

## Problem: Strictly Increasing Beauty Partition

You are given an array  $A$  of size  $N$ . You need to partition it into contiguous, non-empty subarrays such that the beauty of each subarray forms a strictly increasing sequence.

Beauty of a subarray is defined as the sum of its elements.

Return the total number of such valid partitions, modulo  $10^9 + 7$ .

Input:

- int  $N$ : the number of elements in array  $A$
- List<Integer>  $A$ : the array elements

Constraints:

- $1 \leq N \leq 1000$
- $-10^9 \leq A[i] \leq 10^9$

Output:

- Integer: Number of valid partitions modulo  $10^9 + 7$

Example:

Input:  $A = [1, 2, 3]$

Output: 3

Explanation:

Valid partitions are:

- $[1, 2, 3] \Rightarrow$  beauty:  $[6]$
- $[1], [2, 3] \Rightarrow$  beauty:  $[1, 5]$
- $[1], [2], [3] \Rightarrow$  beauty:  $[1, 2, 3]$

-----

```
import java.util.*;
```

```
public class Main {
```

```
    static final int MOD = 1_000_000_007;
```

```
    public static int getAnswer(int N, List<Integer> A) {
```

```
        long[] prefix = new long[N + 1];
```

```
        for (int i = 0; i < N; i++) {
```

```
            prefix[i + 1] = prefix[i] + A.get(i);
```

```
        }
```

```
        Map<Integer, TreeMap<Long, Integer>> memo = new HashMap<>();
```

```
        return dfs(0, Long.MIN_VALUE, A, prefix, memo);
```

```
    }
```

```
    private static int dfs(int start, long prevSum, List<Integer> A, long[] prefix,
```

```
        Map<Integer, TreeMap<Long, Integer>> memo) {
```

```
        if (start == A.size()) return 1;
```

```
        TreeMap<Long, Integer> memAtStart = memo.getOrDefault(start, new TreeMap<>());
```

```
        if (memAtStart.containsKey(prevSum)) return memAtStart.get(prevSum);
```

```
        int count = 0;
```

```

    for (int end = start + 1; end <= A.size(); end++) {
        long currSum = prefix[end] - prefix[start];
        if (currSum > prevSum) {
            count = (count + dfs(end, currSum, A, prefix, memo)) % MOD;
        }
    }

    memAtStart.put(prevSum, count);
    memo.put(start, memAtStart);
    return count;
}

public static void main(String[] args) {
    System.out.println(getAnswer(3, Arrays.asList(1, 2, 3))); // 3
    System.out.println(getAnswer(4, Arrays.asList(1, 1, 1, 1))); // 5
    System.out.println(getAnswer(3, Arrays.asList(1000000000, 1000000000,
1000000000))); // 3
    System.out.println(getAnswer(2, Arrays.asList(-5, 10))); // 2
}
}

```