

# NCERT Assignment

EE22BTECH11009-ANUPAMA KULSHRESHTHA

There are 5% defective items in a large bulk of items.  
What is the probability that a sample of 10 items will include not more than one defective item?

**Solution:**

We define random variable  $X$  as shown in table 1

$X = 0$	Bernoulli Random Variable (Item is not defective)
$X = 1$	Bernoulli Random Variable (Item is defective)
$n$	Number of trials
$p$	Probability of single successful outcome
$k$	Number of successful outcomes

TABLE 1: Definition of  $X$  and parameters.

Then

$$p_X(1) = \frac{5}{100} \quad (1)$$

$$= 0.05 \quad (2)$$

$$p_X(0) = 1 - p_X(1) \quad (3)$$

$$= 0.95 \quad (4)$$

We use binomial distribution to solve this question, whose formula is given by

$$p_X(k) = {}^nC_k p^k (1-p)^{n-k}$$

Here,  $p = 0.05$  and  $q = 0.95$  The CDF of binomial is given by

$$\Pr(X \leq n) = \begin{cases} 0, & n < 0 \\ \sum_{k=0}^n {}^{10}C_k p^k q^{10-k}, & 0 \leq n \leq 10 \\ 1, & \text{otherwise} \end{cases} \quad (5)$$

Here, the desired probability is  $\Pr(X \leq 1)$  Hence,

$$\Pr(X \leq 1) = \sum_{k=0}^1 {}^{10}C_k p^k q^{10-k} \quad (6)$$

$$= 0.9138 \quad (7)$$