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## NCERT Assignment

## EE22BTECH11009-ANUPAMA KULSHRESHTHA

There are 5% defective items in a large bulk of items. What is the probability that a sample of 10 items will include not more than one defective item?

## **Solution:**

We define random variable X as shown in table 1

X = 0	Bernoulli Random Variable (Item is not defective)
X = 1	Bernoulli Random Variable (Item is defective)
n	Number of trials
p	Probability of single successful outcome
k	Number of successful outcomes

TABLE 1: Definition of X and parameters.

Then

$$p_X(1) = \frac{5}{100}$$

$$= 0.05$$

$$p_X(0) = 1 - p_X(1)$$
(1)
(2)

$$p_X(0) = 1 - p_X(1) \tag{5}$$

$$= 0.95 \tag{4}$$

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We use binomial distribution to solve this question, whose formula is given by

$$p_X(k) = {}^{n}C_k p^k (1-p)^{n-k}$$

Here, p = 0.05 and q = 0.95 The CDF of binomial is given by

$$\Pr(X \le n) = \begin{cases} 0, & n < 0\\ \sum_{k=0}^{n} {}^{10}C_k p^k q^{10-k}, & 0 \le n \le 10\\ 1, & \text{otherwise} \end{cases}$$
 (5)

Here, the desired probability is  $Pr(X \le 1)$  Hence,

$$\Pr(X \le 1) = \sum_{k=0}^{1} {}^{10}C_k p^k q^{10-k}$$
 (6)

$$= 0.9138$$
 (7)