

CS273 Midterm Exam
Introduction to Machine Learning: Winter 2015
Tuesday February 10th, 2014

Your name:

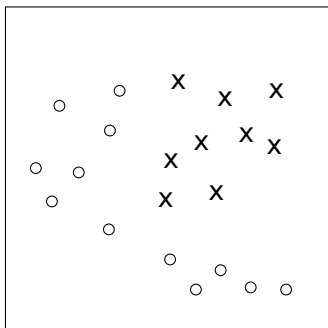
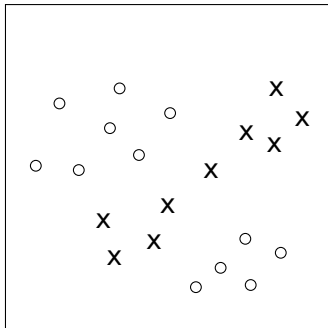
Your UCINetID (e.g., myname@uci.edu):

Your seat (row and number):

- Total time is 80 minutes. **READ THE EXAM FIRST** and organize your time; don't spend too long on any one problem
- Please **write clearly** and **show all your work**.
- If you need clarification on a problem, please raise your hand and wait for the instructor to come over.
- Turn in any scratch paper with your exam.

Problem 1: (8 points) Separability and Features

For each of the following examples of training data, **(1)** sketch a classification boundary that separates the data; **(2)** state whether or not the data are linearly separable, and if not, **(3)** give a set of features that would allow the data to be separated. (Your features do not need to be minimal, but should not contain any obviously unneeded features.)



Problem 2: (8 points) Under- and Over-fitting

Suppose that I am training a neural network classifier to recognize faces in images. Using cross-validation, we discover that my classifier appears to be overfitting the data. Give two ways I could improve my performance – be specific.

After following some of your advice, we now think that the resulting classifier is underfitting. Give two ways, **other than** reversing the methods you mentioned above, that we could improve performance; again, be specific.

Problem 3: (9 points) Bayes Classifiers and Naïve Bayes

Consider the table of measured data given at right. We will use the two observed features x_1, x_2 to predict the class y . In the case of a tie, we will prefer to predict class $y = 0$.

x_1	x_2	y
0	0	1
0	0	1
0	1	1
0	0	0
1	1	0
1	0	0
0	1	1
0	1	1

- (a) Write down the probabilities necessary for a naïve Bayes classifier:

- (b) Using your naïve Bayes model, what value of y is predicted given observation $(x_1, x_2) = (00)$?

- (c) Using your naïve Bayes model, what is the probability $p(y = 1 | x_1 = 0, x_2 = 1)$?

Problem 4: (10 points) Gradient Descent

Suppose that we have training data $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), \dots, (x^{(m)}, y^{(m)})\}$ and we wish to predict y using a nonlinear regression model with two parameters:

$$\hat{y} = a \exp(x_1 + b)$$

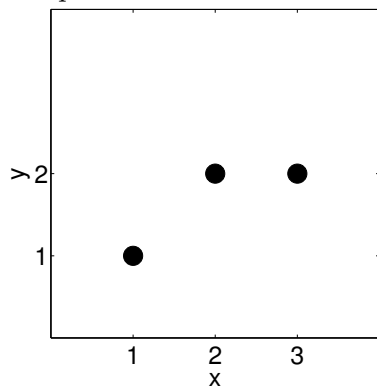
We decide to train our model using gradient descent on the mean squared error (MSE).

- [illegible]

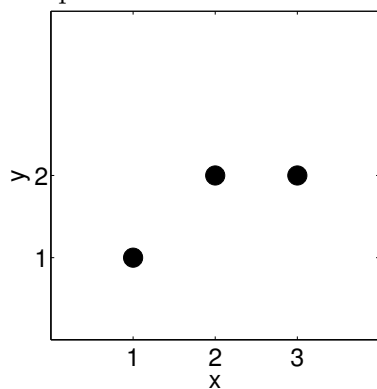
Problem 5: (8 points) Cross-validation and Linear Regression

Consider the following data points, copied in each part. We wish to perform linear regression to minimize mean squared error.

- (a) Compute the leave-one-out cross-validation error of a zero-order (constant) predictor.

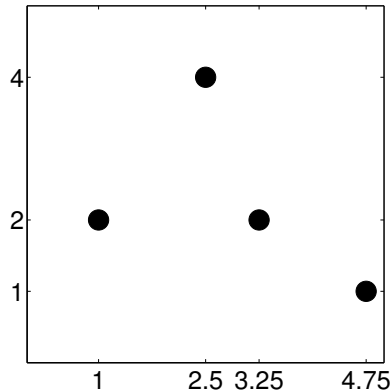


- (b) Compute the leave-one-out cross-validation error of a first-order (linear) predictor.



Problem 6: (12 points) K-Nearest Neighbor Regression

Consider a regression problem for predicting the following data points, using the k-nearest neighbor regression algorithm to minimize mean squared error (MSE). In the case of ties, we will prefer to use the neighbor to the left (smaller x value). Note: if you prefer, you may leave an arithmetic expression, e.g., leave values as $(.6)^2$.



- (a) For $k = 1$, compute the training error on the provided data.

- (b) For $k = 1$, compute the leave-one-out cross-validation error on the data.

- (c) For $k = 3$, compute the training error on the provided data.

- (d) For $k = 3$, compute the leave-one-out cross-validation error on the data.

Problem 7: (4 points) Multiple Choice

For the following questions, assume that we have m data points $y^{(i)}, x^{(i)}, i = 1 \dots m$, each with n features, $x^{(i)} = [x_1^{(i)} \dots x_n^{(i)}]$.

Circle one answer for each:

True or **false**: Linear regression can be solved using either matrix algebra or gradient descent.

True or **false**: The predictions of a k-nearest neighbor classifier will not be affected if we pre-process the data to normalize the magnitude of each feature.

True or **false**: With enough hidden nodes, a Neural Network can separate any data set.

True or **false**: Increasing the regularization of a linear regression model will decrease the bias.

Problem 8: (4 points) Short Answer

Give one advantage of stochastic gradient descent over batch gradient descent, **and** one advantage of batch gradient descent over stochastic.

Problem 9: (12 points) Perceptrons and VC Dimension

In this problem, consider the following perceptron model on two features:

$$\hat{y}(x) = \text{sign}(b + w_1x_1 + w_2x_2)$$

and answer the following questions about the decision boundary and the VC dimension.

- (a) Describe (in words, with diagrams if desired) the possible decision boundaries that can be realized by this classifier

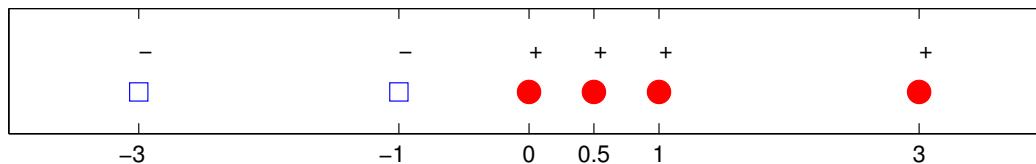
- (b) What is its VC dimension?

Now suppose that I also enforce an additional condition on the parameters of the model: that **only one** of the two weights w_1, w_2 is non-zero (i.e., one of them must be zero, a “feature selection” criterion). Note that the training algorithm can choose which parameter is zero, depending on the data.

- (c) Describe (in words, with diagrams if desired) the decision boundaries that can be realized by this classifier (there should be two “cases”).

- (d) What is its VC dimension?

Problem 10: (9 points) Support Vector Machines



Using the above data with one feature x (whose values are given below each data point) and a class variable $y \in \{-1, +1\}$, with filled circles indicating $y = +1$ and squares $y = -1$ (the sign is also shown above each data point for redundancy), answer the following:

- (a) Sketch the solution (decision boundary) of a linear SVM on the data, and identify the support vectors.
- (b) Give the solution parameters w and b , where the linear form is $wx + b$.
- (c) Calculate the training error:
- (d) Calculate the leave-one-out cross-validation error for these data: