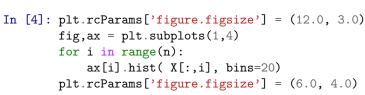
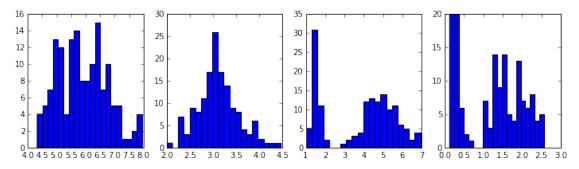
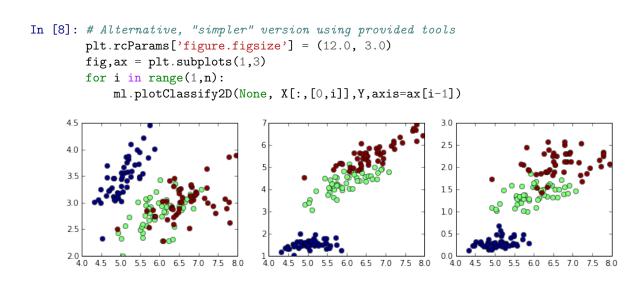
HW1s

October 6, 2016



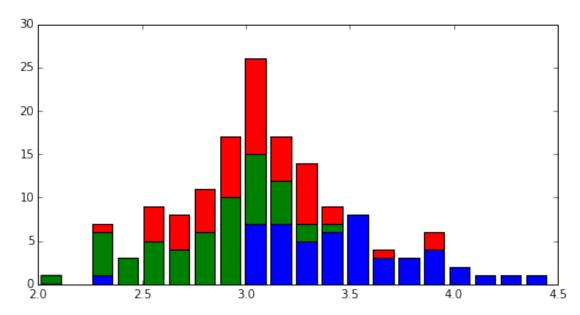


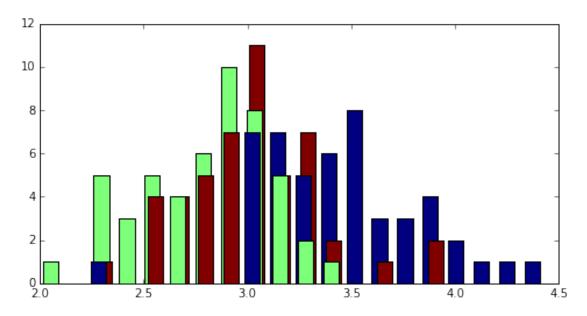
```
In [6]: Xn = X - np.mean(X,axis=0)
        print 'Normed Mean:', np.mean(Xn,axis=0)
         # The mean is now zero (up to numerical precision)
                                    3.75075346e-16 -6.42128993e-16
Normed Mean: [ 2.16043399e-15
                                                                          3.75075346e-16]
In [7]: plt.rcParams['figure.figsize'] = (12.0, 3.0)
        fig,ax = plt.subplots(1,3)
        colors = ['b','g','r']
        for i in range(1,n):
             for c in np.unique(Y):
                 ax[i-1].plot( X[Y==c,0], X[Y==c,i], 'o', color=colors[int(c)] )
     4.0
                                                                 2.0
     3.5
                                                                 1.5
     3.0
                                                                 1.0
      2.5
                                                                 0.5
                                                                 0.0 4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5 8.0
                5.5 6.0 6.5 7.0 7.5 8.0
                                     4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5 8.0
```



1.0.1 Not required

I'll also illustrate the class-specific histograms, since you may find these useful later on. We can do two different styles; a histogram of the data together, with class-specific fill colors ("plt.hist"), or a collection of class-specific histograms on the same plot ("ml.histy").





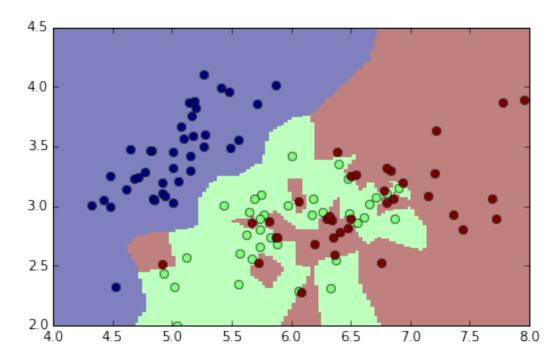
2 P2: kNN Predictions

Start by loading the data again, etc.

```
In [12]: iris = np.genfromtxt("data/iris.txt",delimiter=None)
    X,Y = iris[:,0:4], iris[:,4]
    X,Y = ml.shuffleData(X,Y)
    Xtr, Xva, Ytr, Yva = ml.splitData(X,Y, .75)
```

Now, let's plot the k-nearest neighbor decision boundary using only the first two features:

```
In [13]: knn = ml.knn.knnClassify()
    knn.train(Xtr[:,0:2],Ytr)
    knn.K = 1
    ml.plotClassify2D(knn, Xtr[:,0:2],Ytr)
```



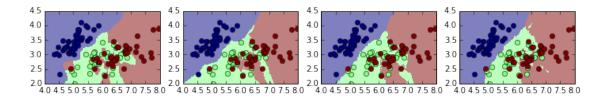
Let's compute error rates at various values of K, and visualize the decision functions as well:

```
In [14]: plt.rcParams['figure.figsize'] = (12.0, 5.0)
         fig,ax = plt.subplots(1,4)
         for i,k in enumerate([1, 5, 10, 20]):
             knn = ml.knn.knnClassify() #!!! TODO: name
             knn.train(Xtr[:,0:2],Ytr)
             knn.K = k
             print "K=",knn.K, "\t Err (Train):",knn.err(Xtr[:,0:2],Ytr), "\t Err (Val):", knn.err(Xva[
             ml.plotClassify2D(knn, Xtr[:,0:2],Ytr, axis=ax[i])
              Err (Train): 0.0
                                        Err (Val): 0.297297297
K= 1
                                                   Err (Val): 0.27027027027
K= 5
              Err (Train): 0.135135135135
               Err (Train): 0.18018018018
                                                   Err (Val): 0.378378378378
K = 10
```

Err (Val): 0.189189189189

Err (Train): 0.279279279279

K = 20



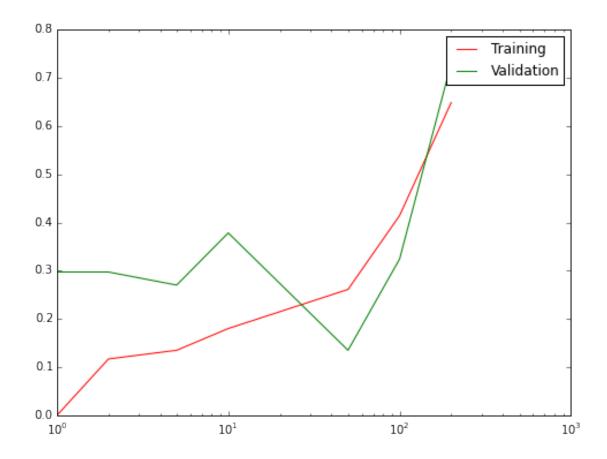
Now, compute the error rate at more values of K, and plot both the training error rate and validation error rates:

```
In [15]: #plt.figure( figsize=(8.0,6.0), )
    plt.rcParams['figure.figsize'] = (8.0, 6.0)
    fig,ax = plt.subplots(1,1)

knn = ml.knn.knnClassify(Xtr[:,0:2],Ytr)
    k_values = [1, 2, 5, 10, 50, 100, 200]
    errTr = np.zeros((len(k_values),))
    errVa = errTr.copy()
    for i,k in enumerate(k_values):
        knn.K = k
        errTr[i] = knn.err(Xtr[:,0:2],Ytr)
        errVa[i] = knn.err(Xva[:,0:2],Yva)

ax.semilogx(k_values,errTr,'r-',k_values,errVa,'g-')
    ax.legend(['Training','Validation'])
    print "Training and validation error as a function of K:"
```

Training and validation error as a function of K:



Based on this plot, k = 50 had the lowest validation error, so I would most likely choose that. You can also see evidence of overfitting (k = 1..10; low training error but high validation error) and of underfitting (k = 100 or more; similar, high training and validation errors).

Your plots may be a bit different, and end up with slightly different values of k, but most likely the trend is similar – at low k, training error is much lower than validation error, suggesting overfitting; at high k, they are similar but high, suggesting underfitting.

3 P3: Bayes Classifiers

You can most easily do this problem by hand, but I'll put it in the Python notebook.

```
In [16]: #(a)

p_y = 4.0/10; # p(y) = 4/10

# p(xi | y=-1)

p_x1_y0 = 3.0/6;

p_x2_y0 = 5.0/6;

p_x3_y0 = 4.0/6;

p_x4_y0 = 5.0/6;

p_x5_y0 = 2.0/6;

# p(xi | y=+1)

p_x1_y1 = 3.0/4;

p_x2_y1 = 0.0/4;

p_x3_y1 = 3.0/4;
```

```
p_x4_y1 = 2.0/4;
         p_x5_y1 = 1.0/4;
In [17]: # (b)
         f_y_1_00000 = p_y*(1-p_x_1_y_1)*(1-p_x_2_y_1)*(1-p_x_3_y_1)*(1-p_x_4_y_1)*(1-p_x_5_y_1)
         print "f_y1_00000 = ",f_y1_00000
          f_{y0}_{00000} = (1-p_y)*(1-p_x1_y0)*(1-p_x2_y0)*(1-p_x3_y0)*(1-p_x4_y0)*(1-p_x5_y0) 
         print "f_y0_00000 = ",f_y0_00000
         if (f_y1_00000 > f_y0_00000):
             print "Predict class +1"
         else:
             print "Predict class -1"
         print "\n\n"
         f_y_1_{11010} = p_y_{(p_x_1_y_1)*(p_x_2_y_1)*(1-p_x_3_y_1)*(p_x_4_y_1)*(1-p_x_5_y_1)}
         print "f_y1_11010 = ",f_y1_11010"
         f_y0_11010 = (1-p_y)*(p_x1_y0)*(p_x2_y0)*(1-p_x3_y0)*(p_x4_y0)*(1-p_x5_y0)
         print f_y0_{11010} = f_y0_{11010}
         if (f_y1_11010 > f_y0_11010):
             print "Predict class +1"
         else:
             print "Predict class -1"
         print "\n"
f_y1_00000 = 0.009375
f_y0_00000 = 0.00185185185185
Predict class +1
f_y1_11010 = 0.0
f_y0_111010 = 0.0462962962963
Predict class -1
In [18]: # (c)
         # p(y1/11010) =
         print "p(y=1|11010) = ", f_y1_11010 / (f_y1_11010 + f_y0_11010)
         print "\n"
         # For the other pattern (not required), p(y1/00000) =
         print "p(y=1|00000) =", f_y1_00000 / (f_y1_00000 + f_y0_00000)
p(y=1|11010) = 0.0
p(y=1|00000) = 0.835051546392
```

(d) A Bayes classifier using a joint distribution model for p(x|y=c) would have $2^5-1=31$ degrees of freedom (independent probabilities) to estimate; here we have only 6 and 4 data points respectively. So such a model would be extremely unlikely to generalize well to new data.