```
In [110]:
          Regina Catipon
          MACS 30100
          2/29/2020
          import pandas as pd
          import numpy as np
          import matplotlib.pyplot as plt
          from sklearn.model_selection import cross_val_score
          from sklearn.linear_model import LogisticRegression, ElasticNetCV, Elast
          icNet
          from sklearn.naive bayes import GaussianNB
          from sklearn.tree import DecisionTreeClassifier
          from sklearn.ensemble import RandomForestClassifier, BaggingClassifier,
          GradientBoostingClassifier
          from sklearn.model selection import RandomizedSearchCV, GridSearchCV
          from sklearn.metrics import accuracy score, roc_curve, roc_auc_score, au
          #from sklearn.inspection import plot partial dependence
```

Conceptual: Cost functions for classification trees

1. (15 points) Consider the Gini index, classification error, and cross-entropy in simple classification settings with two classes. Of these three possible cost functions, which would be best to use when growing a decision tree? Which would be best to use when pruning a decision tree? Why?

Because classification error is simply the fraction of misclassified training observations it is not sensitive enough for tree growing. The other two impurity measures, the Gini index and cross-entropy are considered to be best because they control for variance across the classes which helps to optimize splitting for growth. For pruning, classification error is considered to be an appropriate measure because it prioritizes accuracy.

Application: Predicting attitudes towards racist college professors

Estimate the models

2. (35 points; 5 points/model) Estimate the following models, predicting colrac using the training set (the training .csv) with 10-fold CV:

- Logistic regression
- Naive Bayes
- Elastic net regression
- Decision tree (CART)
- Bagging
- Random forest
- Boosting

Tune the relevant hyperparameters for each model as necessary. Only use the tuned model with the best performance for the remaining exercises. Be sure to leave sufficient time for hyperparameter tuning. Grid searches can be computationally taxing and take quite a while, especially for tree-aggregation methods.

```
In [86]: #load data
    train = pd.read_csv("./data/gss_train.csv")
    test = pd.read_csv("./data/gss_test.csv")

In [42]: #inspect
    train.head()
    #don't have to check for nulls because of preprocessinh
```

Out[42]:

	age	attend	authoritarianism	black	born	childs	colath	colrac	colcom	colmil	 partyid_
0	21	0	4	0	0	0	1	1	0	1	
1	42	0	4	0	0	2	0	1	1	0	
2	70	1	1	1	0	3	0	1	1	0	
3	35	3	2	0	0	2	0	1	0	1	
4	24	3	6	0	1	3	1	1	0	0	

5 rows × 56 columns

```
In [16]: # dropping colrac column and set predictors
X_train = train.drop(['colrac'], axis=1)
X_test = test.drop(['colrac'], axis=1)

#setting prediction output to colrac
y_train, y_test = train['colrac'], test['colrac']
```

Logistic regression

```
In [85]: log_reg = LogisticRegression()
         log_score = cross_val_score(log_reg, X_train,
                                    y_train, scoring = 'roc_auc', cv = 10)
         log roc = np.mean(log score)
         log accu = cross val score(naive bayes, X train,
                                    y_train, scoring = 'accuracy', cv = 10)
         log_err = np.mean(log_accu)
         print("AUC/ROC", log_roc)
         print("Error", log_err)
         /Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line
         ar model/logistic.py:432: FutureWarning: Default solver will be changed
```

to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar_model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar_model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/line ar model/logistic.py:432: FutureWarning: Default solver will be changed to 'lbfgs' in 0.22. Specify a solver to silence this warning.

FutureWarning)

AUC/ROC 0.8703107556427476 Error 0.7344474902240962

Naive Bayes

AUC/ROC 0.8080500250922787 Accuracy 0.7344474902240962

Elasticnet Regression

```
In [87]: #Elastic net regression
         elas = ElasticNetCV(cv=10)
         elas.fit(X train, y train)
         # have to tune alpha and 11
         print( elas.alpha , elas.ll ratio)
         0.0038452641680228584 0.5
In [41]: #using that alpha and 11 ratio
         elas best = ElasticNet(alpha = 0.0038452641680228584, 11 ratio=0.5)
         # is MSE best?
         elas score = cross val score(elas best, X train, y train,
                                    scoring = 'neg mean squared error', cv=10)
         elas mse = np.mean(elas score)
         #AUC/ROC
         elas_score = cross_val_score(elas_best, X_train, y_train,
                                    scoring = 'roc auc', cv=10)
         elas roc = np.mean(elas roc)
         print("AUC/ROC", elas roc)
         print("MSE", -1*elas mse)
```

AUC/ROC 0.8740225489138439 MSE 0.1471453221731916

Decison Tree (CART)

AUC/ROC 0.7217232298218214 Accuracy 0.7174588881444107

Bagging

```
In [47]: #Bagging, but what is the base?
         bagging = BaggingClassifier()
         param grid = {'n estimators': [5, 10, 15, 20, 25, 30, 35, 40, 45, 50]}
         #Gridsearch?
         search = GridSearchCV(estimator = bagging, param grid = param grid,
                               cv = 10, n jobs=-1, verbose = 2)
         search.fit(X train, y train)
         search.best params
         #results = model selection.cross val score(bagging, X train, y train, cv
         = search)
         Fitting 10 folds for each of 10 candidates, totalling 100 fits
         [Parallel(n jobs=-1)]: Using backend LokyBackend with 4 concurrent work
         ers.
         [Parallel(n jobs=-1)]: Done 93 out of 100 | elapsed: 9.4s remainin
               0.7s
         [Parallel(n jobs=-1)]: Done 100 out of 100 | elapsed: 10.2s finished
Out[47]: {'n estimators': 30}
In [48]: # taking those number of estimators
         bagging best = BaggingClassifier(n estimators=30)
```

AUC/ROC 0.8705380367452802 Accuracy 0.7818464643248919

Random Forest

Fitting 10 folds for each of 400 candidates, totalling 4000 fits [Parallel(n jobs=-1)]: Using backend LokyBackend with 4 concurrent work ers. [Parallel(n jobs=-1)]: Done 33 tasks elapsed: 10.7s [Parallel(n jobs=-1)]: Done 270 tasks elapsed: 17.7s [Parallel(n_jobs=-1)]: Done 676 tasks elapsed: 32.3s [Parallel(n_jobs=-1)]: Done 1242 tasks elapsed: 52.2s | elapsed: 1.4min [Parallel(n jobs=-1)]: Done 1972 tasks [Parallel(n jobs=-1)]: Done 2862 tasks elapsed: 2.2min [Parallel(n_jobs=-1)]: Done 3916 tasks | elapsed: 3.2min [Parallel(n jobs=-1)]: Done 4000 out of 4000 | elapsed: 3.3min finishe d Out[55]: {'max depth': 8, 'max features': 25, 'n estimators': 35}

```
In [96]: random_forest_best = RandomForestClassifier(max_depth= 8, max_features=
         25, n_estimators=35)
         #AUC/ROC
         rf_score = cross_val_score(random_forest_best, X_train, y_train,
                                    scoring = 'roc_auc', cv=10)
         rf_roc = np.mean(rf_score)
         #Error
         rf_accu = cross_val_score(bagging_best, X_train, y_train,
                                    scoring = 'accuracy', cv=10)
         rf_err = np.mean(rf_accu)
         #roc a bye baby
         print("AUC/ROC", rf_roc)
         print("Accuracy", rf_err)
         AUC/ROC 0.8798170843241266
         Accuracy 0.7750302007253109
In [59]: X_train.shape
Out[59]: (1476, 55)
```

Gradient Boosting

```
In [78]: gradient = GradientBoostingClassifier()
         param_grid = { 'max_features': [10,20,30,40,50],
                       'learning_rate': [.2,.4,.6,.8,1],
                       'n_estimators': [10,20,30,40,50]
                      }
         gradient_search = GridSearchCV(estimator = gradient, param grid = param g
         rid,
                                      cv = 10, n jobs = -1, verbose = 2)
         #fit the model
         gradient search.fit(X train,y train)
         gradient_search.best_params_
         Fitting 10 folds for each of 125 candidates, totalling 1250 fits
         [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent work
         [Parallel(n_jobs=-1)]: Done 33 tasks
                                                    elapsed:
                                                                 9.6s
         [Parallel(n_jobs=-1)]: Done 245 tasks
                                                    elapsed:
                                                                18.3s
         [Parallel(n jobs=-1)]: Done 651 tasks
                                                    elapsed:
                                                                36.7s
                                                    elapsed:
         [Parallel(n_jobs=-1)]: Done 1217 tasks
                                                                 55.1s
         [Parallel(n_jobs=-1)]: Done 1243 out of 1250 | elapsed: 56.5s remaini
                0.3s
         ng:
         [Parallel(n jobs=-1)]: Done 1250 out of 1250 | elapsed: 56.8s finishe
Out[78]: {'learning rate': 0.2, 'max_features': 30, 'n_estimators': 40}
In [80]: gradient best = GradientBoostingClassifier(learning rate = 0.2,
                                                   max features = 30,
                                                  n = 40
```

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/mode l_selection/_split.py:1978: FutureWarning: The default value of cv will change from 3 to 5 in version 0.22. Specify it explicitly to silence th is warning.

warnings.warn(CV WARNING, FutureWarning)

/Users/reginacatipon/anaconda3/lib/python3.7/site-packages/sklearn/mode l_selection/_split.py:1978: FutureWarning: The default value of cv will change from 3 to 5 in version 0.22. Specify it explicitly to silence th is warning.

warnings.warn(CV_WARNING, FutureWarning)

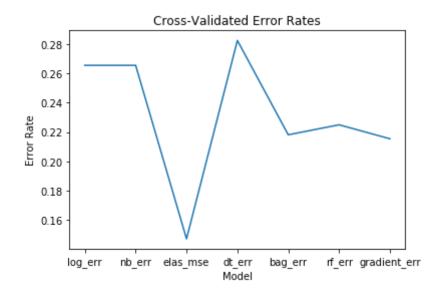
AUC/ROC 0.8689044470809119 Accuracy 0.7845701510414426

Evaluate the models

- 3. (20 points) Compare and present each model's (training) performance based on
 - Cross-validated error rate
 - ROC/AUC

```
In [153]: #Graph
    plt.plot(model_names,err_rates)
    plt.xlabel('Model')
    plt.ylabel('Error Rate')
    plt.title('Cross-Validated Error Rates')
```

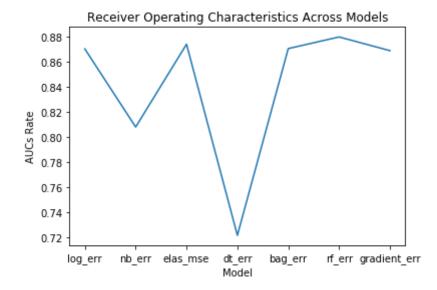
Out[153]: Text(0.5, 1.0, 'Cross-Validated Error Rates')



The lowest error rate was the Elasticnet classifier, the highest was the bagging classifier.

```
In [158]: AUCs = [log_roc, nb_roc, elas_roc, dt_roc, bag_roc, rf_roc, gradient_roc
]
In [161]: #Graph AUC/ROC comparison
plt.plot(model_names,AUCs)
plt.xlabel('Model')
plt.ylabel('AUCs Rate')
plt.title('Receiver Operating Characteristics Across Models')
```

Out[161]: Text(0.5, 1.0, 'Receiver Operating Characteristics Across Models')



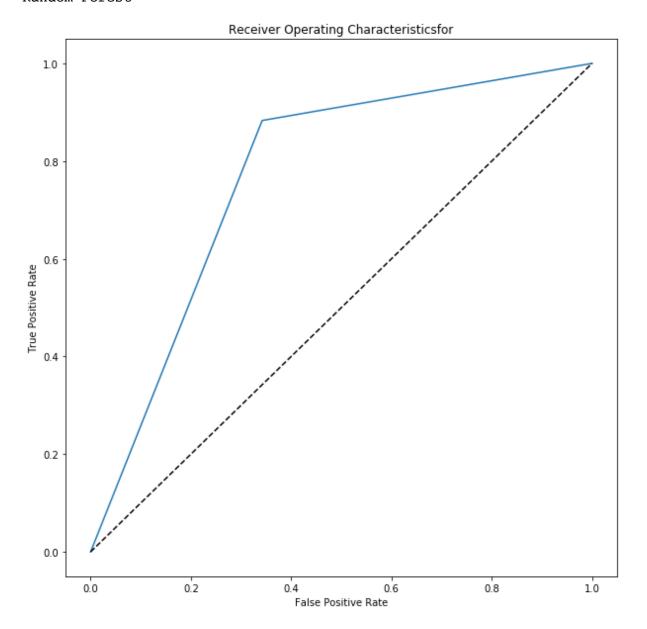
From the graph, it looks like Random Forest performed had the higest AUC.

4.(15 points) Which is the best model? Defend your choice.

```
In [160]: def plot_ROC(model):
              aucVals = []
              #Get the ROC curve
              model.fit(X_train,y_train)
              fpr, tpr, thresholds = roc_curve(y_test, model.predict(X_test))
              auc = metrics.auc(fpr, tpr)
              aucVals.append(auc)
              #setup axis for plotting
              fig, ax = plt.subplots(figsize = (10,10))
              #Plot the class's line
              ax.plot(fpr, tpr, auc)
              #display
              ax.set_title('Receiver Operating Characteristics')
              plt.plot([0,1], [0,1], color = 'k', linestyle='--')
              ax.set_xlabel('False Positive Rate')
              ax.set_ylabel('True Positive Rate')
              plt.show()
              plt.close()
              #return aucVals
```

```
In [149]: #Graph ROC/AUC
    print('')
    print('Random Forest')
    plot_ROC(random_forest_best)
```

Random Forest



The model that did the best was the Random Forest classifier. It scored an AUC/ROC rate of 0.879. While simpler models like Logistic Regression actually scored pretty close with 0.870, Random Forest also had one of the highest accuracy scores, second only to the Gradient Boosting in clssification error rate.

```
In [ ]:
```

Evaluate the best model

5. (15 points) Evaluate the final, best model's (selected in 4) performance on the test set (the test .csv) by calculating and presenting the classification error rate and AUC. Compared to the fit evaluated on the training set in questions 3-4, does the "best" model generalize well? Why or why not? How do you know?

```
In [91]: random_forest_best.fit(X_train, y_train)
    pred = random_forest_best.predict(X_test)

In [95]: #Accuracy
    accuracy = accuracy_score(y_test, pred)
    print(accuracy)

    0.7971602434077079

In [93]: #ROC/AUC
    roc = roc_auc_score(y_test, pred)
    print(roc)

    0.788356504468719
```

I think the model does an average job at generalizing. For example, the Naive Bayes classification, which is sometimes used as a baseline, had a ROC/AUC of 0.81 and an accuracy of 0.73. The ROC/AUC from the predicted y using the tuned Random Forest classification model was a little lower than the Naive Bayes rate at 0.79, and an accuracy score was a little higher than . It, of course, did not outperform the training results, but its accuracy was close to, if not sometimes better, than the training set fits.

```
In [ ]:
```