Factors Affecting CPC



4. Make a data model to predict the factors affecting CPC.

The aim was to build a data model for feature selection. Methods Used: 1. Using Step wise regression 2.Random Forest (Limitation can only perform feature selection till 53 levels but Region and city indicator had more levels. In order to continue withthe model removed region and city indicators) 3.Decision Trees(Same limitation as Random Forest) 4.Boruta

Conclusion: As per the data models top 5 predictors are: a) CTR b) Clicks c) CPV d) Total Spend e) CPCV

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```
Data<-read.csv('D:/Rutgers Study Material/MultivariateData1.csv')
# top 5 columns of the dataset
head(Data)</pre>
```

ïRegion <fctr></fctr>	Region_Indicators <int></int>	City <fctr></fctr>	City_indicators <int></int>	SupplyVendor <fctr></fctr>	SupplyVendors_Ind
1 Hawaii	60	'Aiea	2208	beanstock	
2 Hawaii	60	'Aiea	2208	brightroll	
3 Hawaii	60	'Aiea	2208	brightroll	
4 Hawaii	60	'Aiea	2208	brightroll	
5 Hawaii	60	'Aiea	2208	brightroll	
6 Hawaii	60	'Aiea	2208	brightroll	

```
# Removing the extra columns
drops <- c("ï..Region","City","SupplyVendor","OS","Browser","DeviceType","Impression_Time")
New_data<-Data[ , !(names(Data) %in% drops)]
dim(New_data)</pre>
```

```
[1] 472666 16
```

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```
New_data$CPV[ is.na(New_data$CPV)] <- 0
New_data$CPC[ is.na(New_data$CPC)] <- 0
New_data$CPCV[ is.na(New_data$CPCV)] <- 0</pre>
```

Model fitting
fit<- lm(CPC~., data=New_data)
summary(fit)</pre>

```
Call:
lm(formula = CPC ~ ., data = New data)
Residuals:
     Min
                1Q
                      Median
                                    3Q
                                             Max
-0.012169 -0.000021 0.000005 0.000021 0.039840
Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
                        -1.280e-04 4.415e-06 -28.983 < 2e-16
(Intercept)
Region Indicators
                        -2.602e-09 3.041e-08 -0.086 0.93181
City indicators
                         5.898e-10 4.249e-10
                                                1.388 0.16511
SupplyVendors Indicators 3.216e-07 9.976e-08
                                                3.224 0.00126
                         6.012e-07 1.090e-07
OS Indicators
                                                5.513 3.53e-08
Browser_Indicators
                         2.395e-06 2.633e-07
                                                9.096 < 2e-16
DeviceType Indicators
                        -5.771e-06 8.246e-07 -6.998 2.60e-12
Impression Day
                        -4.916e-07 2.676e-07 -1.837 0.06618
Impressions
                         1.176e-05 2.890e-06
                                                4.070 4.71e-05
Clicks
                         3.144e-04 3.416e-05
                                                9.204 < 2e-16
CTR
                         1.197e-02 3.508e-05 341.272 < 2e-16
VCR
                         2.566e-05 5.627e-06
                                                4.560 5.12e-06
CPV
                         -1.365e-03 2.936e-04 -4.650 3.33e-06
Completes
                        -2.073e-05 4.521e-06 -4.586 4.51e-06
Total_Spend
                         1.190e-02 3.480e-04 34.186 < 2e-16
CPCV
                        -1.321e-03 2.639e-04 -5.004 5.60e-07
(Intercept)
Region Indicators
City indicators
SupplyVendors Indicators **
OS Indicators
Browser_Indicators
DeviceType_Indicators
Impression Day
Impressions
Clicks
CTR
VCR
CPV
Completes
Total_Spend
CPCV
Signif. codes: 0 □***□ 0.001 □*□ 0.01 □*□ 0.05 □.□ 0.1 □ □ 1
Residual standard error: 0.0003526 on 472650 degrees of freedom
Multiple R-squared: 0.8855,
                               Adjusted R-squared: 0.8855
F-statistic: 2.437e+05 on 15 and 472650 DF, p-value: < 2.2e-16
```

Step wise Regression
model1<- step(fit)</pre>

```
Start: AIC=-7515546
CPC ~ Region_Indicators + City_indicators + SupplyVendors_Indicators +
    OS Indicators + Browser Indicators + DeviceType Indicators +
    Impression Day + Impressions + Clicks + CTR + VCR + CPV +
    Completes + Total_Spend + CPCV
                           Df Sum of Sq
                                              RSS
                                                       AIC
- Region Indicators
                            1 0.0000000 0.058762 -7515548
- City_indicators
                            1 0.0000002 0.058763 -7515546
<none>
                                         0.058762 -7515546
- Impression Day
                            1 0.0000004 0.058763 -7515544
- SupplyVendors Indicators 1 0.0000013 0.058764 -7515537
- Impressions
                            1 0.0000021 0.058764 -7515531
- VCR
                            1 0.0000026 0.058765 -7515527
- Completes
                            1 0.0000026 0.058765 -7515526
- CPV
                            1 0.0000027 0.058765 -7515526
- CPCV
                            1 0.0000031 0.058765 -7515522
- OS Indicators
                            1 0.0000038 0.058766 -7515517

    DeviceType Indicators

                            1 0.0000061 0.058768 -7515499
- Browser Indicators
                            1 0.0000103 0.058773 -7515465
- Clicks
                            1 0.0000105 0.058773 -7515463
- Total Spend
                            1 0.0001453 0.058908 -7514380
                            1 0.0144797 0.073242 -7411434
- CTR
Step: AIC=-7515548
CPC ~ City indicators + SupplyVendors Indicators + OS Indicators +
    Browser_Indicators + DeviceType_Indicators + Impression_Day +
    Impressions + Clicks + CTR + VCR + CPV + Completes + Total Spend +
    CPCV
                           Df Sum of Sq
                                              RSS
                                                       AIC
                                         0.058762 -7515548
<none>
- City_indicators
                            1 0.0000003 0.058763 -7515547
- Impression_Day
                            1 0.0000004 0.058763 -7515546
- SupplyVendors Indicators 1 0.0000013 0.058764 -7515539
- Impressions
                            1 0.0000021 0.058764 -7515533
- VCR
                            1 0.0000026 0.058765 -7515529
- Completes
                            1 0.0000026 0.058765 -7515528
- CPV
                            1 0.0000027 0.058765 -7515528
- CPCV
                            1 0.0000031 0.058765 -7515524
- OS Indicators
                            1 0.0000038 0.058766 -7515519
DeviceType_Indicators
                            1 0.0000061 0.058768 -7515501
- Browser Indicators
                            1 0.0000104 0.058773 -7515466
- Clicks
                            1 0.0000105 0.058773 -7515465
- Total_Spend
                            1 0.0001453 0.058908 -7514382
- CTR
                            1 0.0144840 0.073246 -7411408
```

summary(model1)

```
Call:
lm(formula = CPC ~ City indicators + SupplyVendors Indicators +
    OS Indicators + Browser Indicators + DeviceType Indicators +
    Impression Day + Impressions + Clicks + CTR + VCR + CPV +
    Completes + Total_Spend + CPCV, data = New_data)
Residuals:
     Min
                1Q
                      Median
                                    3Q
                                             Max
-0.012169 -0.000021 0.000005 0.000021 0.039840
Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
(Intercept)
                         -1.280e-04 4.399e-06 -29.092 < 2e-16
City indicators
                         5.781e-10 4.023e-10
                                                1.437 0.15068
SupplyVendors Indicators 3.216e-07 9.976e-08
                                                3.224 0.00127
OS Indicators
                         6.011e-07 1.090e-07
                                                5.512 3.54e-08
Browser Indicators
                         2.392e-06 2.620e-07
                                                9.131 < 2e-16
DeviceType Indicators
                        -5.770e-06 8.246e-07 -6.998 2.61e-12
Impression Day
                         -4.916e-07 2.676e-07 -1.837 0.06618
Impressions
                         1.176e-05 2.890e-06
                                                4.070 4.70e-05
Clicks
                                                9.207 < 2e-16
                         3.145e-04 3.416e-05
CTR
                         1.197e-02 3.507e-05 341.323 < 2e-16
VCR
                         2.565e-05 5.626e-06
                                                4.559 5.13e-06
CPV
                         -1.365e-03 2.936e-04 -4.651 3.31e-06
Completes
                         -2.074e-05 4.521e-06 -4.587 4.51e-06
Total Spend
                         1.190e-02 3.480e-04 34.186 < 2e-16
CPCV
                         -1.321e-03 2.639e-04 -5.004 5.62e-07
                         ***
(Intercept)
City indicators
SupplyVendors_Indicators **
OS Indicators
Browser_Indicators
DeviceType_Indicators
Impression Day
Impressions
Clicks
CTR
VCR
CPV
Completes
Total_Spend
CPCV
Signif. codes: 0 □***□ 0.001 □*□ 0.01 □*□ 0.05 □.□ 0.1 □ □ 1
Residual standard error: 0.0003526 on 472651 degrees of freedom
Multiple R-squared: 0.8855,
                               Adjusted R-squared: 0.8855
F-statistic: 2.611e+05 on 14 and 472651 DF, p-value: < 2.2e-16
```

```
Hide
```

```
drops <- c("Region_Indicators","City_indicators")
RF<-New_data[ , !(names(New_data) %in% drops)]</pre>
```

```
dt<-sort(sample(nrow(RF),nrow(RF)*.8))
train<-RF[dt,]
test<-RF[-dt,]
library(randomForest)</pre>
```

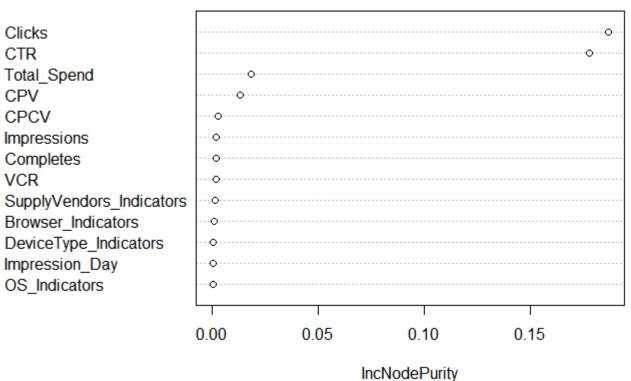
package $\langle U+393C \rangle \langle U+3E31 \rangle$ randomForest $\langle U+393C \rangle \langle U+3E32 \rangle$ was built under R version 3.4.3randomForest 4.6-12

Type rfNews() to see new features/changes/bug fixes.

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```
model3 <- randomForest(CPC~., train, ntree=50)
varImpPlot(model3)</pre>
```

model3



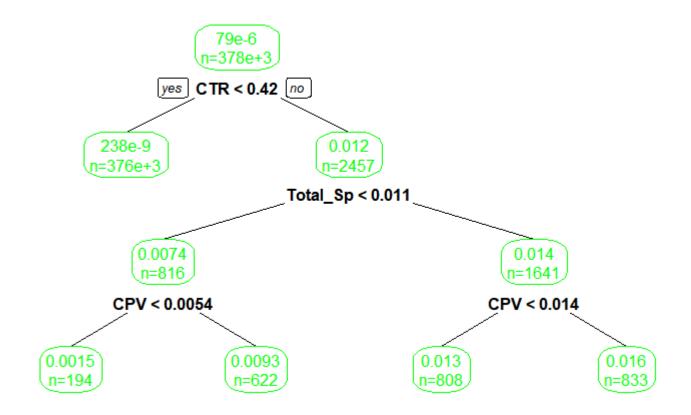
Hide

library(rpart)

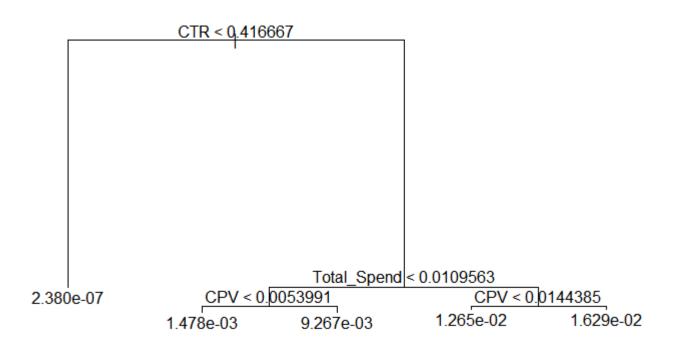
 $package < U+393C> < U+3E31> rpart < U+393C> < U+3E32> \ was \ built \ under \ R \ version \ 3.4.3$

```
library(rpart.plot)
package <U+393C><U+3E31>rpart.plot<U+393C><U+3E32> was built under R version 3.4.3
                                                                                         Hide
library(caret)
package <U+393C><U+3E31>caret<U+393C><U+3E32> was built under R version 3.4.3Loading required pa
ckage: lattice
Loading required package: ggplot2
Attaching package: <U+393C><U+3E31>ggplot2<U+393C><U+3E32>
The following object is masked from <U+393C><U+3E31>package:randomForest<U+393C><U+3E32>:
    margin
                                                                                         Hide
pred2 <- predict(model3, test)</pre>
confusionMatrix(pred2, test$CPC)
Error in confusionMatrix.default(pred2, test$CPC) :
  the data cannot have more levels than the reference
                                                                                         Hide
str(train)
'data.frame':
               378132 obs. of 14 variables:
 $ SupplyVendors_Indicators: int 3 4 4 4 4 4 4 4 4 4 ...
 $ OS_Indicators
                         : int 1 8 9 11 12 12 12 13 1 1 ...
 $ Browser Indicators
                         : int 4 1 1 1 1 1 1 1 1 1 ...
 $ DeviceType_Indicators
                         : int 111111111...
 $ Impression Day
                         : int 1354455444...
 $ Impressions
                         : int 111111111...
 $ Clicks
                         : int 0000000000...
 $ CTR
                         : num 0000000000...
 $ CPC
                         : num
                                00000000000...
 $ VCR
                         : num
                                0101100111...
 $ CPV
                                0.01271 0.00997 0.00941 0.01025 0.00968 ...
                         : num
 $ Completes
                         : int 0101100111...
 $ Total_Spend
                         : num 0.01271 0.00997 0.00941 0.01025 0.00968 ...
 $ CPCV
                          : num 0 0.00997 0 0.01025 0.00968 ...
```

```
model <- rpart(CPC~.,data=train)
prp(model, type=2, extra=1, col="green")</pre>
```



library(tree)
model1<-tree(CPC~.,train)
plot(model1)
text(model1,pretty=0)</pre>



boruta_output <- Boruta(CPC ~ ., doTrace=2,data=New_data)</pre>

1. run of importance source...

Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 32 seconds.

Growing trees.. Progress: 50%. Estimated remaining time: 1 minute, 2 seconds.

Growing trees.. Progress: 75%. Estimated remaining time: 30 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 46 seconds.

Computing permutation importance.. Progress: 71%. Estimated remaining time: 25 seconds.

2. run of importance source...

Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 33 seconds.

Growing trees.. Progress: 50%. Estimated remaining time: 1 minute, 1 seconds.

Growing trees.. Progress: 77%. Estimated remaining time: 27 seconds.

Computing permutation importance.. Progress: 34%. Estimated remaining time: 1 minute, 0 seconds.

Computing permutation importance.. Progress: 68%. Estimated remaining time: 28 seconds.

```
Growing trees.. Progress: 26%. Estimated remaining time: 1 minute, 29 seconds.

Growing trees.. Progress: 51%. Estimated remaining time: 59 seconds.

Growing trees.. Progress: 78%. Estimated remaining time: 26 seconds.

Computing permutation importance.. Progress: 38%. Estimated remaining time: 53 seconds.

Computing permutation importance.. Progress: 68%. Estimated remaining time: 30 seconds.
```

```
Growing trees.. Progress: 26%. Estimated remaining time: 1 minute, 28 seconds.

Growing trees.. Progress: 51%. Estimated remaining time: 58 seconds.

Growing trees.. Progress: 79%. Estimated remaining time: 25 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 53 seconds.

Computing permutation importance.. Progress: 73%. Estimated remaining time: 24 seconds.
```

5. run of importance source...

```
Growing trees.. Progress: 21%. Estimated remaining time: 1 minute, 56 seconds.

Growing trees.. Progress: 42%. Estimated remaining time: 1 minute, 27 seconds.

Growing trees.. Progress: 63%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 83%. Estimated remaining time: 24 seconds.

Computing permutation importance.. Progress: 31%. Estimated remaining time: 1 minute, 9 seconds.

Computing permutation importance.. Progress: 58%. Estimated remaining time: 44 seconds.

Computing permutation importance.. Progress: 91%. Estimated remaining time: 9 seconds.
```

6. run of importance source...

```
Growing trees.. Progress: 20%. Estimated remaining time: 2 minutes, 5 seconds.

Growing trees.. Progress: 39%. Estimated remaining time: 1 minute, 38 seconds.

Growing trees.. Progress: 57%. Estimated remaining time: 1 minute, 11 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 31 seconds.

Computing permutation importance.. Progress: 31%. Estimated remaining time: 1 minute, 7 seconds.

Computing permutation importance.. Progress: 64%. Estimated remaining time: 35 seconds.

Computing permutation importance.. Progress: 96%. Estimated remaining time: 3 seconds.
```

7. run of importance source...

```
Growing trees.. Progress: 27%. Estimated remaining time: 1 minute, 25 seconds.

Growing trees.. Progress: 52%. Estimated remaining time: 58 seconds.

Growing trees.. Progress: 77%. Estimated remaining time: 28 seconds.

Computing permutation importance.. Progress: 41%. Estimated remaining time: 44 seconds.

Computing permutation importance.. Progress: 81%. Estimated remaining time: 14 seconds.
```

```
Growing trees.. Progress: 28%. Estimated remaining time: 1 minute, 20 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 22 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 43 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 12 seconds.
```

```
Growing trees.. Progress: 27%. Estimated remaining time: 1 minute, 25 seconds.

Growing trees.. Progress: 52%. Estimated remaining time: 58 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 23 seconds.

Computing permutation importance.. Progress: 41%. Estimated remaining time: 45 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 12 seconds.
```

10. run of importance source...

```
Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 31 seconds.

Growing trees.. Progress: 52%. Estimated remaining time: 57 seconds.

Growing trees.. Progress: 78%. Estimated remaining time: 26 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 47 seconds.

Computing permutation importance.. Progress: 81%. Estimated remaining time: 14 seconds.
```

11. run of importance source...

```
Growing trees.. Progress: 27%. Estimated remaining time: 1 minute, 22 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 81%. Estimated remaining time: 21 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 42 seconds.

Computing permutation importance.. Progress: 85%. Estimated remaining time: 11 seconds.
```

```
After 11 iterations, +39 mins: confirmed 9 attributes: Browser_Indicators, Clicks, CPV, CTR, DeviceType_Indicators and 4 more; still have 6 attributes left.
```

12. run of importance source...

```
Growing trees.. Progress: 28%. Estimated remaining time: 1 minute, 19 seconds.

Growing trees.. Progress: 55%. Estimated remaining time: 50 seconds.

Growing trees.. Progress: 81%. Estimated remaining time: 21 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 42 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 12 seconds.
```

```
Growing trees.. Progress: 28%. Estimated remaining time: 1 minute, 20 seconds.

Growing trees.. Progress: 54%. Estimated remaining time: 52 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 22 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 42 seconds.

Computing permutation importance.. Progress: 84%. Estimated remaining time: 11 seconds.
```

```
Growing trees.. Progress: 26%. Estimated remaining time: 1 minute, 27 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 23 seconds.

Computing permutation importance.. Progress: 41%. Estimated remaining time: 44 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 13 seconds.
```

15. run of importance source...

```
Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 34 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 80%. Estimated remaining time: 23 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 46 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 13 seconds.
```

```
After 15 iterations, +52 mins: confirmed 4 attributes: Completes, CPCV, Impressions, VCR; still have 2 attributes left.
```

16. run of importance source...

```
Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 32 seconds.

Growing trees.. Progress: 52%. Estimated remaining time: 58 seconds.

Growing trees.. Progress: 78%. Estimated remaining time: 26 seconds.

Computing permutation importance.. Progress: 39%. Estimated remaining time: 47 seconds.

Computing permutation importance.. Progress: 81%. Estimated remaining time: 14 seconds.
```

17. run of importance source...

```
Growing trees.. Progress: 27%. Estimated remaining time: 1 minute, 22 seconds.

Growing trees.. Progress: 55%. Estimated remaining time: 50 seconds.

Growing trees.. Progress: 82%. Estimated remaining time: 19 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 42 seconds.

Computing permutation importance.. Progress: 84%. Estimated remaining time: 11 seconds.
```

```
Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 32 seconds.

Growing trees.. Progress: 51%. Estimated remaining time: 59 seconds.

Growing trees.. Progress: 78%. Estimated remaining time: 25 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 45 seconds.

Computing permutation importance.. Progress: 82%. Estimated remaining time: 13 seconds.
```

```
Growing trees.. Progress: 29%. Estimated remaining time: 1 minute, 14 seconds.

Growing trees.. Progress: 57%. Estimated remaining time: 46 seconds.

Growing trees.. Progress: 85%. Estimated remaining time: 16 seconds.

Computing permutation importance.. Progress: 43%. Estimated remaining time: 41 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 12 seconds.
```

20. run of importance source...

```
Growing trees.. Progress: 26%. Estimated remaining time: 1 minute, 28 seconds.

Growing trees.. Progress: 44%. Estimated remaining time: 1 minute, 19 seconds.

Growing trees.. Progress: 69%. Estimated remaining time: 41 seconds.

Growing trees.. Progress: 96%. Estimated remaining time: 4 seconds.

Computing permutation importance.. Progress: 41%. Estimated remaining time: 44 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 12 seconds.
```

21. run of importance source...

```
Growing trees.. Progress: 27%. Estimated remaining time: 1 minute, 24 seconds.
Growing trees.. Progress: 54%. Estimated remaining time: 52 seconds.
Growing trees.. Progress: 80%. Estimated remaining time: 22 seconds.
Computing permutation importance.. Progress: 41%. Estimated remaining time: 44 seconds.
Computing permutation importance.. Progress: 84%. Estimated remaining time: 11 seconds.
```

22. run of importance source...

```
Growing trees.. Progress: 28%. Estimated remaining time: 1 minute, 19 seconds.

Growing trees.. Progress: 56%. Estimated remaining time: 49 seconds.

Growing trees.. Progress: 82%. Estimated remaining time: 20 seconds.

Computing permutation importance.. Progress: 43%. Estimated remaining time: 40 seconds.

Computing permutation importance.. Progress: 84%. Estimated remaining time: 11 seconds.
```

```
After 22 iterations, +1.3 hours:
confirmed 1 attribute: City_indicators;
still have 1 attribute left.
```

```
Growing trees.. Progress: 28%. Estimated remaining time: 1 minute, 21 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 81%. Estimated remaining time: 21 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 43 seconds.

Computing permutation importance.. Progress: 84%. Estimated remaining time: 12 seconds.
```

```
Growing trees.. Progress: 26%. Estimated remaining time: 1 minute, 26 seconds.

Growing trees.. Progress: 53%. Estimated remaining time: 54 seconds.

Growing trees.. Progress: 79%. Estimated remaining time: 24 seconds.

Computing permutation importance.. Progress: 42%. Estimated remaining time: 42 seconds.

Computing permutation importance.. Progress: 83%. Estimated remaining time: 13 seconds.
```

25. run of importance source...

```
Growing trees.. Progress: 25%. Estimated remaining time: 1 minute, 33 seconds.

Growing trees.. Progress: 51%. Estimated remaining time: 58 seconds.

Growing trees.. Progress: 78%. Estimated remaining time: 27 seconds.

Computing permutation importance.. Progress: 40%. Estimated remaining time: 46 seconds.

Computing permutation importance.. Progress: 76%. Estimated remaining time: 19 seconds.
```

```
After 25 iterations, +1.4 hours:
confirmed 1 attribute: Region_Indicators;
no more attributes left.
```

```
boruta_signif <- names(boruta_output$finalDecision[boruta_output$finalDecision %in% c("Confirme
d", "Tentative")])
plot(boruta_output, cex.axis=.7, las=2, xlab="", main="Variable Importance")</pre>
```

Variable Importance

