```
In [1]: import matplotlib.pyplot as plt
        import seaborn as sns
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.model selection import cross val score
        from sklearn.linear model import LogisticRegression
        from sklearn.naive bayes import GaussianNB
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.ensemble import GradientBoostingClassifier
        from sklearn.model selection import RandomizedSearchCV
        from sklearn.model selection import GridSearchCV
        from sklearn.ensemble import GradientBoostingClassifier
        from sklearn.metrics import roc auc score, accuracy score, roc curve
        from tqdm import tqdm
        from sklearn.inspection import plot partial dependence
        from sklearn.linear model import ElasticNetCV
        from sklearn.linear model import ElasticNet
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.ensemble import BaggingClassifier
        import numpy as np
        import pandas as pd
```

Conceptual: Cost functions for classification trees

1. (15 points) Consider the Gini index, classification error, an d cross-entropy in simple classification settings with two class es. Of these three possible cost functions, which would be best to use when growing a decision tree? Which would be best to use when pruning a decision tree? Why?

When growing a decision tree, cross-entropy or the Gini index are potential evaluation measures; they are both sensitive to node purity and control for variance across classes (which helps prevent overfitting). Therefore, either of these would be better than using classification error as an evaluation measure, given that it is not sensitive enough. However, there is a tradeoff to

consider, given that classification error rate might be better to use in situations where one prioritizes prediction accuracy in the final pruned tree.

Strobl, C., Boulesteix, A. L., & Augustin, T. (2007). Unbiased split selection for classification trees based on the Gini index. Computational Statistics & Data Analysis, 52(1), 483-501.

## In [ ]:

Application: Predicting attitudes towards racist college professors In this problem set, you are going to predict attitudes towards racist college professors, using the GSS survey data. Specifically, each respondent was asked "Should a person who believes that Blacks are genetically inferior be allowed to teach in a college or university?" Given the kerfuffle over Richard J. Herrnstein and Charles Murray's The Bell Curve and the ostracization of Nobel laureate James Watson over his controversial views on race and intelligence, this analysis will provide further insight into the public debate over this issue.

gss\_\*.csv contains a selection of features from the 2012 GSS. The outcome of interest colrac is a binary variable coded as either ALLOWED or NOT ALLOWED, where 1 = the racist professor should be allowed to teach, and 0 = the racist professor should not be allowed to teach. Documentation for the other predictors (if the variable is not clearly coded) can be viewed here. Some data pre-processing has been done in advance for you to ease your model fitting: (1) Missing values have been imputed; (2) Categorical variables with low-frequency classes had those classes collapsed into an "other" category; (3) Nominal variables with more than two classes have been converted to dummy variables; and (4) Remaining categorical variables have been converted to integer values, stripping their original labels

Your mission is to bring trees into the context of other classification approaches, thereby constructing a series of models to accurately predict an individual's attitude towards permitting racist professors to teach. The learning objectives of this exercise are:

- 1. Implement a battery of learners (including trees)
- 2. Tune hyperparameters
- 3. Substantively evaluate models

```
In [2]: | gss_tr = pd.read_csv("gss_train.csv")
 In [3]: gss_te = pd.read_csv("gss_test.csv")
 In [4]: x_tr = gss_tr.drop(['colrac'], axis=1)
          y tr = gss tr['colrac']
          X te = gss te.drop(['colrac'], axis=1)
          Y te = gss te['colrac']
In [46]: x tr.head() #making sure colrac was dropped (what we're regressing on)
Out[46]:
             age attend authoritarianism black born childs colath colcom colmil colhomo ... partyi
           0
              21
                     0
                                   4
                                         0
                                                           1
                                                                  0
                                                                                1 ...
              42
                     0
                                         0
                                              0
                                                    2
                                                           0
                                                                  1
                                                                        0
                                                                                0 ...
              70
                                         1
                                                          0
           3
              35
                     3
                                         0
                                              0
                                                    2
                                                          0
                                                                                0 ...
              24
                     3
          5 rows × 55 columns
In [48]: X te.head() #making sure colrac was dropped (what we're regressing on)
Out[48]:
             age attend authoritarianism black born childs colath colcom colmil colhomo ... partyi
              22
                     2
                                                                                0 ...
                                   1
                                         0
              49
                     0
                                                           0
              50
              55
                                                                                0 ...
              22
                     3
                                         0
                                                    0
                                                                  0
```

- 2. Estimate the models (35 points; 5 points/model) Estimate the following models, predicting colrac using the training set (the training .csv) with 10-fold CV:
- Logistic regression
- Naive Bayes
- Elastic net regression
- Decision tree (CART)
- Bagging
- Random forest
- Boosting

Did out of order, but included all

Tune the relevant hyperparameters for each model as necessary. Only use the tuned model with the best performance for the remaining exercises. Be sure to leave sufficient time for hyperparameter tuning. Grid searches can be computationally taxing and take quite a while, especially for tree-aggregation methods.

```
In [29]: #Logistic regression
    logistic_reg = LogisticRegression()

#Accuracy
#calculating cv score, taking mean
    logistic_reg_acc = np.mean(cross_val_score(logistic_reg, x_tr, y_tr, sc oring = 'accuracy', cv=10))

#AUC/ROC
#calculating cv score, taking mean
```

```
logistic roc auc = np.mean(cross val score(logistic reg, x tr, y tr, sc
oring = 'roc auc', cv=10))
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.pv:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear_m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
```

```
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
 FutureWarning)
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
odel/logistic.py:432: FutureWarning: Default solver will be changed to
'lbfgs' in 0.22. Specify a solver to silence this warning.
  FutureWarning)
```

```
/Users/Sruti/opt/anaconda3/lib/python3.7/site-packages/sklearn/linear m
         odel/logistic.py:432: FutureWarning: Default solver will be changed to
         'lbfgs' in 0.22. Specify a solver to silence this warning.
           FutureWarning)
In [30]: print(logistic reg acc)
         print(logistic roc auc)
         0.7926804423928105
         0.8703107556427476
In [22]: #Naive Bayes
         naive bayes = GaussianNB()
         #AUC/ROC
         #calculating cv score, taking mean
         roc ac nb = np.mean(cross val score(naive bayes, x tr, y tr, scoring =
         'roc auc', cv=10))
         #Accuracy
         acc nb = np.mean(cross val score(naive bayes, x tr, y tr, scoring = 'ac
         curacy', cv=10))
         #calculating cv score, taking mean
         #10-fold for both, using built-in sklearn methods
In [25]: print(acc nb) #NB accuracy output, lower than reg
         print(roc ac nb) #NB roc/auc output, lower than req
         0.7344474902240962
         0.8080500250922787
In [26]: #Random Forest
In [7]: random forest = RandomForestClassifier()
```

```
param grid = {'n estimators': [5, 10, 20, 30, 40, 50],
        'max depth': [10, 20, 30, 40, 50, 60, 70, 80, 90],
         'max features': [5, 10, 20, 30, 40, 50] }
        #max depth: The maximum depth of the tree
        #n estimators: The number of trees in the forest.
        #max features: The number of features to consider when looking for the
         best split
        #verbose: Controls the verbosity when fitting and predicting
        #n iobs: # of iobs to run in parallel. -1 means using all processors
        random forest grid = GridSearchCV(estimator = random forest, param grid
         = param grid,
        cv = 10, n jobs = -1, verbose = 2)
        random forest grid.fit(x tr, y tr)
        Fitting 10 folds for each of 324 candidates, totalling 3240 fits
        [Parallel(n jobs=-1)]: Using backend LokyBackend with 4 concurrent work
        ers.
        [Parallel(n jobs=-1)]: Done 33 tasks
                                                     elapsed:
                                                                 5.5s
        [Parallel(n jobs=-1)]: Done 230 tasks
                                                     elapsed: 15.8s
                                                    | elapsed: 41.4s
        [Parallel(n jobs=-1)]: Done 636 tasks
        [Parallel(n jobs=-1)]: Done 1075 tasks
                                                    I elapsed: 1.2min
        [Parallel(n jobs=-1)]: Done 1581 tasks
                                                      elapsed: 1.8min
        [Parallel(n jobs=-1)]: Done 2249 tasks
                                                     | elapsed: 2.6min
        [Parallel(n jobs=-1)]: Done 2859 tasks
                                                    I elapsed: 3.4min
        [Parallel(n jobs=-1)]: Done 3240 out of 3240 | elapsed: 3.9min finishe
Out[7]: GridSearchCV(cv=10, error score='raise-deprecating',
                     estimator=RandomForestClassifier(bootstrap=True, class wei
        ght=None,
                                                      criterion='gini', max dep
        th=None,
                                                      max features='auto',
                                                      max leaf nodes=None,
                                                      min impurity decrease=0.
```

```
υ,
                                                      min impurity split=None,
                                                      min samples leaf=1,
                                                      min samples split=2,
                                                      min weight fraction leaf=
        0.0,
                                                      n estimators='warn', n jo
        bs=None,
                                                      oob score=False,
                                                      random state=None, verbos
        e=0,
                                                      warm start=False),
                     iid='warn', n jobs=-1,
                     param grid={'max depth': [10, 20, 30, 40, 50, 60, 70, 80,
        90],
                                 'max features': [5, 10, 20, 30, 40, 50],
                                 'n estimators': [5, 10, 20, 30, 40, 50]},
                     pre dispatch='2*n jobs', refit=True, return train score=Fa
        lse,
                     scoring=None, verbose=2)
In [8]: random forest grid.best params #using these 'best' in next, final ste
Out[8]: {'max depth': 10, 'max features': 10, 'n estimators': 40}
In [9]: random forest final = RandomForestClassifier(n estimators=40, max depth
        =10, max features=10)
        #Accuracy
        ##calculating cv score, taking mean
        rf accuracy = np.mean(cross val score(random forest final, x tr, y tr,
        scoring = 'accuracy', cv=10))
        #AUC/ROC
        #calculating cv score, taking mean
```

```
rf roc auc = np.mean(cross val score(random forest_final, x_tr, y_tr, s
         coring = 'roc auc', cv=10))
In [10]: print(rf accuracy) #random forest accuracy; better than nb
         print(rf roc auc) #random forest auc/roc; better than nb
         0.7919633371215347
         0.8774826682371953
In [5]: #Decision tree
         decision tree = DecisionTreeClassifier()
         #Accuracy
         ##calculating cv score, taking mean
         decision tree acc = np.mean(cross val score(decision tree, x tr, y tr,
         scoring = 'accuracy', cv=10))
         #AUC/ROC
         #calculating cv score, taking mean
         dt roc auc = np.mean(cross val score(decision tree, x tr, y tr, scoring
          = 'roc auc', cv=10))
In [6]: print(decision tree acc) #decision tree accuracy; roughly the same as n
         print(dt roc auc) #decision tree roc/auc; not as good as nb or random f
         orest
         0.7303381555778488
         0.7184698869205912
In [11]: #Elastic net regression
         \#Tuned\ alpha\ and\ l1,\ ratio = 0.5\ and\ alpha = 0.004
         tune = ElasticNetCV(cv=10)
         tune.fit(x tr, y tr)
         alpha = tune.alpha
```

```
l1 = tune.l1 ratio
         print(alpha, l1)
         0.0038452641680228584 0.5
In [12]: #using the alpha and l1 obtained above
         elastic net = ElasticNet(alpha=0.0038452641680228584, l1 ratio=0.5)
         #regression, mse
         elastic net acc = np.mean(cross val score(elastic net, x tr, y tr, scor
         ing='neg mean squared error', cv=10))
         #AUC/ROC still
         en roc auc= np.mean(cross val score(elastic net, x tr, y tr, scoring =
         'roc auc', cv=10))
In [14]: \#elastic\ net\ acc = 0.1471453221731916, using mse, elastic net accuracy
         #en roc auc = 0.8740225489138439, elastic net roc/auc; almost as high a
         s rf
In [16]: #Bagging
         #staying consistent with n estimators from random forest
         param grid = {'n estimators': [5, 10, 20, 30, 40, 50]}
In [17]: bagging = BaggingClassifier()
         bagging grid = GridSearchCV(estimator = bagging, param grid = param gri
         d.
         cv = 10, n jobs = -1, verbose = 2)
         #max depth: The maximum depth of the tree
         #n estimators: The number of trees in the forest.
         #max features: The number of features to consider when looking for the
          best split
         #verbose: Controls the verbosity when fitting and predicting
         #n jobs: # of jobs to run in parallel, -1 means using all processors
```

```
bagging grid.fit(x tr, y tr)
         Fitting 10 folds for each of 6 candidates, totalling 60 fits
         [Parallel(n jobs=-1)]: Using backend LokyBackend with 4 concurrent work
         ers.
         [Parallel(n jobs=-1)]: Done 33 tasks
                                                    I elapsed:
                                                                  7.6s
         [Parallel(n jobs=-1)]: Done 60 out of 60 | elapsed: 12.9s finished
Out[17]: GridSearchCV(cv=10, error score='raise-deprecating',
                      estimator=BaggingClassifier(base estimator=None, bootstrap
         =True,
                                                  bootstrap features=False,
                                                  max features=1.0, max samples=
         1.0.
                                                  n estimators=10, n jobs=None,
                                                  oob score=False, random state=
         None,
                                                  verbose=0, warm start=False),
                      iid='warn', n jobs=-1,
                      param grid={'n estimators': [5, 10, 20, 30, 40, 50]},
                      pre dispatch='2*n jobs', refit=True, return train score=Fa
         lse,
                      scoring=None, verbose=2)
In [18]: bagging grid.best params #using this in next, final step
Out[18]: {'n estimators': 40}
In [19]: bagging fit = BaggingClassifier(n estimators=40)
         #Accuracy
         ##calculating cv score, taking mean
         bagging acc = np.mean(cross val score(bagging fit, x tr, y tr, scoring
         = 'accuracy', cv=10))
         #AUC/ROC
         ##calculating cv score, taking mean
```

```
b_roc_auc = np.mean(cross_val_score(bagging_fit, x_tr, y_tr, scoring =
         'roc auc', cv=10))
In [20]: print(bagging acc) #bagging accuracy, a little lower than rf
         print(b roc auc) #bagging roc/auc; almost as high as rf, higher than el
         astic net
         0.7763816754708414
         0.8749782762509121
In [21]: #Gradient Boosting
         #keeping n estimators consistent with rf and bagging
         param grid = {'n estimators': [5, 10, 20, 30, 40, 50], 'learning rate':
          [0.1, 0.4, 0.7, 1], 'max features': [None, 'sqrt']}
In [22]: grad boost = GradientBoostingClassifier()
         grad boost grid = GridSearchCV(estimator = grad boost, param grid = par
         am grid,
         cv = 10, n jobs = -1, verbose = 2)
         #max depth: The maximum depth of the tree
         #n estimators: The number of trees in the forest.
         #max features: The number of features to consider when looking for the
          best split
         #verbose: Controls the verbosity when fitting and predicting
         #n jobs: # of jobs to run in parallel, -1 means using all processors
         grad boost grid.fit(x tr, y tr)
         Fitting 10 folds for each of 48 candidates, totalling 480 fits
         [Parallel(n jobs=-1)]: Using backend LokyBackend with 4 concurrent work
         ers.
         [Parallel(n jobs=-1)]: Done 108 tasks
                                                                  4.9s
                                                    | elapsed:
         [Parallel(n jobs=-1)]: Done 480 out of 480 | elapsed: 16.7s finished
Out[22]: CridCoarch(V/ov=10 array scare=!roica doprocating!
```

```
vur[22]: GridSearchCv(Cv=i0, error_score= raise-deprecating ,
                      estimator=GradientBoostingClassifier(criterion='friedman m
         se',
                                                            init=None, learning r
         ate=0.1,
                                                            loss='deviance', max
         depth=3,
                                                            max features=None,
                                                            max leaf nodes=None,
                                                            min impurity decrease
         =0.0,
                                                            min impurity split=No
         ne,
                                                            min samples leaf=1,
                                                            min samples split=2,
                                                            min weight fraction l
         eaf=0.0,
                                                            n estimators=100,
                                                            n iter no change=Non
         e,
                                                            presort='auto',
                                                            random state=None,
                                                            subsample=1.0, tol=0.
         0001,
                                                            validation fraction=
         0.1,
                                                            verbose=0, warm start
         =False),
                      iid='warn', n jobs=-1,
                      param grid={'learning rate': [0.1, 0.4, 0.7, 1],
                                   'max features': [None, 'sqrt'],
                                   'n estimators': [5, 10, 20, 30, 40, 50]},
                      pre dispatch='2*n jobs', refit=True, return train score=Fa
         lse,
                      scoring=None, verbose=2)
In [23]: grad boost grid.best params #using these in next, final step
Out[23]: {'learning rate': 0.1, 'max features': None, 'n estimators': 50}
```

```
In [25]: grad boost fit = GradientBoostingClassifier(learning rate=0.1, max feat
         ures='sqrt', n estimators=50)
         #Accuracy
         ##calculating cv score, taking mean
         grad acc = np.mean(cross val score(grad boost fit, x tr, y tr, scoring
         = 'accuracy', cv=10))
         #AUC/ROC
         ##calculating cv score, taking mean
         grad roc auc= np.mean(cross val score(grad boost fit, x tr, y tr, scori
         nq = 'roc auc', cv=10)
In [26]: print(grad acc) #gradient boost accuracy - higher than rf
         print(grad roc auc) #gradient boost roc/auc - slightly lower than rf
         0.8021627606239304
         0.874622962550528
            3. Evaluate the models (20 points) Compare and present each mode
            l's (training) performance based on
            - Cross-validated error rate
            - ROC/AUC
In [ ]: #Accuracy
         cver = list(1 - np.array([0.79268, 0.73445, 0.853, 0.73034, 0.77642, 0.
         79196. 0.802221))
         #listing all the error scores we've obtained, 1-acc for each model outp
         11t
         #elastic net = 1-mse output
In [36]: model = ['logistic', 'nb', 'elastic', 'decision tree', 'bagging', 'rand
```

```
om forest', 'boosting']
#all the models I ran

#graphing
plt.plot(model, cver, marker='x', color='red')

plt.xlabel('model type')
plt.ylabel('cv error rate')
plt.title('Comparing CV error rate and model type');
```

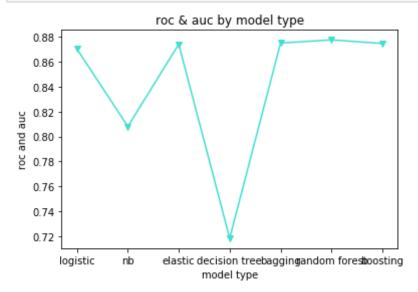
## O.26 - O.24 - O.20 - O.18 - O.16 - O.

```
In [ ]: #AUC/ROC

#all the auc/roc i've obtained
roc_auc = [0.8703, 0.8081, 0.8740, 0.7185, 0.8750, 0.8775, 0.8746]

#all the models I ran
model = ['logistic', 'nb', 'elastic', 'decision tree', 'bagging', 'rand
om forest', 'boosting']
```

```
plt.xlabel('model type')
plt.ylabel('roc and auc')
plt.title('roc & auc by model type');
```



4. (15 points) Which is the best model? Defend your choice.

Based on both error plots: boosting has the lowest cv error rate (described in terms of acc) and the third highest roc/auc (though, very close to the two highest: random forest and bagging, which is why I'd still consider it the best). Logistic regression also performs very well (very low cv error rate, very high roc/auc). Elastic net had very low mse, but extremely low roc/auc.

5. Evaluate the best model (15 points) Evaluate the final, best model's (selected in 4) performance on the test set (the test . csv) by calculating and presenting the classification error rate and AUC. Compared to the fit evaluated on the training set in q

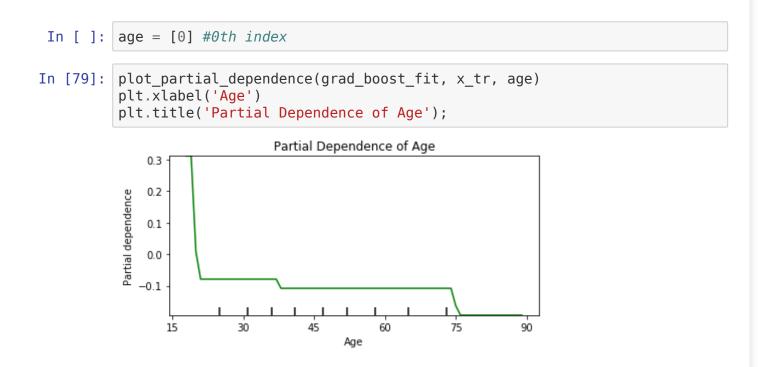
```
In [67]: grad boost fit.fit(x tr, y tr) #using the same fit function from earlie
Out[67]: GradientBoostingClassifier(criterion='friedman mse', init=None,
                                     learning rate=0.2, loss='deviance', max dept
         h=3,
                                     max features='sqrt', max leaf nodes=None,
                                     min impurity decrease=0.0, min impurity spli
         t=None,
                                     min samples leaf=1, min samples split=2,
                                     min weight fraction leaf=0.0, n estimators=4
         Θ,
                                     n iter no change=None, presort='auto',
                                     random state=None, subsample=1.0, tol=0.000
         1,
                                     validation fraction=0.1, verbose=0,
                                     warm start=False)
In [71]: #fitting to test data and calculating corresponding acc and auc/roc sco
         res:
         test error qb= 1 - accuracy score(Y te, grad boost fit.predict(X te))
         gb roc auc= roc auc score(Y te, grad boost fit.predict(X te))
In [72]: print(test error qb) #(test) gradient boost accuracy
         print(gb roc auc) #test auc roc gradient boost
         0.21501014198782964
         0.7776481297583582
         The "best" model, gradient boost, doesn't generalize as well - the test roc/auc (0.778) is lower
```

uestions 3-4, does the "best" model generalize well? Why or why

not? How do you know?

than the training roc/auc (.8768322053533322), which suggests that the model overfit to the training data.

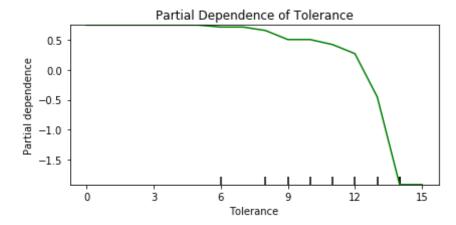
6. Bonus: PDPs/ICE (Up to 5 extra points) Present and substantively interpret the "best" model (selected in question 4) using PD Ps/ICE curves over the range of: tolerance and age. Note, interpretation must be more than simple presentation of plots/curves. You must sufficiently describe the changes in probability estimates over the range of these two features. You may earn up to 5 extra points, where partial credit is possible if the solution is insufficient along some dimension (e.g., technically/code, interpretation, visual presentation, etc.).



Age doesn't seem to be affecting colrac very much (no clear positive or negative correlation from

plot), partial dependence is pretty much the same across age, save from roughly 15-18 where it starkly decreases.

```
In []: features = [32] #32nd index (used iloc to determine)
In [84]: plot_partial_dependence(grad_boost_fit, x_tr, features)
    plt.xlabel('Tolerance')
    plt.title('Partial Dependence of Tolerance');
```



Looks like there's a strong negative correlation here (as tolerance increases, partial dependence decreases -> values given for colrac decrease - in other words, higher tolerance generally links with the opinion that racist profs should not be allowed to teach.

```
In [ ]:
```