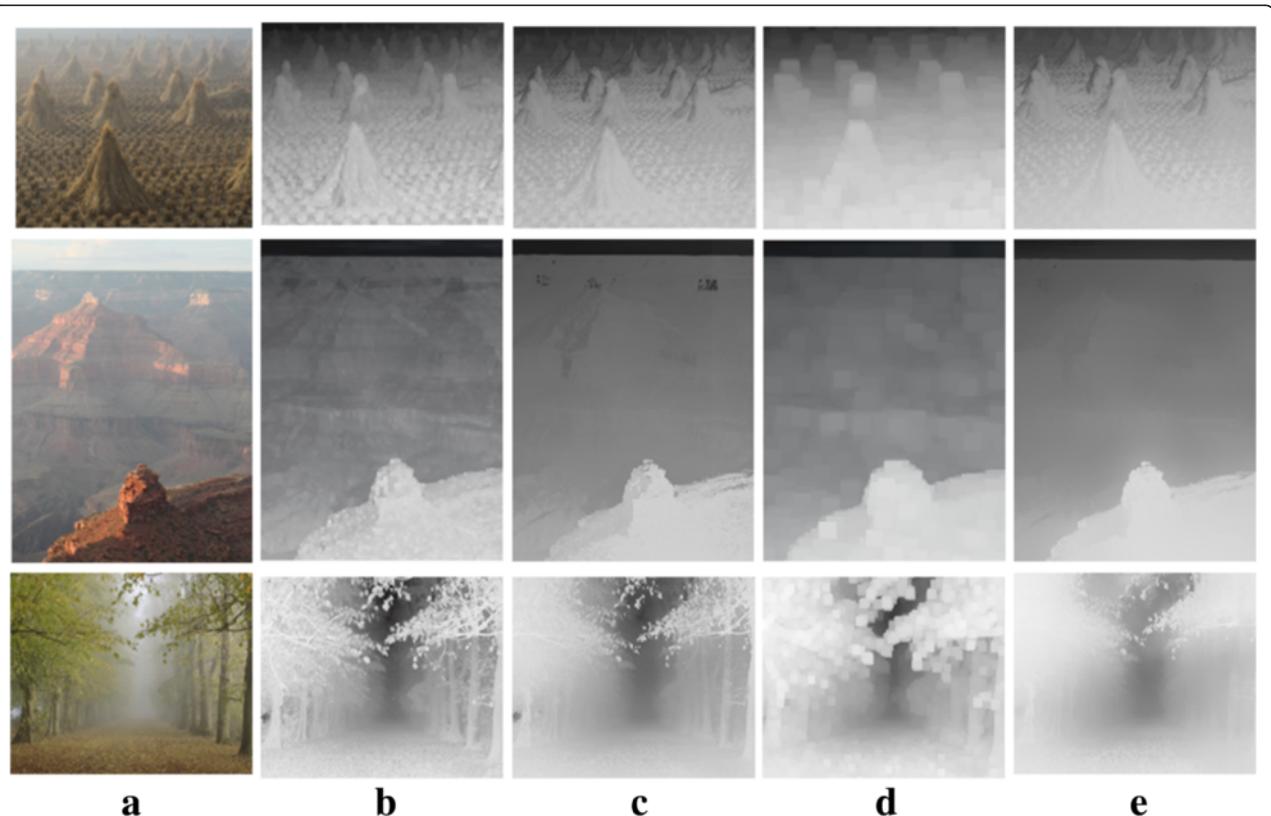
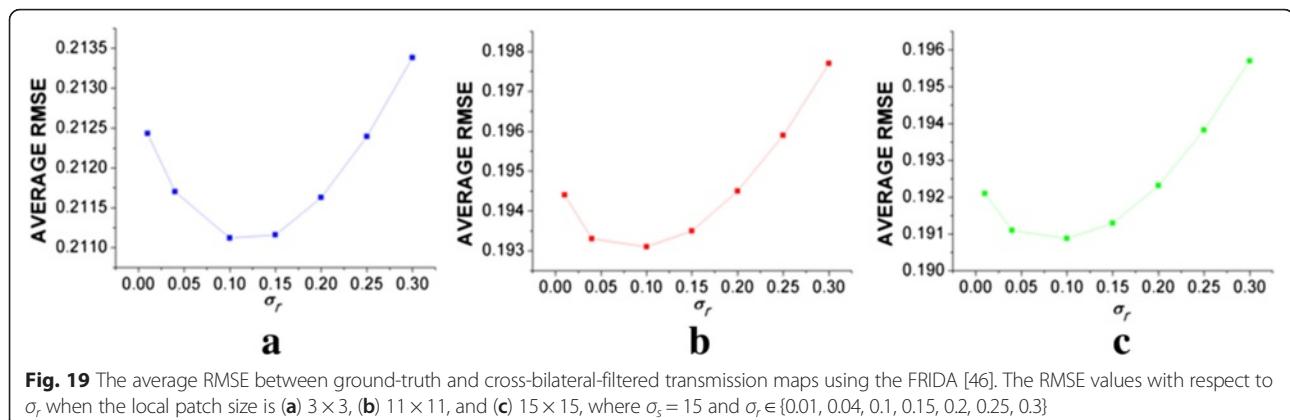


Fig. 18 The result of the cross-bilateral filter. **a** Hazy images. **b** Transmission map obtained using the local patch with the size 3×3 . **c** Cross-bilateral filtered transmission map using $\sigma_s = 15$ and $\sigma_r = 0.1$. **d** Transmission map obtained using the local patch with the size 15×15 . **e** Cross-bilateral-filtered transmission map using $\sigma_r = 15$ and $\sigma_r = 0.1$



matting to the guided filter [13, 18, 22, 48]. The guided filter also uses the hazy image I as a guidance, but its novelty lies in adopting the linear model as follows:

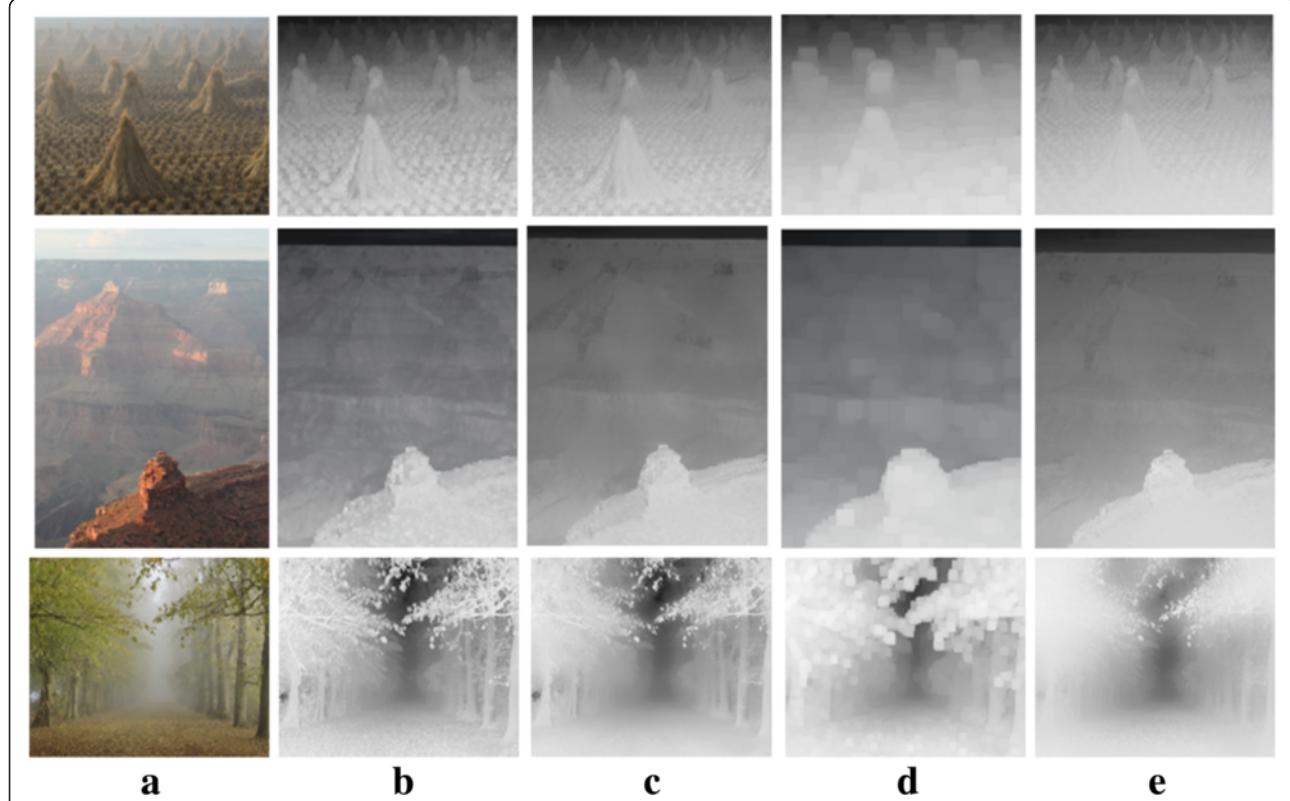
$$\hat{t}(y) = a_x I(y) + b_x, \quad \forall y \in \Omega_x, \quad (24)$$

where the coefficients a_x and b_x are assumed to be constant in Ω_x and are derived by minimizing the following energy:

$$E(a_x, b_x) = \sum_{y \in \Omega(x)} \left((a_x I(y) + b_x - \tilde{t}(y))^2 + (\varepsilon a_x)^2 \right), \quad (25)$$

where ε is a regularization parameter penalizing large a_x . The solution (a_x, b_x) can be obtained as

$$a_x = \frac{\frac{1}{|\mathcal{W}|} \sum_{y \in \Omega_x} I_y \tilde{t}(y) - \mu_x \bar{t}(x)}{\sigma_x^2 + \varepsilon}, \quad b_x = \bar{t}(x) - b_x \mu_x, \quad (26)$$



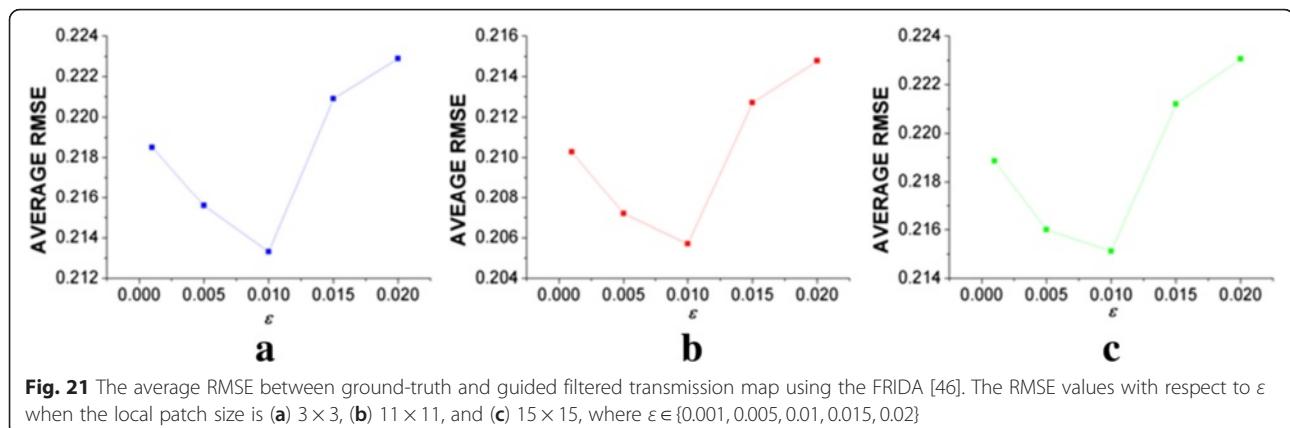


Fig. 21 The average RMSE between ground-truth and guided filtered transmission map using the FRIDA [46]. The RMSE values with respect to ε when the local patch size is (a) 3×3 , (b) 11×11 , and (c) 15×15 , where $\varepsilon \in \{0.001, 0.005, 0.01, 0.015, 0.02\}$

where μ_x and σ_x^2 are the mean and variance of the guidance image I in window Ω_x , respectively. $|w|$ denotes the number of pixels in Ω_x and $\bar{t}(x) = \frac{1}{|w|} \sum_{y \in \Omega(x)} \tilde{t}(y)$. Considering the overlapping windows in calculating a_x and b_x , the final refined transmission map $\hat{t}(x)$ is obtained as

$$\hat{t}(x) = \bar{a}_x \tilde{t}(x) + \bar{b}_x, \quad (27)$$

where $\bar{a}_x = \frac{1}{|w|} \sum_{y \in \Omega(x)} a_y$ and $\bar{b}_x = \frac{1}{|w|} \sum_{y \in \Omega(x)} b_y$ denote the average of all the coefficients obtained at pixel x .

Figure 20 shows the result of the guided filter. Since the refined transmission map is fully obtained from the hazy image, the resultant map contains the similar level of sharpness of the hazy image without yielding significant false color textures. Figure 21 shows the quantitative performance of the guided filter with different ε values. As ε increases, the transmission map becomes smooth, and thus, a proper selection of ε is significant. In our experiments using the FRIDA, ε of 0.01 produced the smallest RMSE value regardless of the size of the local patch.

1.3.4.6 Auxiliary methods for transmission map enhancement Recent efforts are made to enhance the transmission map [31, 32, 34–36], which can be categorized into three different approaches. The first approach is to use the transmission map obtained at low resolution [34, 36]. In [34], the guided filter is performed at low resolution and the filter coefficients at the original resolution are obtained using bilinear interpolation, which enables a speedup of the transmission map refinement. In [36], non-overlapping patches with the size 10×10 are used to obtain a very low resolution transmission map, and then, it is combined with a very high-resolution transmission map obtained using $\Omega(x) = x$ in Eq. (9). This combination scheme can make the transmission map refinement unnecessary.

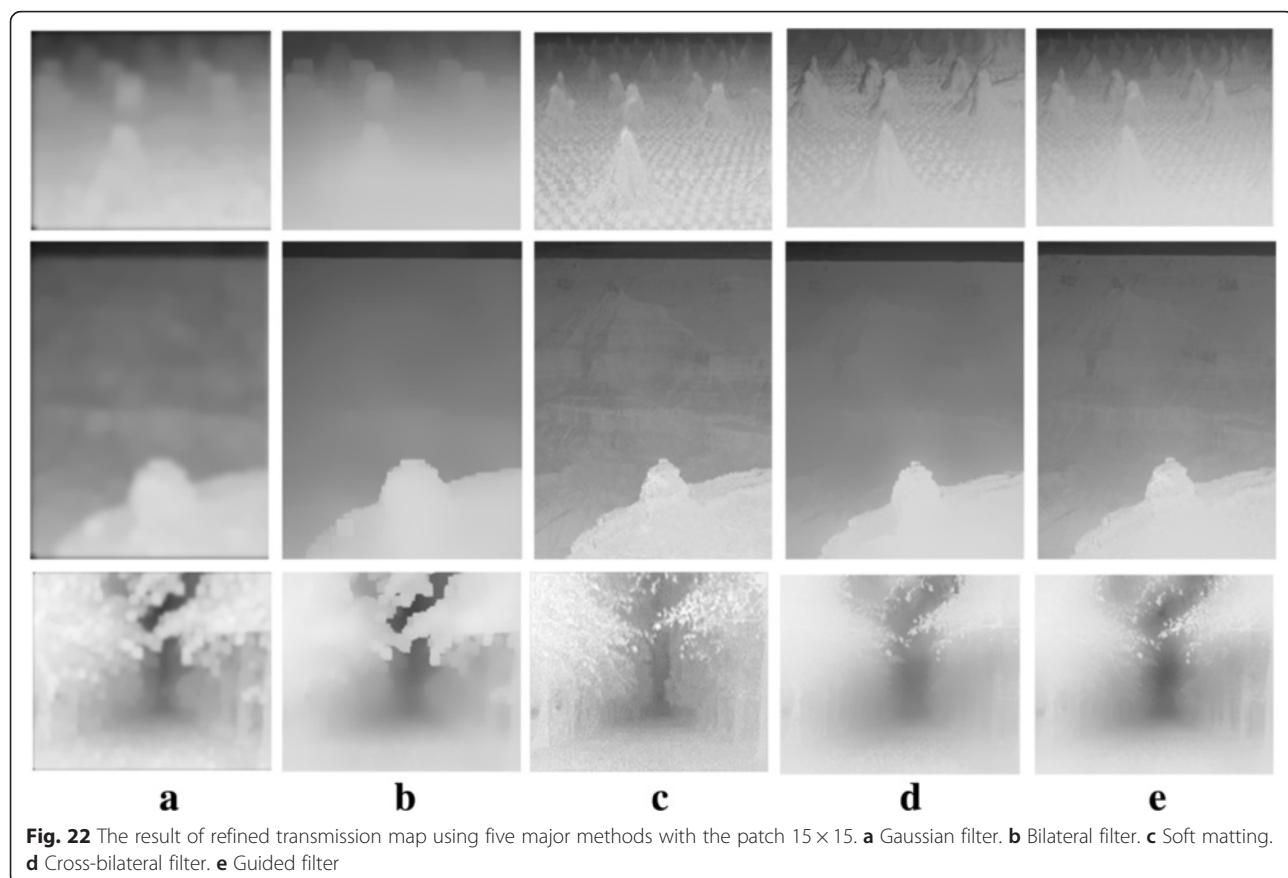
In the second approach, the transmission map enhancement can be achieved by applying a preprocessing filter to the hazy image. In [32], the total variation based image restoration and morphological filtering are applied to the hazy image, which can prevent producing unnecessary texture details from the estimated transmission map. In [34], an edge-enhanced hazy image is used as a guidance image at the guided filtering step to reconstruct the transmission map with sharp edges.

The third approach is to estimate the transmission map not from rectangular patches but from segments. In [31], the watershed segmentation is performed to extract regions that the transmission can be reliably estimated. In [35], a gray-level thresholding is performed to divide an image into sky and non-sky regions and transmission maps are then separately estimated for the two regions. Since blurry transmission maps are originated from rectangular patch-wise processing in Eq. (9), these segmentation-based methods tend to produce sharp transmission maps without further refinement.

1.3.4.7 Comparisons In the above subsections, the transmission map refinement schemes were described individually. The parameter sensitivity of each method was also discussed in detail. We then empirically tuned the best parameter(s) for each method as shown in Table 5 and compared the performance of the methods. Figure 22 shows some refinement results of the five methods for the same transmission maps. As can be seen, the methods that use

Table 5 Parameters used for the performance comparison

Common		Transmission map refinement	
Patch size	15×15	Gaussian	$\sigma_s = 5$
p%	0.1	Bilateral	$\sigma_s = 15, \sigma_r = 0.1$
Selection criterion of A	Highest intensity	Soft matting	$\lambda = 10^{-4}$
W_0	0.9	Cross-bilateral	$\sigma_s = 15, \sigma_r = 0.1$
t_0	0.1	Guided filter	$\varepsilon = 0.01$



the hazy image as a cross channel (i.e., soft matting, cross-bilateral filter, and guided filter) provide sharper transmission maps than the methods that do not use the hazy image (i.e., Gaussian and bilateral filters).

Quantitative quality evaluation is also possible because the ground-truth transmission map of the FRIDA can be used as the common reference frame. Table 6 compares the RMSE values obtained by the five methods. The soft matting performed the best, and the cross-bilateral and guided filters showed comparable second-best performance.

In addition, we measured the processing time required for transmission map refinement methods as shown in Table 7. A PC with Windows 8, 3.60 GHz CPU, 8 RAM, and MATLAB 2014(a) was used for the evaluation. The memory requirement was also measured using the peak and total memory [49]. The results indicate that the filter-based methods such as bilateral and cross-bilateral

filters are memory-efficient. The guided filter is the most memory-inefficient, but its time complexity is low compared to other methods.

1.3.5 Dehazed image construction

After estimating the atmospheric light \hat{A} and transmission map \hat{t} , the dehazed image J can be readily obtained from the degradation model as Eq. (6). Specifically, J is given as

$$J(x) = \frac{I(x) - \hat{A}}{\max(\hat{t}(x), t_0)} + \hat{A}, \quad (28)$$

where t_0 is a typical value for avoiding a low value of the denominator. Most DCP-based dehazing methods used t_0 as 0.1 [11–14, 20, 21, 25–27]. Figure 23 shows the dehazed images obtained using the top three transmission map refinement methods. As can be seen, the reconstruction of J by Eq. (28) can yield visually pleasant dehazed images.

When the hazy image contains significant color distortion by abnormal climate such as sandstorm [12], the estimated atmospheric light \hat{A} becomes far from achromatic, and thus, color correction is required at the dehazed

Table 6 Comparison of the RMSE values obtained by the five transmission map refinement methods. The patch sizes set to 15×15

RMSE of transmission map				
Gaussian	Bilateral	Soft matting	Cross-bilateral	Guided filter
0.2109	0.2057	0.1826	0.1971	0.1969

Table 7 Comparison of transmission map refinement methods with respect to the time complexity and memory requirements

Image	Resolution	Time (s)				Total/peak memory(Mb)			
		Ga	Bi	Cr	Gu	Ga	Bi	Cr	Gu
Fig. 24 (1)	600 × 400	4.358	9.900	20.257	2.706	74.713/36.703	76.594/38.619	76.684/38.649	625.209/70.992
Fig. 24 (2)	600 × 525	5.444	12.643	25.737	3.244	94.8314/48.225	97.440/50.761	97.407/50.761	797.781/85.364
Fig. 24 (3)	800 × 457	6.431	14.274	29.088	3.758	132.413/64.056	135.362/67.004	135.495/67.004	963.107/107.111
Fig. 24 (4)	450 × 600	4.715	11.558	22.825	2.908	82.739/42.672	84.963/44.859	85.796/45.286	687.942/74.707
FRIDA	640 × 480	5.167	11.833	24.308	3.142	92.797/47.289	95.290/49.768	95.290/49.767	780.075/83.565

Ga Gaussian, Bi bilateral filter, Cr cross-bilateral filter, Gu guided filter

image reconstruction. In such a case, J is obtained as follows:

$$J^c(x) = \frac{I^c(x) - (\hat{A}^c - d^c)}{\max(\hat{t}(x), t_0)} + (\hat{A}^c - d^c), \quad (29)$$

where the upper-script c represents the color channel, $c \in \{r, g, b\}$, and d^c denotes the difference between the average values of the red and c channels of I . In other words, the offset in the red channel caused by sandstorm is subtracted before the construction of the dehazed image. Figure 24b, c shows the dehazed images obtained by using the same refined transmission map as shown in Fig. 22e but with Eqs. (28) and (29), respectively. The experimental results demonstrate the necessity of the color correction at the dehazed image construction stage. Equation (29) can also be easily extended to the images that appeared greenish or bluish due to other abnormal weather conditions or improper camera parameter settings. There are also several works considering the noise amplification problem during dehazed image

construction [29, 35]. In addition, to obtain high contrast dehazed images, some image processing techniques can be applied including as linear stretching [30], gamma correction [32], and histogram specification [33].

Finally, Fig. 25 shows the time consumption of each dehazing step. Specifically, using the same experimental condition mentioned in Section 1.3.4, the average processing time of the 30 FRIDA test images was measured. The transmission map refinement step required the longest time when the bilateral and cross-bilateral filters were used, and the dark channel construction and transmission map estimation steps also required non-negligible time due to the block-min process in Eqs. (4) and (9).

1.4 Performance evaluation methods

In Section 1.3, we reviewed the conventional DCP-based dehazing algorithms by dividing them into subcomponents and discussing various methods used in each sub-component. Finally, we need to objectively evaluate the quality of the dehazed images. In this section, we first

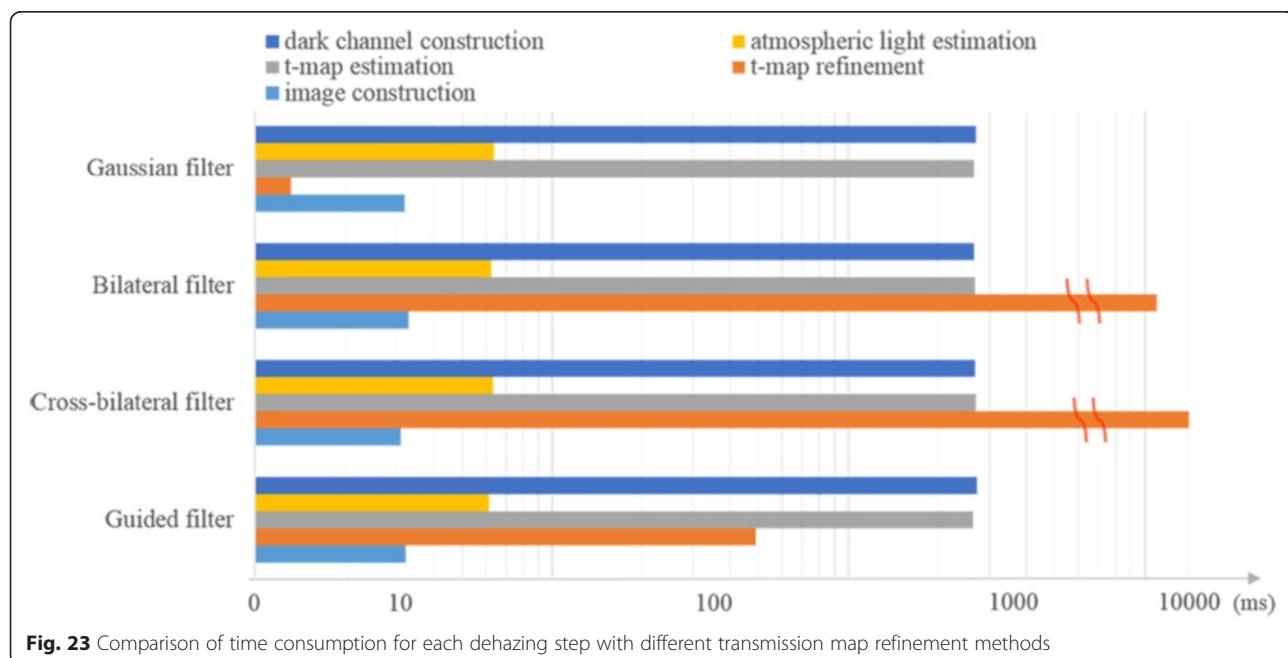


Fig. 23 Comparison of time consumption for each dehazing step with different transmission map refinement methods

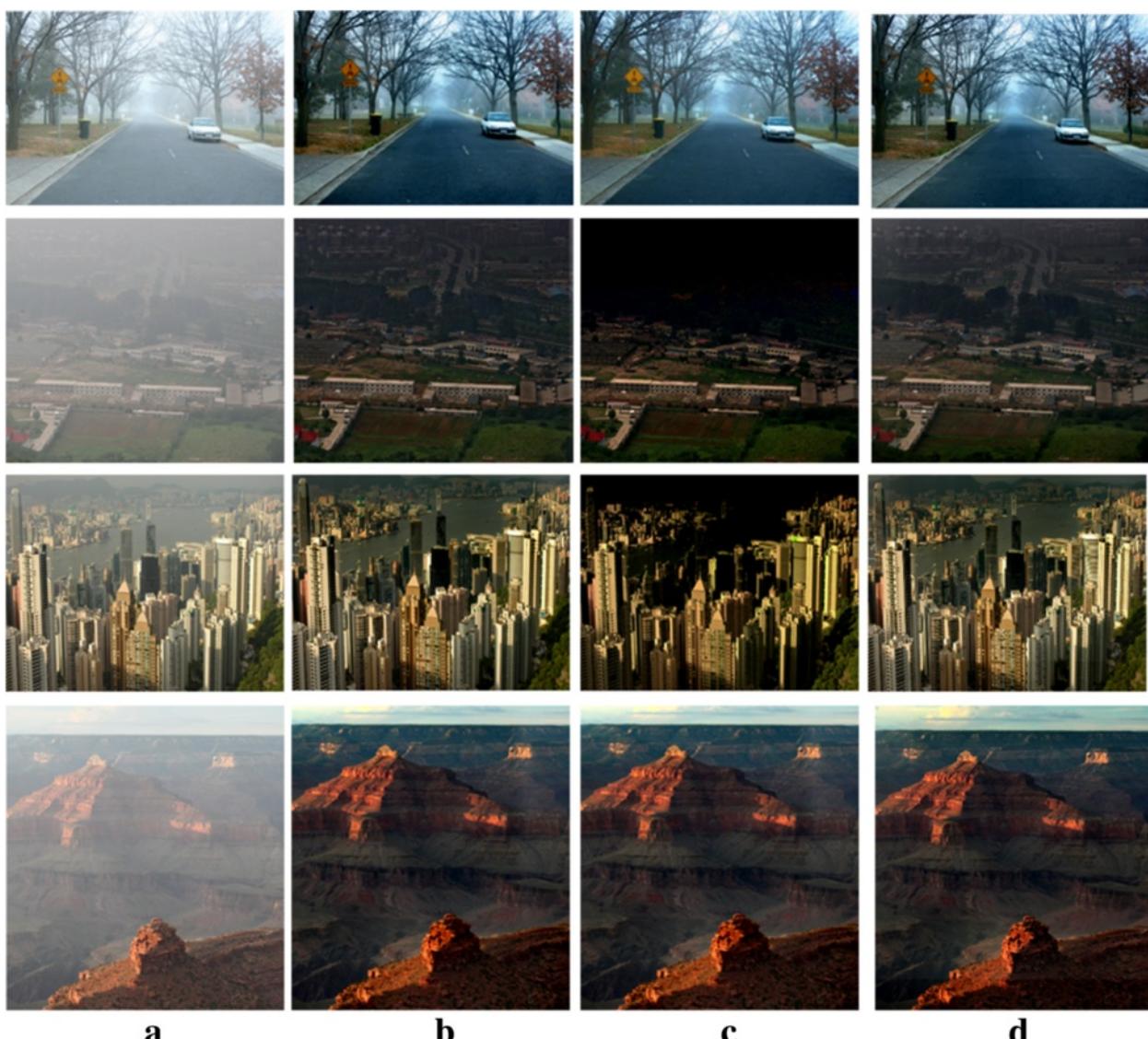


Fig. 24 The image dehazing results when the transmission maps as shown in Fig. 22 are used. **a** Hazy images. **b** Dehazed image using Fig. 22d. **c** Dehazed image using Fig. 22c. **d** Dehazed image using Fig. 22e

study the existing metrics developed for evaluating the quality of dehazed images.

Table 8 lists the metrics used for evaluating the quality of dehazed images. The most widely used metric is the ratio of visible edges between dehazed and hazy images (denoted as Q_e) [23, 42, 50, 51]. Since the dehazed image tends to have sharper details than the hazy image, it is considered that the higher the Q_e value the better the dehazed image. In order to more precisely measure the local image sharpness, the ratio of visible edges' gradients between the dehazed and hazy images (denoted as Q_g) is also evaluated [23, 42, 50, 51]. In a similar manner, the higher the Q_g value, the better the dehazed image. In [38, 50, 51], the percentage of pixels which becomes

completely black or completely white after dehazing (denoted as Q_o) is measured. As Q_o accounts for the over-enhancement, the smaller the Q_o value, the better the dehazed image. Other quality metrics developed for general image restoration problems such as image entropy [23] and Q-metric [27] are often directly used to evaluate the quality of dehazed images, which are not discussed in this section.

One problem is that the reliability of the aforementioned metrics has not been verified yet. As the quality of the dehazed image is strongly dependent on the accuracy of the transmission map, we relate the RMSE (between the ground-truth and estimated transmission maps) and the quality metrics of image dehazing. Figure 26 compares the

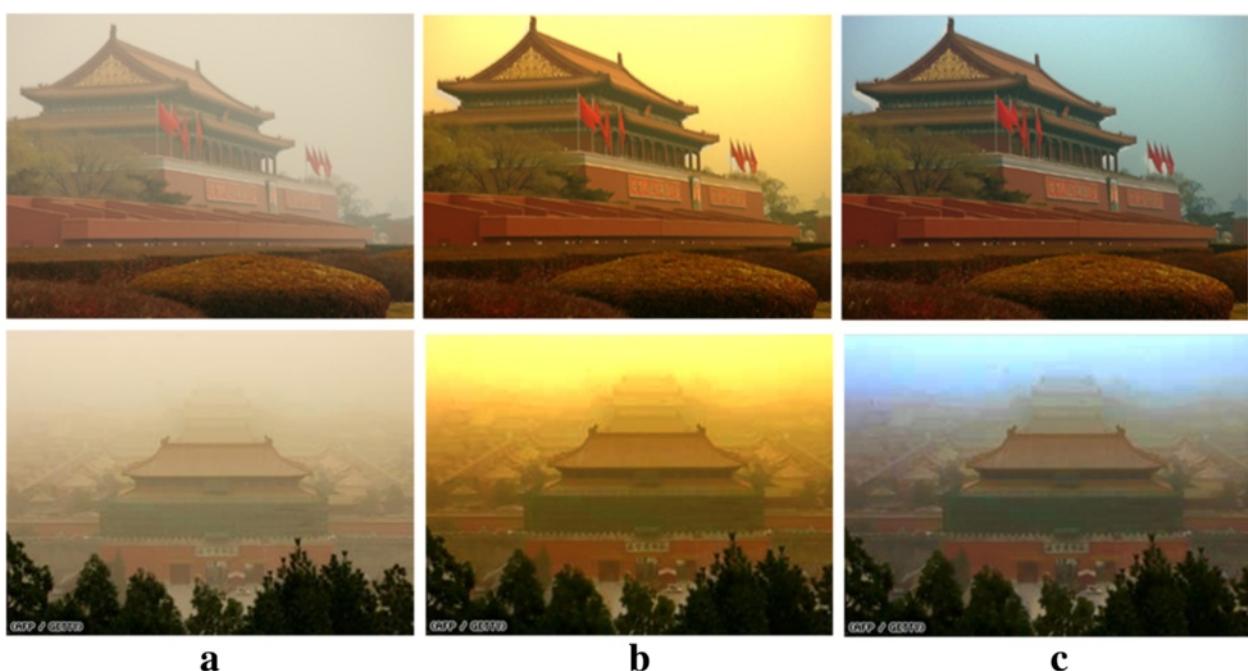


Fig. 25 Image dehazing result for the image captured under abnormal weather condition. **a** Hazy images. **b** Dehazed image using Eq. (28). **c** Dehazed image using Eq. (29)

RMSE and quality metrics, where the red curves denote the fitted functions. Each point indicates the result for various haze density ($\beta \in [0.005, 0.015]$). As can be seen, a general tendency of the quality metrics is consistent with their definitions (i.e., the RMSE value tends to decrease as Q_e and Q_g increases and vice versa with respect to Q_o).

Figure 27 shows the case when Q_e and Q_g are not trustworthy. As can be seen in Fig. 27b, d, some false positive edges are detected and they tend to unnecessarily increase Q_e and Q_g values. Therefore, the dehazed images obtained using the Gaussian filter have even higher Q_e and Q_g values than those obtained using the soft matting (in Fig. 26, Gaussian filter: $Q_e = 1.7311$, $Q_g = 1.1073$; soft matting: $Q_e = 1.1675$, $Q_g = 0.8774$). Therefore, Q_e and Q_g should be used considering the characteristics of the dehazed algorithms. More dedicated quality evaluation methods need to be developed for image dehazing.

Table 8 Quality metrics developed for evaluating the quality of dehazed images

Reference	Metric
[23, 42, 50, 51]	The ratio of visible edges between input and output images (Q_e), the ratio of visible edges' gradients between input and output images (Q_g)
[38, 50, 51]	Q_e , Q_g , percentage of pixels which becomes completely black or completely white after dehazing (Q_o)

Lastly, an application-specific quality metric of image dehazing is also presented [52]. When image dehazing is developed for computer vision applications, it is expected that the dehazed image results in the performance enhancement of computer vision tasks such as object detection and recognition. Since detection and matching of feature points play an important role for such computer vision tasks, the numbers of matched feature points are compared between hazy and dehazed image pairs [52]. It is then assumed that the more the matched feature points, the better the image dehazing algorithm. We believe that other application-specific quality metrics can be devised in a similar manner.

1.5 Summary

In this paper, we performed an in-depth survey on DCP-based image dehazing methods. Especially, we classified relevant research articles related to the DCP according to the four steps and performed a step-by-step analysis. Our findings can be summarized as follows.

- *Dark channel construction:* the local patch size is a very important parameter for dark channel construction. Color textures are transferred to the dark channel when a small local patch is used, whereas blurry dark channels are obtained when a large local patch is used. In addition, a physically

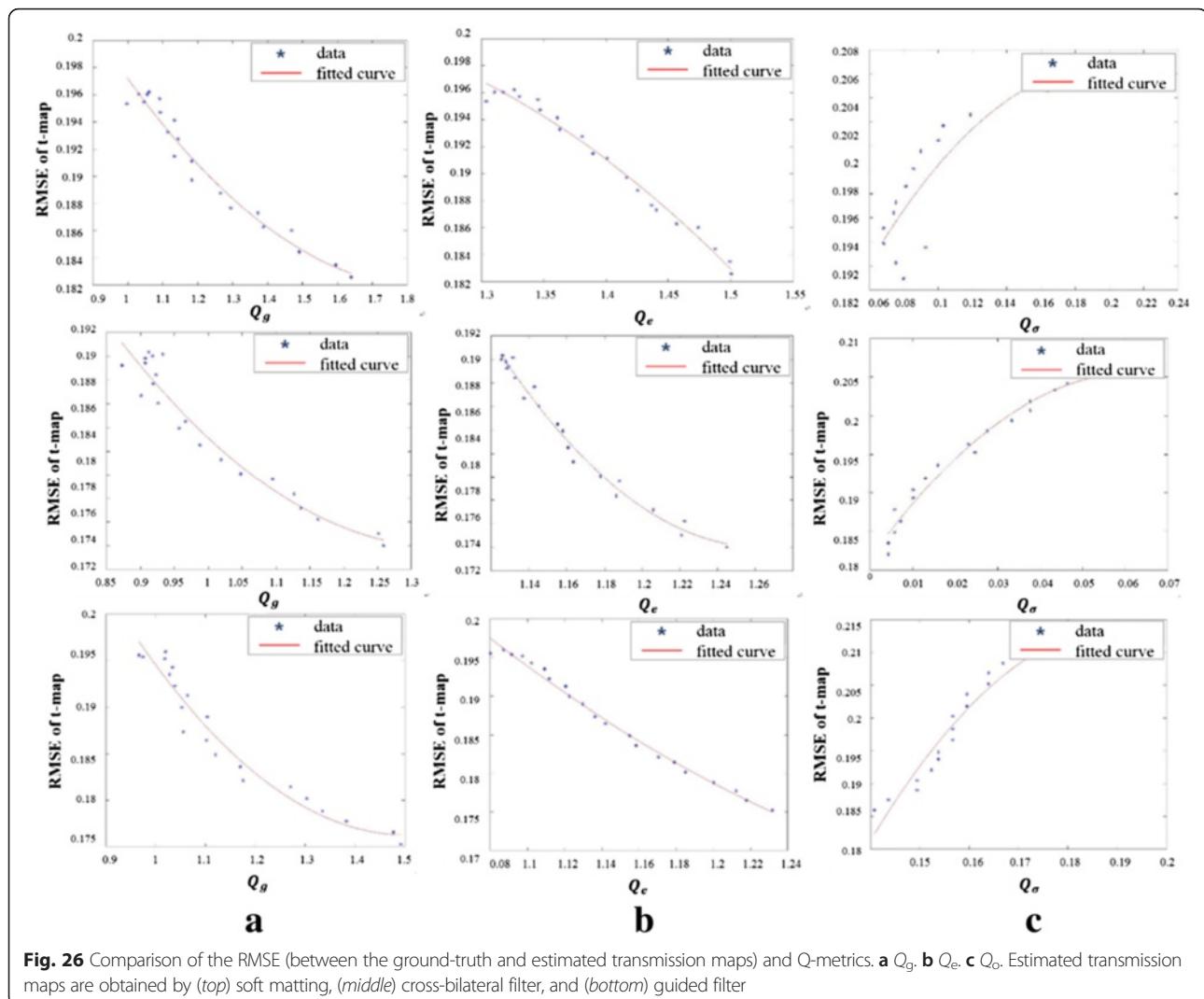


Fig. 26 Comparison of the RMSE (between the ground-truth and estimated transmission maps) and Q-metrics. **a** Q_g , **b** Q_e , **c** Q_σ . Estimated transmission maps are obtained by (top) soft matting, (middle) cross-bilateral filter, and (bottom) guided filter

less meaningful median filter is found to be not very effective in dark channel construction.

- *Atmospheric light estimation:* the atmospheric light is reliably estimated from the dark channel, especially when the dark channel is obtained using a large local patch. Therefore, if the local patch size used in dark channel construction is not large enough, it is recommended to use an additional dark channel with a larger local patch size only for atmospheric light estimation. The use of local entropy is also found to be effective in enhancing the estimation accuracy because atmospheric light estimation from bright objects can be prevented.
- *Transmission map estimation:* the under-estimation problem of the transmission map is addressed. The conventional gain and offset control methods are examined, but an adaptive correction scheme is found to be necessary for precise estimation of the

transmission map, which is missing in the current literature.

- *Transmission map refinement:* the performance of transmission map refinement is improved when a hazy image is used as a guidance image. The soft matting method shows the best transmission map estimation accuracy, and the guided and cross-bilateral filters show the second-best accuracy. The Gaussian and guided filters perform best in terms of the computational complexity, but the guided filter is most memory-inefficient among the five investigated refinement schemes.
- *Quality metric for image dehazing:* the performance of the image dehazing can be indirectly measured by comparing the ground-truth and estimated transmission maps. The conventional quantitative quality metrics using only the dehazed image are investigated, but they are found to be not trustworthy

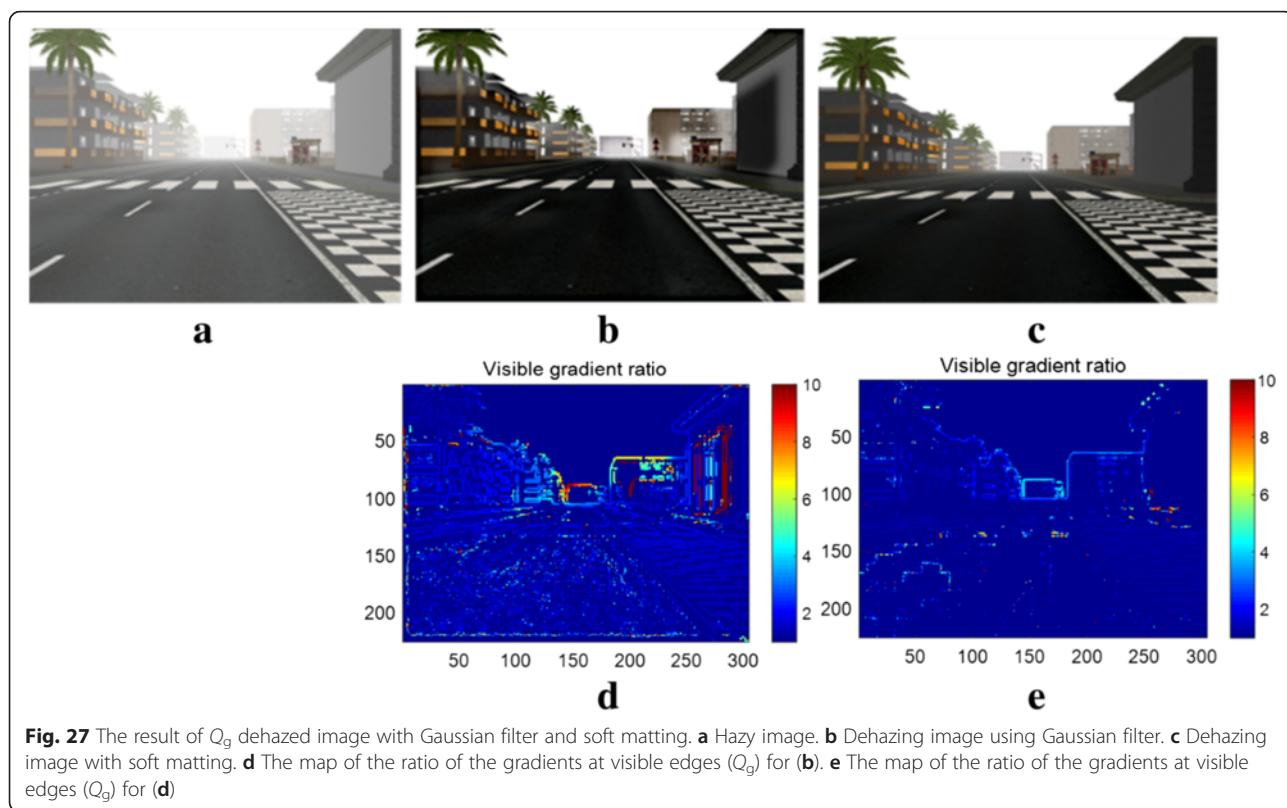


Fig. 27 The result of Q_g dehazed image with Gaussian filter and soft matting. **a** Hazy image. **b** Dehazing image using Gaussian filter. **c** Dehazing image with soft matting. **d** The map of the ratio of the gradients at visible edges (Q_g) for (b). **e** The map of the ratio of the gradients at visible edges (Q_g) for (d)

enough. An advanced or application-specific quality metric needs to be developed.

2 Conclusions

In this paper, we performed an in-depth study on one of the most successful dehazing algorithms: the DCP-based image dehazing algorithm. Considering the four major steps of the DCP-based image dehazing, which are atmospheric light estimation, transmission map estimation, transmission map refinement, and image reconstruction, we classified recent research articles related to the DCP according to these four steps and performed a step-by-step analysis of conventional methods. Moreover, the conventional methods developed for evaluating the performance of image dehazing were also summarized and discussed. We believe that our detailed survey and experimental analysis will help readers understand the DCP-based dehazing methods and will facilitate development of advanced dehazing algorithms.

Abbreviations

DCP: dark channel prior; FRIDA: foggy road image database; RMSE: root-mean-square error.

Competing interests

The authors declare that they have no competing interests.

Acknowledgements

This research was supported by the Basic Science Research Program through the National Research Foundation of Korea(NRF) funded by the Ministry of Science, ICT and Future Planning (NRF-2014R1A1A2057970).

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Received: 24 June 2015 Accepted: 9 January 2016

Published online: 19 January 2016

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