

# Perceptron

AND/OR  
Gate

Binary

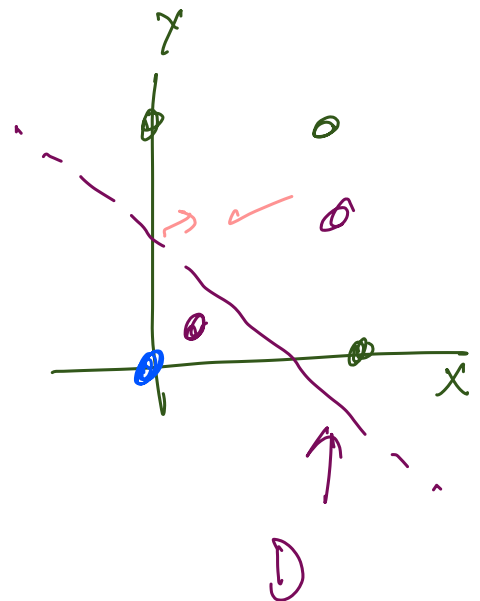
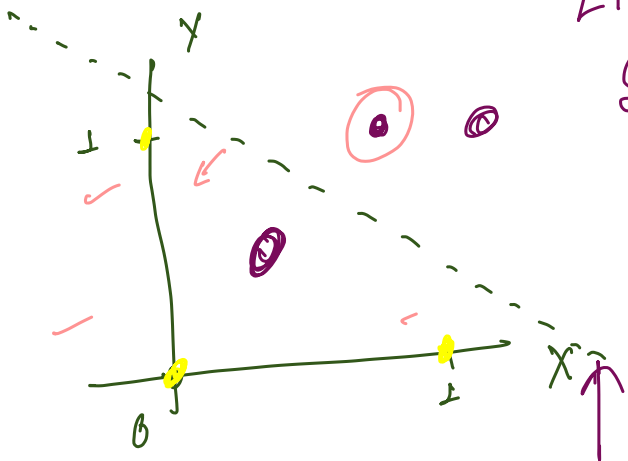
AND

$x_1$	$x_2$	$y$
0	0	0 ✓
0	1	0 ✓
1	0	0 ✓
1	1	1 ✓

OR

$x_1$	$x_2$	$y$
0	0	0 ✓
0	1	1 ✓
1	0	1 ✓
1	1	1 ✓

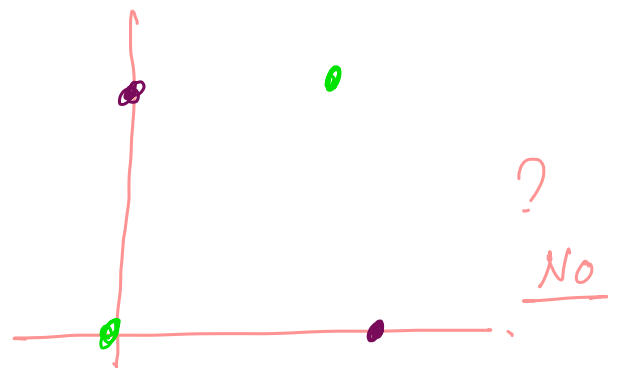
Linearly  
Separable



DS Decision  
Surface

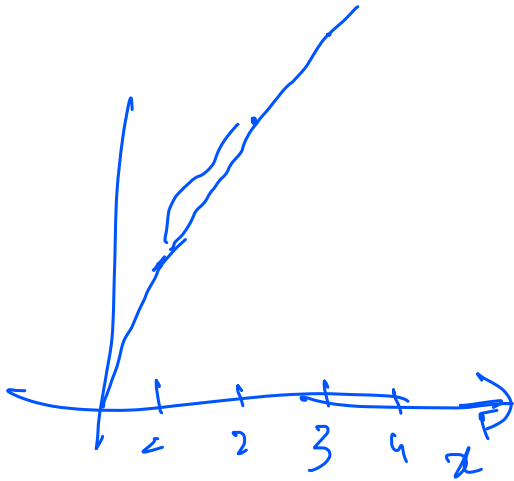
XOR

$x_1$	$x_2$	$y$
0	0	0 ✓
0	1	1 ✓
1	0	1 ✓
1	1	0 ✓



Can we have a linear  
decision surface?

$$\underline{y=2x} \quad y=6x \quad \checkmark$$



x	-1	2	3	5
y	-2	4	6	10

x	1	2	3	4	5
y	6	12	18	24	30

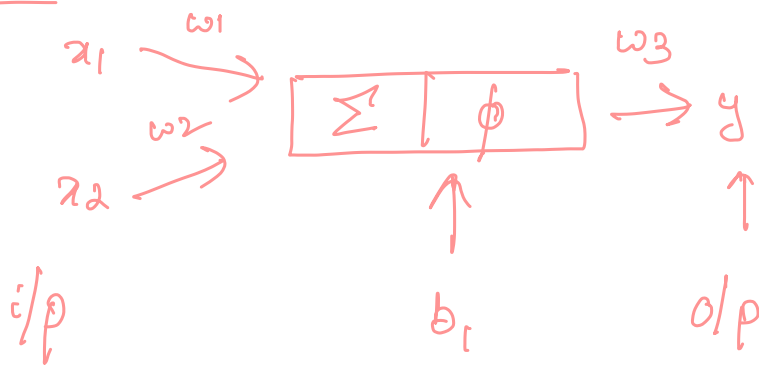
As we increase the value of  $x$ , the value of  $y$  expands linearly.

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$$\underline{y = 6x + c}$$

linear or non-linearly?  
Plot the graph.

# Single Perceptron



$\Sigma$  = weighted average

$\phi \rightarrow$  Transfer function (TF)

$$\omega_3 \leftarrow \phi(x_1 \omega_1 + x_2 \omega_2 + b)$$

If TF was not there &  $b=0$  then

$$\omega_3 \leftarrow x_1 \omega_1 + x_2 \omega_2$$

let  $\omega_2 = 0$

$$\boxed{\omega_3 \leftarrow x_1 \omega_1}$$

To intro non-linearity  $\rightarrow$  transfer function has been used

also bias.

AI  $\rightarrow$  ML  $\rightarrow$  NN  $\rightarrow$  DL

AI - Artificial Intelligence

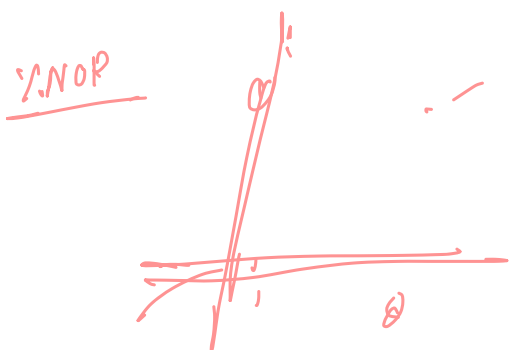
ML  $\rightarrow$  Machine Learning

NN  $\rightarrow$  Neural Net

DL  $\rightarrow$  Deep Learning

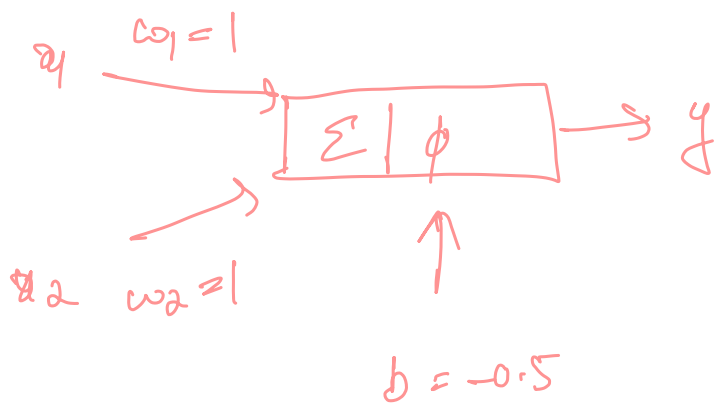
$$p = x_1 \omega_1 + x_2 \omega_2 + b$$

$$\phi(p) = \begin{cases} 0 & \Sigma x \omega + b \geq 0 \\ 1 & \text{otherwise} \end{cases}$$



Non-linearity

# Perceptron OR



$x_1$	$x_2$	$y$
0	0	0 ✓
0	1	1 ✓
1	0	1 ✓
1	1	1 ✓

1st case

$$x_1 = 0 \quad x_2 = 0$$

$$P = \frac{x_1 w_1 + x_2 w_2 + b}{0}$$

$$= -0.5 \leq 0$$

$$= 0 \quad \checkmark$$

$$y = \begin{cases} 0 & \text{if } w \cdot a + b \leq 0 \\ 1 & \text{otherwise} \end{cases}$$

3rd

$$x_1 = 1 \quad x_2 = 0$$

$$P = 1 \times 1 + -0.5$$

$$= 0.5 > 0$$

$$= 1$$

2nd

$$x_1 = 0 \quad x_2 = 1$$

$$P = x_1 w_1 + x_2 w_2 + b$$

$$= 1 \times 1 - 0.5$$

$$= 0.5 > 0$$

$$= 1$$

4th

$$x_1 = 1 \quad x_2 = 1$$

$$P = 1 \times 1 + 1 \times 1 - 0.5$$

$$= 1.5 > 0$$

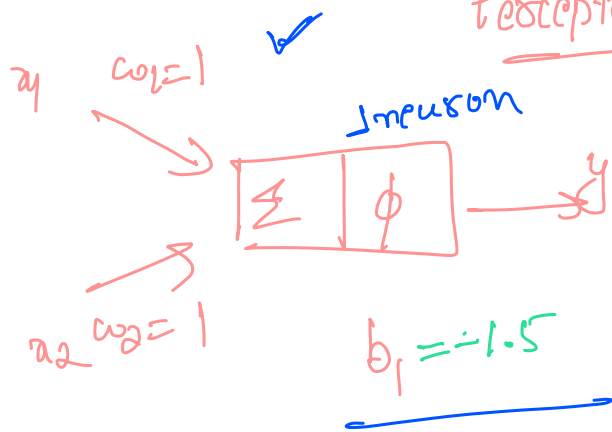
$$= 1$$

$$\boxed{w_1 = w_1 + \Delta w_1} \rightarrow \text{zero}$$

$$w_1 = \eta (y - \hat{y}) x_1$$

$\rightarrow \text{zero}$

# Perceptron ANN



$x_1$	$x_2$	$y$
0	0	0 ✓
0	1	0 ✓
1	0	1 ✓
1	1	1 ✓

$$\phi = \begin{cases} 0 & \text{if } w \cdot x + b \leq 0 \\ 1 & \text{otherwise} \end{cases}$$

1st case

$$x_1 = 0 \quad x_2 = 0$$

$$\begin{aligned} \phi(p) &= \phi(x_1 w_1 + x_2 w_2 + b_1) \\ &= \phi(-1.5) \leq 0 \\ &= 0 \end{aligned}$$

3rd case

$$x_1 = 1 \quad x_2 = 0$$

$$\begin{aligned} \phi(p) &= \phi(x_1 w_1 + x_2 w_2 + b_1) \\ &= \phi(-0.5) \leq 0 \\ &= 0 \end{aligned}$$

2nd

$$x_1 = 0 \quad x_2 = 1$$

$$\begin{aligned} \phi(p) &= \phi(x_1 w_1 + x_2 w_2 + b_1) \\ &= \phi(0 \times 1 + 1 \times 1 + (-1.5)) \\ &= \phi(-0.5) \leq 0 \\ &= 0 \end{aligned}$$

4th

$$x_1 = 1 \quad x_2 = 1$$

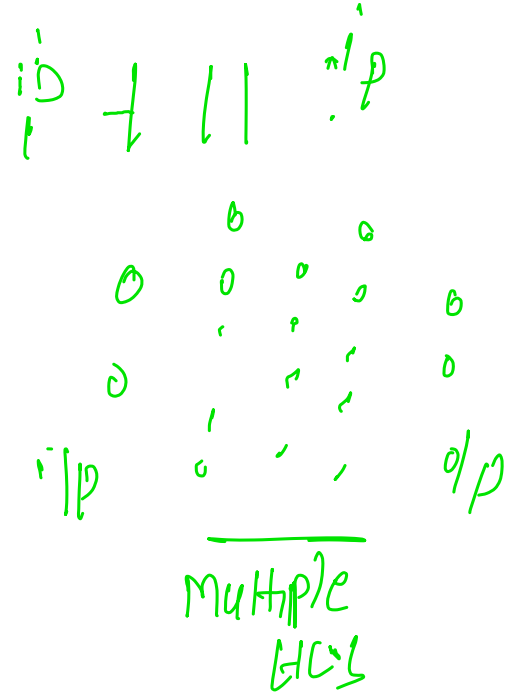
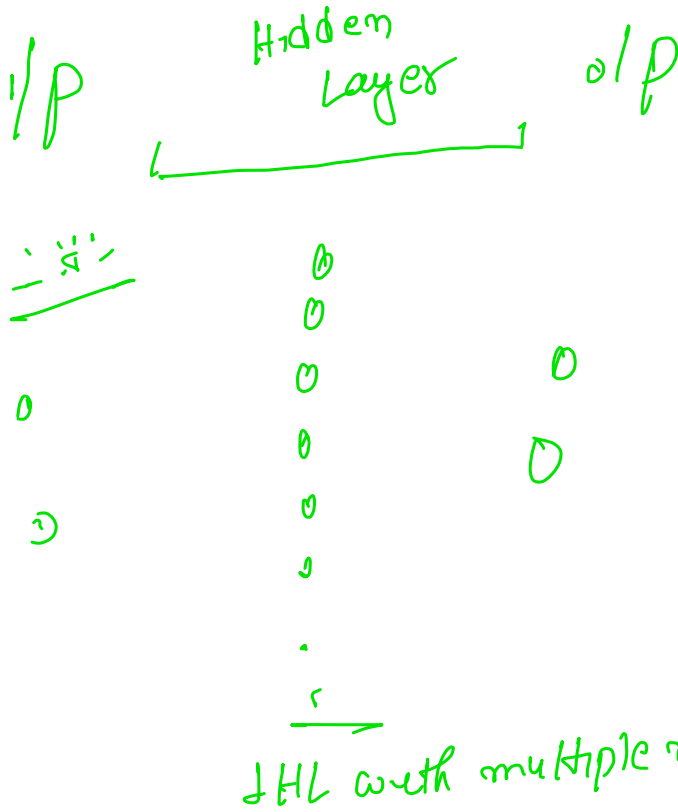
$$\begin{aligned} \phi(p) &= \phi(1 + 1 - 1.5) \\ &= \phi(0.5) > 0 \\ &= 1 \end{aligned}$$

XOR

1 single neuron is enough?

1 Hidden Layer

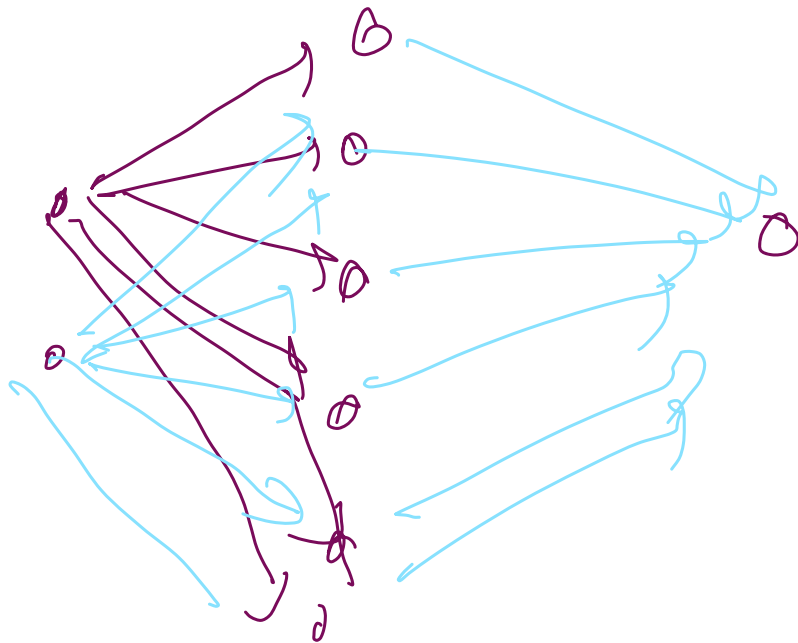
more than 1 'A'



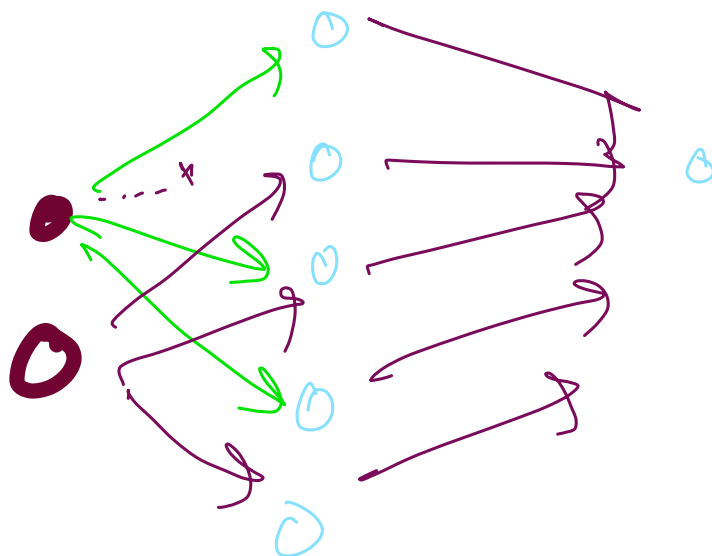
Fully Connected (FC)

↳ all neurons are connected to all other neurons

MPLP → Multi Layer Perceptron



FL



Not FC