

Mechanical Processing in Internally Coupled Ears

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Outline for Section 1

Introduction

Auditory Systems

Hearing Cues

The Model

Mouth Cavity

Acoustic Head Model
Pressure Derivation

Eardrum

Model

Membrane Vibrations

Coupled Membranes

Boundary Conditions

Evaluation

Vibration Amplitude

Directional Cues

Internal Level Difference
Internal Time Difference

Conclusion

Auditory Systems

Auditory Systems



Independent Ears

Eustachian tubes generally very narrow.

Effectively independent eardrum vibrations.



Coupled Ears

Wide eustachian tubes open into the mouth cavity.

Eardrums vibrations influence each other.

Hearing Cues

Binaural Hearing Cues

Localization using frequency dependent phase and amplitude differences between the ears.

Interaural Time Difference

Equivalent to phase difference between membrane vibrations.

Interaural Level Difference

Equivalent to amplitude difference between membrane vibrations.

Hearing Cues

Advantages of Coupled Ears

- ▶ Low frequencies result in reduced degradation of hearing cues in dense environments.

Outline for Section 2

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Boundary Conditions

Evaluation

Vibration Amplitude

Directional Cues

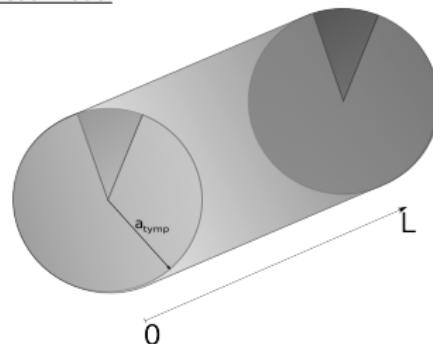
Internal Level Difference

Internal Time Difference

Conclusion

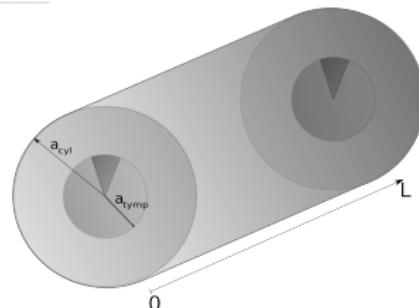
Mouth Cavity

Mouth Cavity

Previous Model

a_{tym} fixed.

$$V_{\text{cyl}} = \pi a_{\text{tym}}^2 L$$

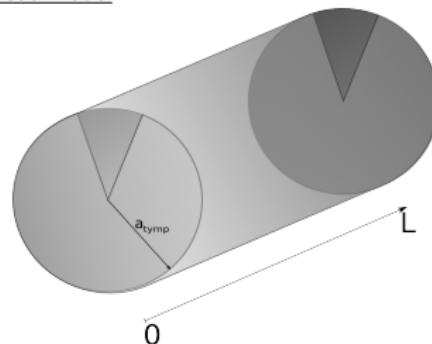
Our Model

a_{tym} , V_{cyl} fixed.

$$a_{\text{cyl}} = \sqrt{V_{\text{cyl}}/\pi L}$$

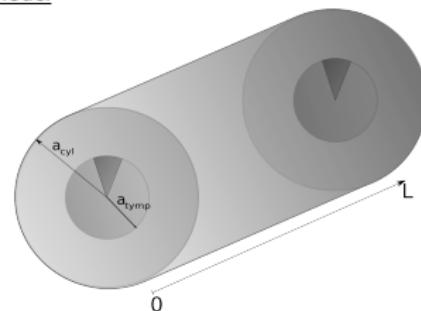
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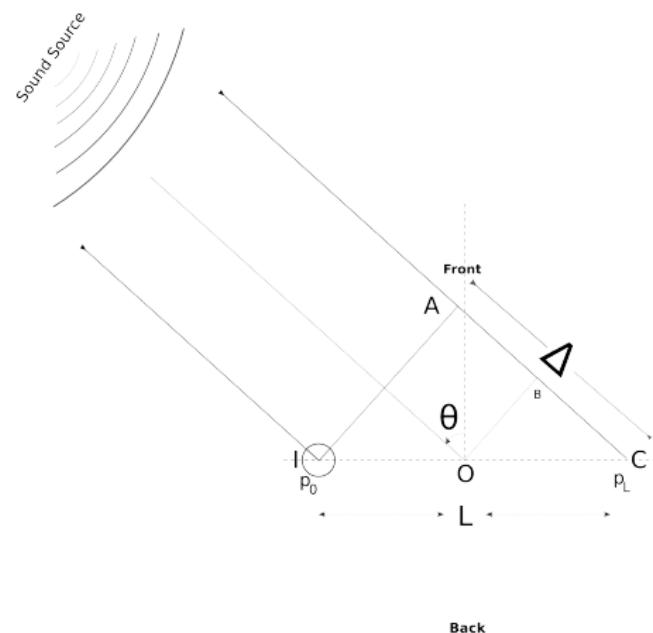
Mouth Cavity

Acoustic Head Model

- ▶ **I** - Ipsilateral ear, **C** - Contralateral ear.

p_0, p_L - sound pressure on eardrums, θ - sound source direction.

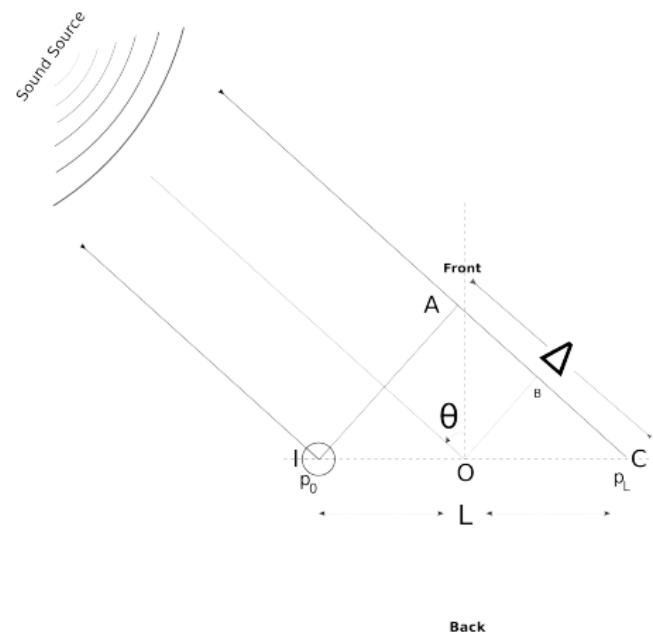
- ▶ Sound source "far away".
- ▶ No appreciable amplitude difference, $|p_0| = |p_L|$.
- ▶ Phase difference between sound at both ears - $\Delta = kL \sin \theta$.
- ▶ $p_0 = p e^{j\omega t - .5kL \sin \theta}$
 $p_L = p e^{j\omega t + .5kL \sin \theta}$



Mouth Cavity

Acoustic Head Model

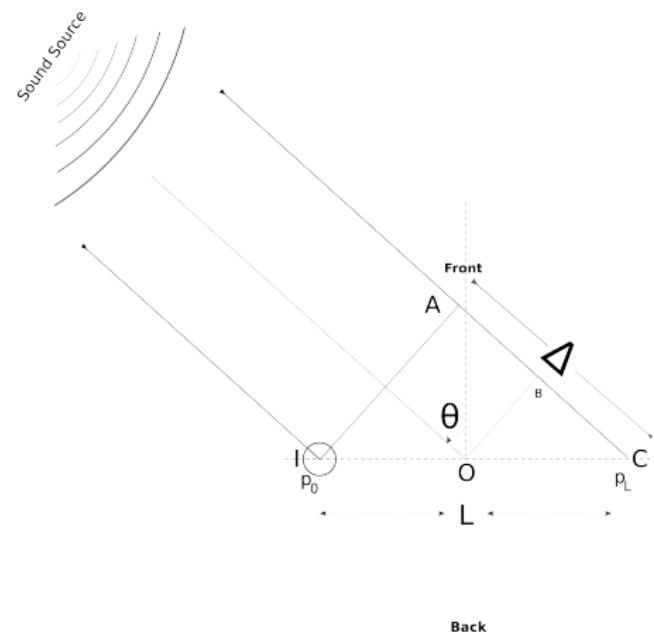
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Mouth Cavity

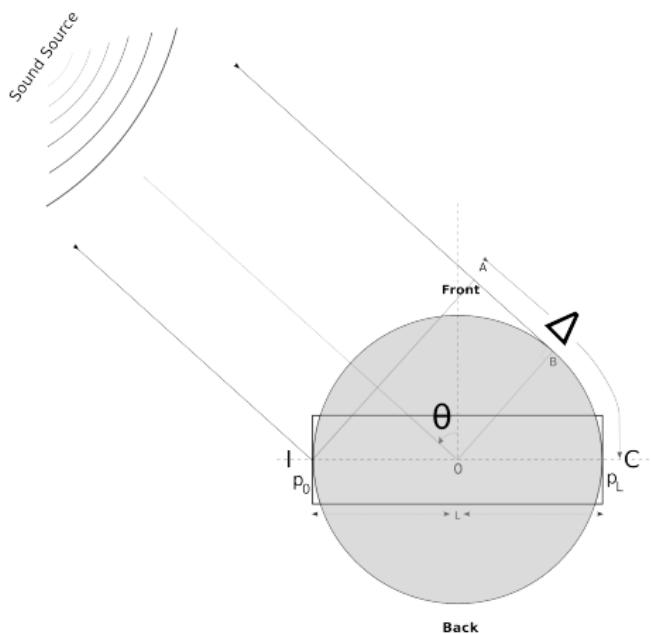
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Acoustic Head Model contd.

- ▶ $|p_0| = |p_L|$.
 - ▶ Increased phase difference due to diffraction - $\Delta = 1.5kL \sin \theta$.
 - ▶ $p_0 = p e^{j\omega t - .75kL \sin \theta}$
 $p_L = p e^{j\omega t + .75kL \sin \theta}$



Mouth Cavity

Cavity Pressure

3D Wave Equation

$$\frac{1}{c^2} \partial_t^2 p(x, r, \phi, t) = \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial p(x, r, \phi, t)}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 p(x, r, \phi, t)}{\partial \phi^2} + \frac{\partial p(x, r, \phi, t)}{\partial x^2} \quad (1)$$

To be solved using the separation ansatz

$$p(x, r, \phi, t) = f(x)g(r)h(\phi)e^{j\omega t}.$$

Separated Equations

x- and ϕ - directions

$$\frac{d^2 f(x)}{dx^2} + \zeta^2 f(x) = 0 \longrightarrow f(x) = e^{\pm j\zeta x} \quad (2)$$

$$\frac{d^2 h(\phi)}{d\phi^2} + q^2 h(\phi) = 0 \longrightarrow h(\phi) = e^{\pm jq\phi} \quad (3)$$

r-direction, Bessel functions

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial g(r)}{\partial r} \right) + \left[\nu^2 - \frac{q^2}{r^2} \right] g(r) = 0 \longrightarrow g(r) = J_q(\nu r) \quad (4)$$

$$\text{where, } \nu^2 = k^2 - \zeta^2$$



Mouth Cavity

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Boundary Conditions - ϕ

Smoothness and Continuity in ϕ .

$$\phi \rightarrow h(0) = h(2\pi) \quad \text{and} \quad h'(0) = h'(2\pi)$$

$$\Rightarrow h(\phi) = \cos q\phi, \quad q = 0, 1, 2, \dots \quad (5)$$

Boundary Conditions - r

Impenetrable boundary at $r = a_{\text{cyl}}$, i.e. normal derivative vanishes

$$-j\rho\omega \mathbf{v} = \mathbf{n} \cdot \nabla p(x, r, \phi; t) \Big|_{r=a_{\text{cyl}}} \equiv \frac{\partial g}{\partial r} \Big|_{r=a_{\text{cyl}}} = 0 \quad (6)$$

$$\Rightarrow g(r) = J_q(\nu_{qs} r / a_{\text{cyl}}) \quad (7)$$

Bessel Prime Zeros

- ▶ ν_{qs} - zeros of J'_q , $s = 0, 1, 2, \dots$
- ▶ $\nu_{00}=0$

Mouth Cavity

General Solution

Pressure Modes

$$p(x, r, \phi, t) = \sum_{q=0, s=0}^{\infty} \left[A_{qs} e^{j\zeta_{qs}x} + B_{qs} e^{-j\zeta_{qs}x} \right] p_{qs}(r, \phi) e^{j\omega t} \quad (8)$$

$$p_{qs}(r, \phi) = \cos q\phi J_q(\nu_{qs} r / a_{\text{cyl}}) \quad (9)$$

$$\text{where, } \zeta_{qs} = \sqrt{k^2 - \nu_{qs}^2 / a_{\text{cyl}}^2}$$

Plane Wave Mode

$$p_{\text{pw}}(x, r, \phi; t) = \left[A_{00} e^{jkx} + B_{00} e^{-jkx} \right] e^{j\omega t} \quad (10)$$

Mouth Cavity

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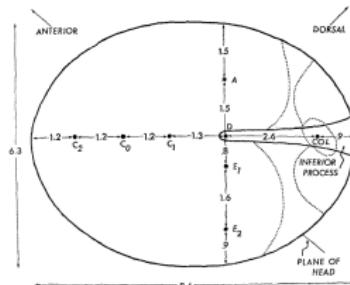
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Eardrum

Eardrum

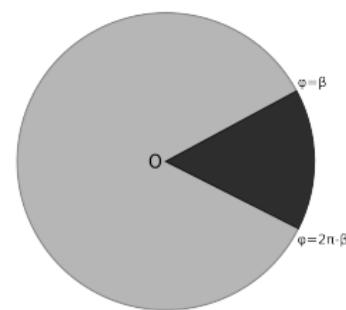
Sketch of a Tokay eardrum as seen from the outside^a.



COL - approximate position opposite the extracolumella insertion.

^aG. A. Manley, "The middle ear of the tokay gecko," *Journal of Comparative Physiology*, vol. 81, no. 3, pp. 239–250, 1972

The ICE eardrum.



Extracolumnella (dark) - rigid, stationary.

Tympanum - assumed linear elastic.

Rigidly clamped at the boundaries ($r = a_{\text{tym}}^*$ and $\phi = \beta, 2\pi - \beta$)

Membrane Vibrations

Membrane EOM

$$-\partial_t^2 u(r, \phi; t) - 2\alpha \partial_t u(r, \phi; t) + c_M^2 \Delta_{(2)} u(r, \phi; t) = \frac{1}{\rho_m d} \Psi(r, \phi; t) \quad (11)$$

Membrane parameters

α - damping coefficient, c_M^2 - propagation velocity

ρ_m - density, d - thickness.

Free-Undamped Membrane, $\alpha \rightarrow 0$, $\Psi \rightarrow 0$

Separation Ansatz

$$u(r, \phi; t) = f(r)g(\phi)h(t) \quad (12)$$

Separated Equations

$$\frac{d^2 g(\phi)}{d\phi^2} + \kappa^2 g(\phi) = 0 \quad (13)$$

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial f(r)}{\partial r} \right) + \left[\mu^2 - \frac{\kappa^2}{r^2} \right] f(r) = 0 \quad (14)$$

$$\frac{d^2 h(t)}{dt^2} + c_M^2 \mu^2 h(t) = 0 \quad (15)$$

Boundary Conditions

ϕ -direction: $u(r, \beta; t) = u(r, 2\pi - \beta, t) = 0$

$$\Rightarrow g(\phi) = \sin \kappa(\phi - \beta) \quad (16)$$

where, $\kappa = \frac{m\pi}{2(\pi - \beta)}$, $m = 1, 2, 3, \dots$

r -direction: $u(a_{\text{tym}} \cos \phi, \phi; t) = 0$

$$\Rightarrow f(r) = J_\kappa(\mu_{mn} r / a_{\text{tym}}) \quad (17)$$

where, μ_{mn} is the n^{th} zero of J_κ

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Free eigenmodes

$$u_{mn}(r, \phi) = \sin \kappa(\phi - \beta) J_\kappa(\mu_{mn} r) \quad (18)$$

$$u_{\text{free}}(r, \phi; t) = \sum_{m=0, n=1}^{\infty} C_{mn} u_{mn}(r, \phi) e^{j\omega_{mn} t} \quad (19)$$

where, $\omega_{mn} = c_M \mu_{mn}$

Damped membrane

$$\tilde{u}_{\text{free}}(r, \phi; t) = \sum_{m=0, n=1}^{\infty} \tilde{C}_{mn} u_{mn}(r, \phi) e^{j\omega_{mn} t - \alpha t} \quad (20)$$

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Forced Vibrations: $\Psi = p e^{j\omega t}$

Steady State Solution

$$u_{ss}(r, \phi; t) =: \sum_{m=0, n=1}^{\infty} C_{mn} u_{mn}(r, \phi) e^{j\omega t} \quad (21)$$

Substitute u_{ss} in Membrane EOM.

$$C_{mn} = \frac{p \int dS u_{mn}}{\Omega_{mn} \int dS u_{mn}^2} \quad (22)$$

$$\Omega_{mn} = \rho_M d [(\omega^2 - \omega_{mn}^2) - 2j\alpha\omega]$$

Forced Vibrations: $\Psi = pe^{j\omega t}$

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Forced Vibrations contd.

Transient Solution

Same as the solution for a free damped membrane

$$u_t(r, \phi; t) = \sum_{m=0, n=1}^{\infty} \tilde{C}_{mn} u_{mn}(r, \phi) e^{j\omega_{mn}t - \alpha t} \quad (23)$$

\tilde{C}_{mn} determined from the membrane displacement at $t = 0$.
 $u_t \rightarrow 0$ exponentially as $t \rightarrow \infty$.

Steady State Approximation

$u \approx u_{ss}$ if α is "large".

Forced Vibrations contd.

Transient Solution

Same as the solution for a free damped membrane

$$u_t(r, \phi; t) = \sum_{m=0, n=1}^{\infty} \tilde{C}_{mn} u_{mn}(r, \phi) e^{j\omega_{mn}t - \alpha t} \quad (23)$$

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$u \approx u_{ss}$ if α is “large” .

Coupled Membranes

Coupled Membranes

$$u_{0/L} = \sum_{m=0, n=1}^{\infty} C_{mn}^0 u_{mn}(r, \phi) e^{j\omega t} \quad (24)$$

Membrane Equations

$$\sum_{m=0, n=1}^{\infty} \Omega_{mn} C_{mn}^0 u_{mn}(r, \phi) e^{j\omega t} = p_0 e^{j\omega t} - p(0, r, \phi; t) \quad (25)$$

$$\sum_{m=0, n=1}^{\infty} \Omega_{mn} C_{mn}^L u_{mn}(r, \phi) e^{j\omega t} = p_L e^{j\omega t} - p(L, r, \phi; t) \quad (26)$$

Coupled Membranes

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$$u_{0/L} = \sum_{m=0, n=1}^{\infty} C_{mn}^0 u_{mn}(r, \phi) e^{j\omega t} \quad (24)$$

Membrane Equations

$$\sum_{m=0, n=1}^{\infty} \Omega_{mn} C_{mn}^0 u_{mn}(r, \phi) e^{j\omega t} = p_0 e^{j\omega t} - p(0, r, \phi; t) \quad (25)$$

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“Surface” Velocity

$$U_{0/L} = \begin{cases} u_{0/L}, & 0 < r < a_{\text{tym}} \text{ and } \beta < \phi < 2\pi - \beta \\ 0, & \text{otherwise} \end{cases} . \quad (27)$$

Velocity in x -direction

$$v_x = - \sum_{q=0, s=0}^{\infty} \frac{\zeta_{qs}}{\rho\omega} \left(A_{qs} e^{j\zeta_{qs}x} - B_{qs} e^{-j\zeta_{qs}x} \right) p_{qs}(r, \phi) e^{j\omega t} \quad (28)$$

Boundary Conditions

Exact

$$U_0 = -\frac{1}{j\omega} v_x(0, r, \phi; t) \quad (29)$$

$$U_L = \frac{1}{j\omega} v_x(L, r, \phi; t) \quad (30)$$

Approximate

$$U_{0/L} \approx S^{0/L}(t) =: \int dS U_{0/L} \quad (31)$$

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Approximate

$$U_{0/L} \approx S^{0/L}(t) =: \int dS U_{0/L} \quad (31)$$

Boundary Conditions

Higher pressure modes disappear, i.e.

$$p = [A_{00}e^{jkx} + B_{00}e^{-jkx}] e^{j\omega t}$$

$$A_{00} = -\frac{\rho\omega^2}{2k \sin kL} (S^0 e^{-jkL} + S^L) \quad (32)$$

$$B_{00} = -\frac{\rho\omega^2}{2k \sin kL} (S^0 e^{jkL} + S^L) \quad (33)$$

Coupled Equations

$$\sum_{m=0,n=1}^{\infty} \Omega_{mn} C_{mn}^0 u_{mn}(r, \phi) = p_0 + \frac{\rho\omega^2}{k} \left(\frac{S^0}{\tan kL} + \frac{S^L}{\sin kL} \right) \quad (34)$$

$$\sum_{m=0,n=1}^{\infty} \Omega_{mn} C_{mn}^L u_{mn}(r, \phi) = p_L + \frac{\rho\omega^2}{k} \left(\frac{S^0}{\sin kL} + \frac{S^L}{\tan kL} \right) \quad (35)$$

Decoupling

Decouple by taking the sum and difference of the above equations.

Coupled Equations

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Coupled Membranes

Decoupled Equations

$$\sum_{m=0,n=1}^{\infty} \Omega_{mn} C_{mn}^+ u_{mn}(r, \phi) = p_+ + \frac{\rho\omega^2}{k} S^+ \cot \frac{kL}{2} \quad (36)$$

$$\sum_{m=0,n=1}^{\infty} \Omega_{mn} C_{mn}^- u_{mn}(r, \phi) = p_- - \frac{\rho\omega^2}{k} S^- \tan \frac{kL}{2} \quad (37)$$

$$C_{mn}^+ = \left[p_+ + \frac{\rho\omega^2}{k} S^+ \cot \frac{kL}{2} \right] \frac{\int dS u_{mn}}{\Omega_{mn} \int dS u_{mn}^2} \quad (38)$$

$$C_{mn}^- = \left[p_- - \frac{\rho\omega^2}{k} S^- \tan \frac{kL}{2} \right] \frac{\int dS u_{mn}}{\Omega_{mn} \int dS u_{mn}^2} \quad (39)$$

Decoupled Equations contd.

$$S^+ = \frac{p_L + p_0}{\Lambda + \Gamma_+} \quad S^- = \frac{p_L - p_0}{\Lambda + \Gamma_-} \quad (40)$$

$$\Gamma_+ = -\frac{\rho\omega^2}{k} \cot \frac{kL}{2}, \quad \Gamma_- = \frac{\rho\omega^2}{k} \tan \frac{kL}{2} \quad (41)$$

$$\frac{1}{\Lambda} = \frac{1}{\pi a_{\text{cyl}}^2} \sum_{m=0, n=1}^{\infty} \frac{\left(\int dS u_{mn} \right)^2}{\Omega_{mn} \int dS u_{mn}^2} \quad (42)$$

Final Expressions

Membrane Displacement

$$S_0(t) = G_{ipsi}^s p_0 + G_{contra}^s p_L \quad (43)$$

$$S_L(t) = G_{contra}^s p_0 + G_{ipsi}^s p_L \quad (44)$$

$$G_{ipsi}^s = \left(\frac{1}{\Lambda + \Gamma_+} + \frac{1}{\Lambda + \Gamma_-} \right) / 2 \quad (45)$$

$$G_{contra}^s = \left(\frac{1}{\Lambda + \Gamma_+} - \frac{1}{\Lambda + \Gamma_-} \right) / 2 \quad (46)$$

Introduction

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The Model

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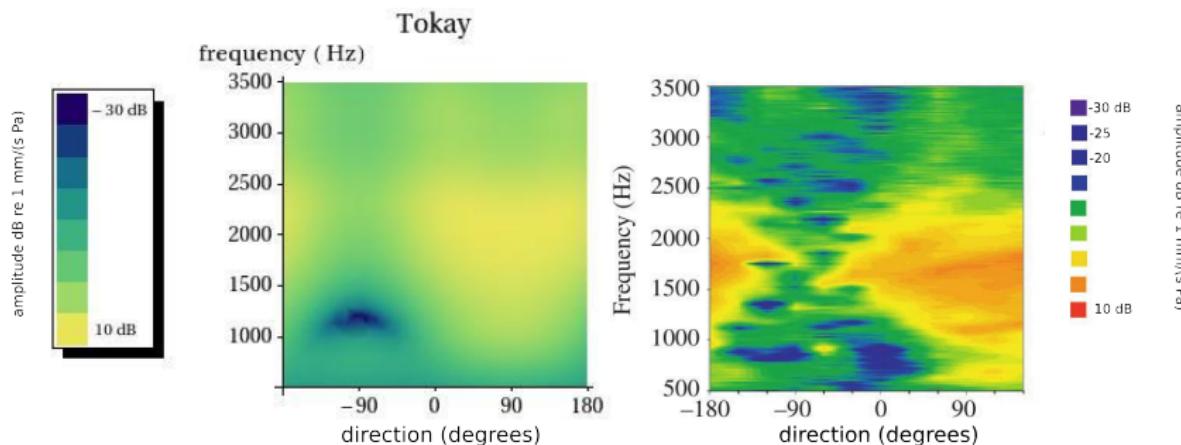
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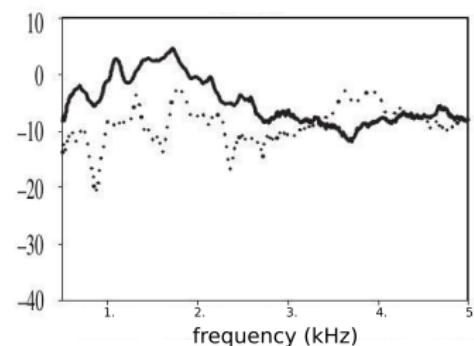
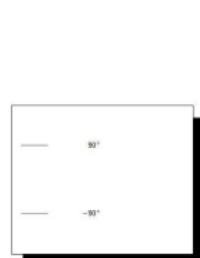
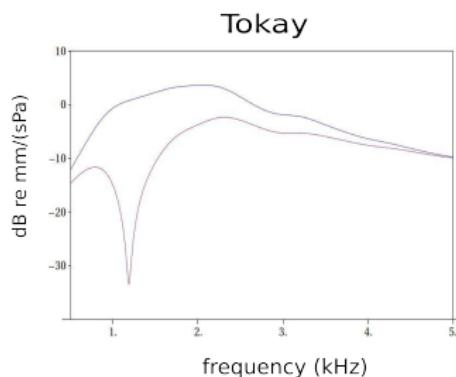
Vibration Amplitude



- ▶ Plot of $20\log_{10} \left| \dot{S}^0 / (\pi a_{cyl}^2) \right|$ w.r.t direction frequency.
- ▶ $|p_0| = |p_L| = 1 \text{ Pa}$.

Vibration Amplitude

Vibration Amplitude - Spectrum



- ▶ Plot of $20\log_{10} \left| \dot{S}^0 / (\pi a_{cy}^2) \right|$, against frequency for $\theta = 90^\circ$.
- ▶ $|p_0| = |p_L| = 1 \text{ Pa}$.

Vibration Amplitude

▶ Inputs to ears

- ▶ Negligible level (amplitude) difference
- ▶ Small time (phase) difference

- ▶ We still need functions that quantify the directional and frequency dependence of the system.

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Directional Cues

Hearing Cues

Internal Level Difference -

$$iLD := 20 \log_{10} \left(\left| \frac{\dot{S}^0}{\dot{S}^L} \right| \right). \quad (47)$$

Internal Time Difference -

$$iTD := \text{Arg} \left(\frac{\dot{S}^0}{\dot{S}^L} \right) / \omega. \quad (48)$$

Directional Cues

Hearing Cues

Internal Level Difference -

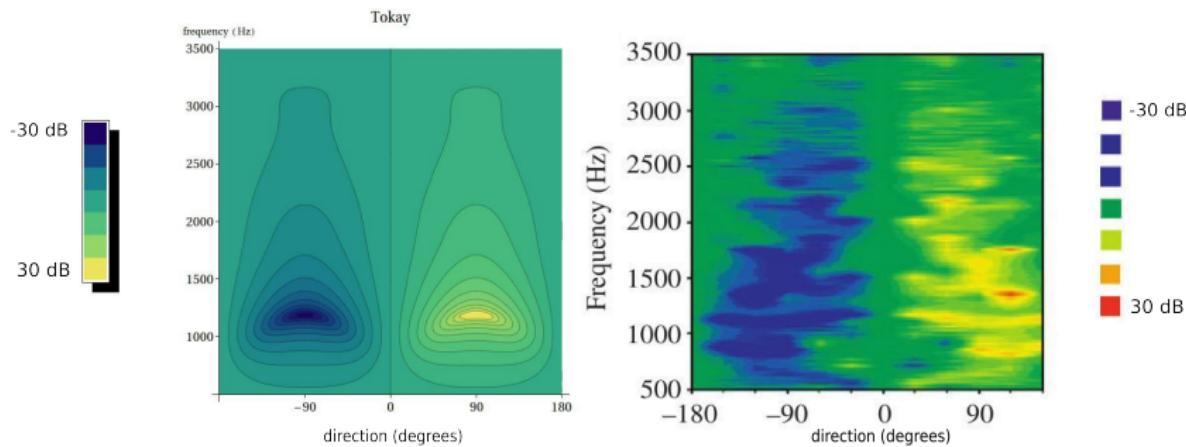
$$iLD := 20 \log_{10} \left(\left| \frac{\dot{S}^0}{\dot{S}^L} \right| \right). \quad (47)$$

Internal Time Difference -

$$iTD := \text{Arg} \left(\frac{\dot{S}^0}{\dot{S}^L} \right) / \omega. \quad (48)$$

Directional Cues

Internal Level Difference



- ▶ Plot of iLD, against frequency and direction.

Outline for Section 4

Introduction

Auditory Systems

Hearing Cues

The Model

Mouth Cavity

Acoustic Head Model
Pressure Derivation

Eardrum

Model

Membrane Vibrations

Coupled Membranes

Boundary Conditions

Evaluation

Vibration Amplitude

Directional Cues

Internal Level Difference

Internal Time Difference

Conclusion

Introduction

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The Model

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Evaluation

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○○

Conclusion

Conclusion

Thank You

