

reference point → moving anticlockwise.
Every turn shall be left turn

$$1) T(n) = nT(n-1) + n, \text{ if } n \geq 1, \\ = 1 \quad \text{if } n = 1$$

$$2) T(n) = \Theta(1) \quad \text{if } n \leq 140 \\ = T\left(\frac{n}{5}\right) + T\left(\frac{4n}{5}\right) + \Theta(n) \quad \text{if } n \geq 140$$

$$3) T(n) = 2T\left(\frac{n}{4}\right) + 3T\left(\frac{n}{6}\right) + \Theta(n \log n) \quad ; \quad n \geq 1 \\ = 1$$

$$4) T(n) = nT(n-1) + n$$

$$\Rightarrow T(n) = aT(n-b) + f(n) \Rightarrow \textcircled{2} T(n) = \Theta(n^k \log^p n) \\ \boxed{p \geq 0} \\ k \geq 1$$

Akronatz

$$T(x) = \begin{cases} \Theta(1) & \text{if } 1 \leq x \leq x_0 \\ \sum_{i=1}^k a_i T(b_i x) + g(x) & \text{if } x > x_0, \end{cases} \quad b_i \in (0, 1)$$

$$T(x) = \Theta\left(x^p \left(1 + \int_1^x \frac{g(u)}{u^{p+1}} du\right)\right)$$

$$\sum_{i=1}^k a_i b_i^p = 1$$

$$T(n) = n T(n-1) + n$$

Master's Theorem for ^{Decreasing} ~~Divide & Conquer~~

$$T(n) = a T(n-b) + f(n)$$

$$f(n) = \Theta(n^k \log^p n) = n$$

$$\therefore k=1, p=0$$

$$\log_b a = \log_1 n$$

★

$$E_2: T(n) = T(\sqrt{n}) + \log n$$

$$= T(n^{1/2}) + \log_2 n$$

$$n = 2^m$$

$$T(2^m) = T(2^{m/2}) + \log_2 2^m =$$

$$T(2^m) = T(2^{m/2}) + m$$

$$S(m) = T(2^m)$$

$$S(m/2) = T(2^{m/2})$$

$$\therefore S(m) = S\left(\frac{m}{2}\right) + m \Rightarrow S(m) = O(m) = T(2^m)$$

$$T(n) = O(m) = O(\log_2 n)$$

$$E_3: T(n) = T(\sqrt{n}) + 1$$

$$O(\log_2 \log_2 n)$$