

AI / ML / DL

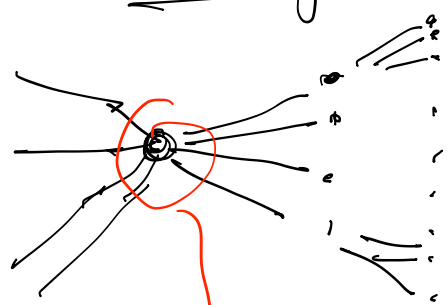
- SVM
- RFs
- DTs
- ...

ANN

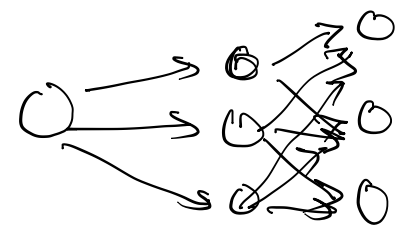
- Fully connected
- Convolutional NN
- RNNs
- GRUs
- ...

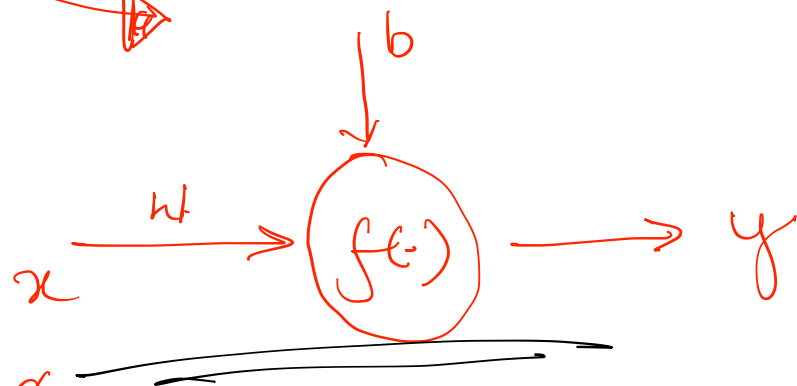
Basic element of ANN: Perceptron

biological neurons



||
Neuron





with b

$$y = f(wx)$$

$$\rightarrow y = f(wx + b)$$

$$[y = Mx + c] \quad (\text{if } f = I(\cdot))$$

$$y = f(wx + w_0 \cdot 1)$$

$$= f(\underline{w}^T \underline{x})$$

column vectors.

$$= f\left(\begin{bmatrix} w & w_0 \end{bmatrix} \begin{bmatrix} x \\ 1 \end{bmatrix}\right)$$

$f \equiv$ activation fn. \Rightarrow Introducing
non linearity

$$y = wx + b$$

✓ lin. eqn.
 Linear system? No

System.
 $y = f(x)$

Homogeneity ✓

$$y_1 = f(x_1)$$

$$y_2 = f(x_2)$$

$$x_2 = a \cdot x_1$$

$$\text{if } y_2 = a \cdot y_1$$

Superposition ✓

$$y_1 = f(x_1)$$

$$y_2 = f(x_2)$$

$$x_3 = x_1 + x_2$$

$$\begin{aligned} y_3 &= y_1 + y_2 = f(x_1) + f(x_2) \\ &= f(x_1 + x_2) \\ &= f(x_3) \end{aligned}$$

$$y = wx + b$$

$$y_2 \neq a \cdot y_1$$

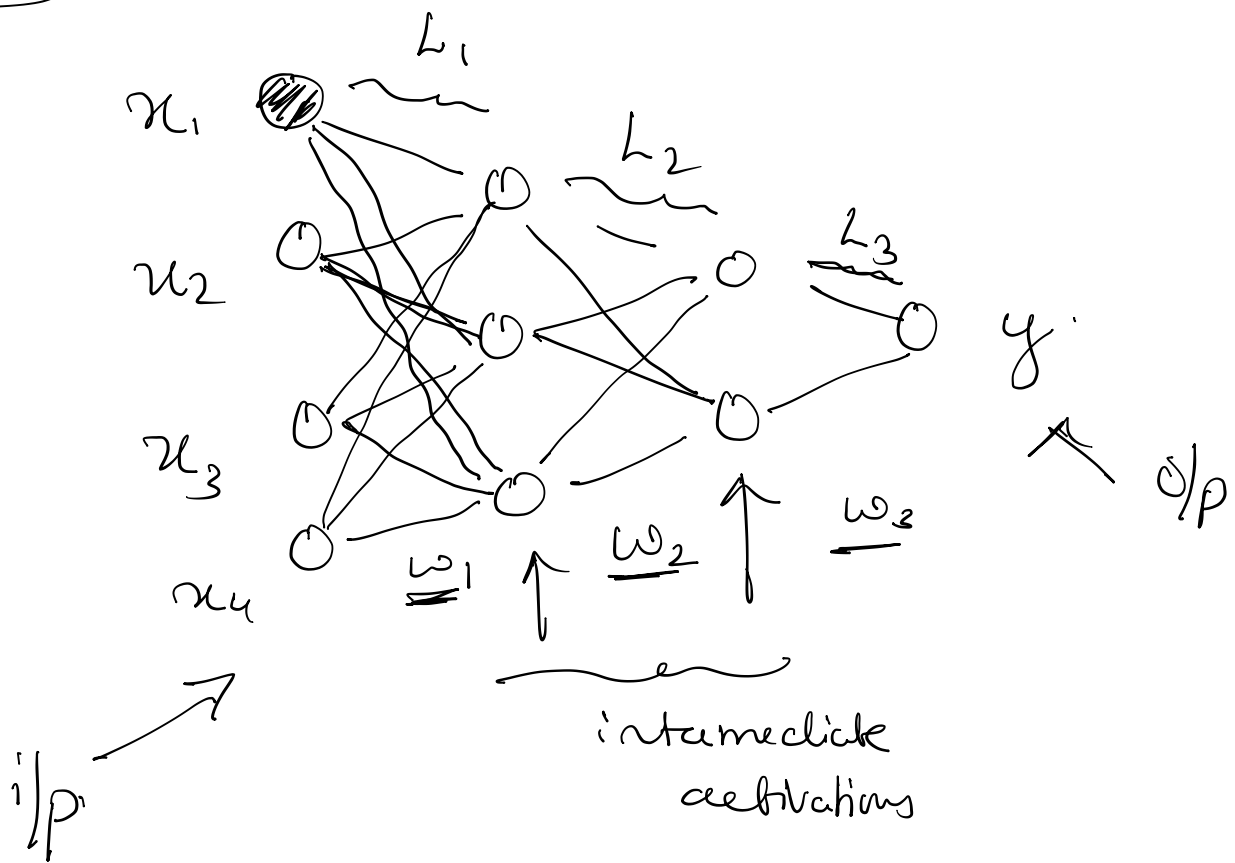
$$y_3 \neq y_1 + y_2$$

\hookrightarrow due to bias term

① Activation fn "f" \rightarrow makes y a non-linear cm.
 \rightarrow makes \hat{y} as non-linear system.

② bias term 'b' \rightarrow makes \hat{y} as non-linear system.

MLP:-

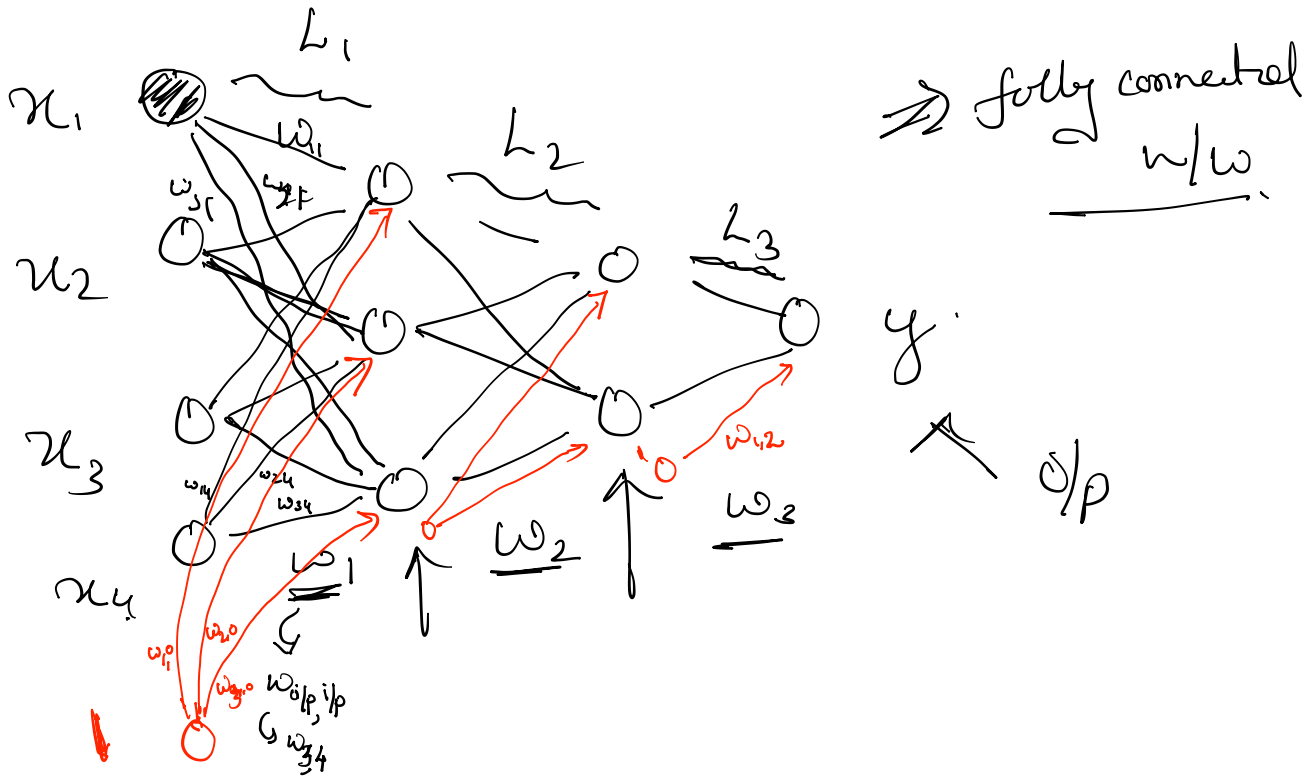


$$\underline{\underline{\omega}} = \begin{bmatrix} \underline{\omega}_1 & \underline{\omega}_2 & \underline{\omega}_3 \end{bmatrix}$$

$$y = \underline{\underline{\omega}}^T x$$

$$X = [x_1 \ x_2 \ x_3 \ x_4]^T$$

parameters \Rightarrow Model



w/o bias

L_1			L_2			L_3		
i/p	o/p	w_1	i/p	o/p	w_2	i/p	o/p	w_3
4	3	12	3	2	6	2	1	2
4	3	$4 \times 3 + 3 = 15$	3	2	$3 \times 2 + 2 = 8$	2	1	$2 \times 1 + 1 = 3$

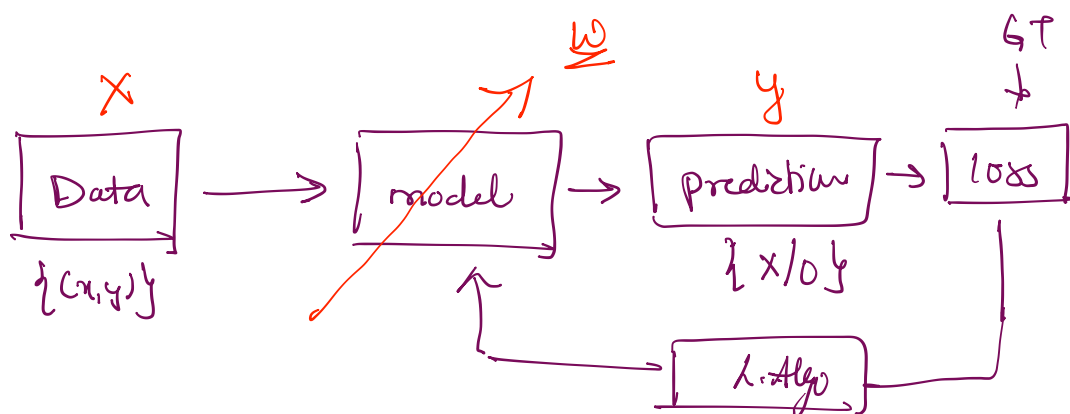
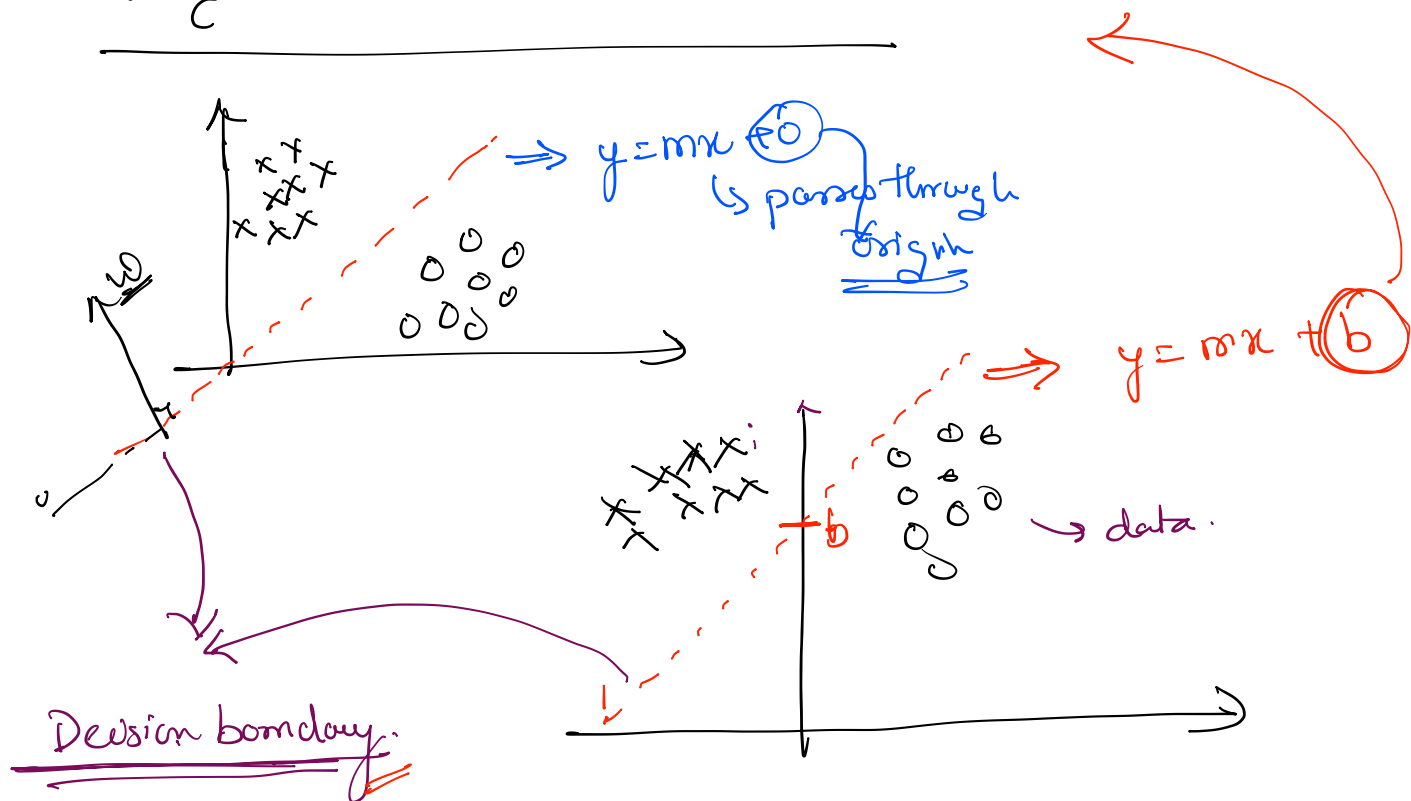
with bias

$$12 + 6 + 2 = \underline{\underline{20}}$$

$$15 + 8 + 3 = \underline{\underline{26}}$$

→ # parameters for an Act. fⁿ $\geq \underline{0}$.

why do we need bias term?



$$y = \underline{w^T x}$$

(x, y) on the line
 $y = 0$

How is w related to decision boundary

$$w^T x = 0$$

$w \perp$ decision boundary