

Enrollment No.....



Faculty of Management Studies

End Sem Examination Dec 2024

MS3CO32 Elementary Mathematics & Statistics

Programme: BBA

Branch/Specialisation: Management

Duration: 3 Hrs.

Maximum Marks: 60

Note: All questions are compulsory. Internal choices, if any, are indicated. Answers of Q.1 (MCQs) should be written in full instead of only a, b, c or d. Assume suitable data if necessary. Notations and symbols have their usual meaning.

		Marks	BL	PO	CO	PSO
Q.1	i. If $x:6 = 55:11$ then value of x is_____.	1	02	01	02	
	(a) 30 (b) 33					
	(c) 34 (d) None of these					
	ii. Formula of Simple Interest is_____.	1	01	01	01	
	(a) $P + R + T$ (b) $\frac{PRT}{100}$					
	(c) PRT (d) None of these					
	iii. If $A = \{a, e, i, o, u\}$ and $B = \{a, b\}$ then value $(A \cap B)$ is_____.	1	02	02	02	
	(a) $\{a, e, i, o, u, b\}$ (b) $\{a, e, b\}$					
	(c) $\{a\}$ (d) None of these					
	iv. $A = \{x: x \neq x\}$ is-	1	02	02	01	
	(a) Singleton set (b) Empty set					
	(c) Finite set (d) None of these					
	v. Which of the following is example of reflexive relation?	1	02	01	01	
	(a) $\{(1, 1), (2, 3), (3, 2)\}$					
	(b) $\{(1, 2), (2, 3), (3, 1)\}$					
	(c) $\{(1, 1), (2, 1), (1, 2)\}$					
	(d) None of these					
	vi. Let $f(x) = 2 + x$ then value $f(-1)$ is-	1	03	03	04	
	(a) 1 (b) 0 (c) 2 (d) None of these					
	vii. Value of 4P_4 is-	1	03	05	04	
	(a) 22 (b) 24 (c) 26 (d) None of these					

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viii.	Value of $\frac{7!}{6!}$ is -	1	03	05	04
	(a) 1 (b) 7 (c) 6 (d) None of these.				
ix.	General formula of arithmetic mean is-	1	02	01	01
	(a) $\frac{a+b}{2}$ (b) $a + b$				
	(c) $\frac{a}{2}$ (d) None of these				
x.	Geometric Mean of 'x' and $\frac{1}{x}$ is-	1	03	01	01
	(a) 1 (b) ± 1 (c) -1 (d) None of these				
Q.2	i. Evaluate $\{15 \times 32 \div 2 \times 5\} \div 75$.	2	05	07	04
	ii. Three students contested an election and received 1000, 5000 and 10000 votes respectively. What is the percentage of the total votes the winning student gets?	3	03	03	03
	iii. The ratio of ages of Abha and her mother is 2:5. at the time of Abha's birth her mother age was 27 years. Find the present ages of Abha and her mother.	5	03	02	03
OR	iv. What sum of money will produce Rs.28,600 as an interest in 3 years and 3 months at 2.5% per annum simple interest?	5	03	02	03
Q.3	Attempt any two:				
	i. Define set and its types (any four).	5	01	01	01
	ii. Draw the Venn diagram for the following- (a) $(A \cup B) \cap (A \cup C)$ (b) $A' \cap (C - B)$	5	02	02	03
	iii. If $A = \{a, b, c, d, e\}$, $B = \{a, c, e, g\}$ and $C = \{b, e, f, g\}$ then prove that- (a) $A \cap (B - C) = (A \cap B) - (A \cap C)$ (b) $A - (B \cap C) = (A - B) \cup (A - C)$	5	03	04	03
Q.4	Attempt any two:				
	i. Determine whether the following relation R on set A are reflexive, symmetric and transitive, where $A = \{2, 3, 4\}$ and $R = \{(2, 2), (3, 3), (4, 4), (2, 3), (3, 4)\}$.	5	03	01	02

[3]

	ii.	A publisher house finds that the production of cost directly attributed to each book is Rs.30 and that the fixed cost are Rs.15,000. If each book can be sold for Rs.45 then determine - (a) The cost function (b) The revenue function (c) The break-even point	5	03	02	03
	iii.	Define Function. Write any four types of function with example.	5	02	01	01
Q.5	i.	A student has 10 text books and 8 other books. In how many ways can he selected 4 text books and 3 other books?	4	03	03	03
	ii.	Find the middle term in the expansion of- (a) $\left(x^2 - \frac{1}{x}\right)^6$ (b) $\left(x - \frac{1}{x}\right)^{11}$	6	05	05	04
OR	iii.	By using binomial theorem, expand $(x + 2a)^5$.	6	04	05	04
Q.6	i.	Find the 21 st term of sequence 25, 30, 35, ...	4	04	02	03
	ii.	The third term of a G.P. is 24 and the sixth term is 192. Find the tenth term.	6	03	02	03
OR	iii.	Find the sum of the following Geometric Series to infinity: $1 - \frac{1}{2} + \frac{1}{4} - \dots$	6	05	03	03

Solution

Page No

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Date

YCUVA

Faculty of Management Studies

Marks

End Sem Examination Dec-2024

"MS3C032"

Elementary Mathematics & Statistics

programme: BBA (BA)

Q:1 MCQs

i) (a) 30

ii) (c) PRT/100

iii) (c) {9}

iv) (a) singleton

v) (d) : $\{(1,1) (2,1) (1,2)\}$ None of these

vi) (a) 1

vii) (b) 24

viii) (b) 7

ix) (a) $9H/2$ x) (b) ± 1

Q: 2 (i)

$$15 \times 32 \div 2 \times 5$$

By "Boomer's" Rule

$$15 \times \frac{32}{2} \times 5$$

$$\Rightarrow 15 \times 16 \times 5$$

$$= 15 \times 80$$

$$= \boxed{1200}$$

Marks

1

1

ii) Three students contested an election and received 1000, 5000 and 10000 votes

The total vote is 16000.

The percentage of student 1

$$\left(\frac{1000}{16000} \times 100 \right) \% = \frac{100}{16} \%$$

The student 2 percentage

$$\left(\frac{5000}{16000} \times 100 \right) \% = \frac{500}{16} \%$$

The student 3 percentage

$$\frac{10000}{16000} \times 100 = \frac{100}{16} \%$$

The student - 2 will be winner.

Marks

Q: 2 (ii) Given The Ratio of ages of Abha and her mother is

2:5 (Assuming)

According to the problem at the time of Abha's birth her mother age was 27

$$5x = 2x + 27$$

$$3x = 27 \rightarrow \boxed{x = 9}$$

The present ages of Abha and her mother is

$$\text{Abha} \rightarrow 2x = 2 \times 9 = 18 \text{ year}$$

$$\text{Mother} \rightarrow 5x = 5 \times 9 = 45 \text{ year}$$

Q: 2 (iv)

$$\text{Given } P = 28600/-$$

$$R = 2.5\% \text{ per annum}$$

$$T = 3 \text{ year, 3 months}$$

$$= 3 \frac{1}{4} = 3 \frac{1}{4} \text{ year}$$

$$\text{Simple interest} = \frac{P \times R \times T}{100}$$

Marks

3

$$= \frac{28600 \times \frac{13}{4} \times 2.5}{100}$$

$$= 2323.75$$

—————x—————

Q:3(i) Define

Set:- A set is an collection of Unordered well defined collection of finite number of objects is called set. it is denoted by The symbol of Capital letter A to Z and all the elements of the finite sets inside in the { } curly bracket.

2

Types :

(1) Finite set: A set in which finite number of elements is called finite set

ex $A = \{2, 4, 6, 8, 10\}$

1

② Null set: A set in which no any element are present (empty) is called Null set. It is denoted by ϕ

$$\phi = \{ \}$$

③ disjoint set: If A and B are two finite sets then $A \cap B = \phi$ is called disjoint-

Ex $A = \{2, 5, 7\}$

$$B = \{8, 9\}$$

$$A \cap B = \phi$$

4) Difference of two sets: The Difference of two sets $A - B$ in which taking after subtraction only set A not B.

$$\forall x \in (A - B) \Rightarrow x \in A \text{ and } x \notin B$$

Ex $A = \{1, 2, 3, 4, 5\}$

$$B = \{5, 6\}$$

$$A - B = \{1, 2, 3, 4\}$$

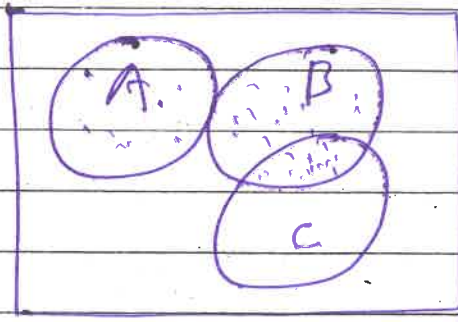
Q.3 (ii)

Venn diagram :- The pictorial representation of finite no. of sets.

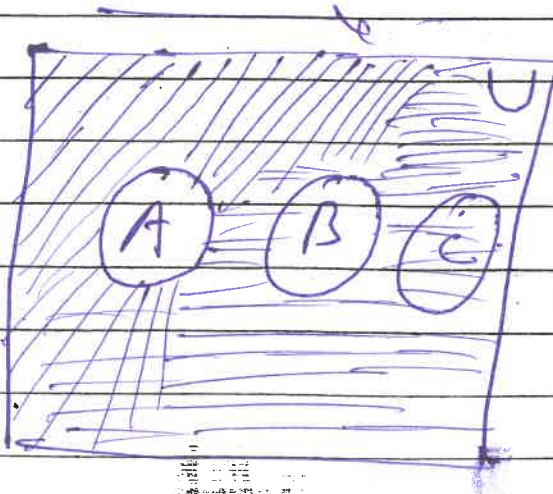
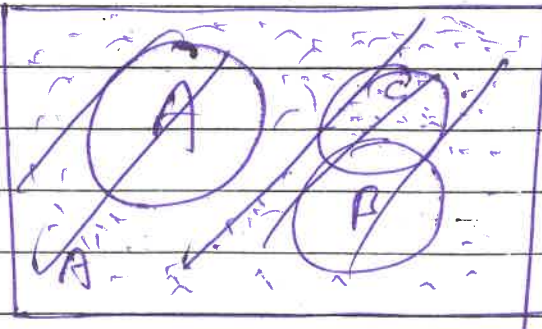
Marks

(a) $(A \cup B) \cap (A \cup C) = A \cup (B \cap C)$

Identical sets A, B and C are taken for drawing Venn-diagrams



(b) $A' \cap (C - B)$



Q: 3 (ii)

$$\text{if } A = \{a, b, c, d, e\}$$

$$B = \{a, c, e, g\}, C = \{b, e, d, g\}$$

(i) to show that -

$$A \cap (B - C) = (A \cap B) - (A \cap C)$$

L.H.S $B - C = \{a, c\}$

$$A \cap (B - C) = \{a, c\}$$

R.H.S $A \cap B = \{a, c, e\}$

$$A \cap C = \{e\}$$

$$(A \cap B) - (A \cap C) = \{a, c\}$$

proven

$$b) A - (B \cap C) = (A - B) \cup (A - C)$$

$$B \cap C = \{e, g\} \quad A - B = \{b, d, f\}$$

$$A - C = \{a, c, d\}$$

L.H.S $A - \{B \cap C\} = \{a, b, c, d\}$

R.H.S

$$(A - B) \cup (A - C) = \{a, b, c, d\} \text{ proven}$$

Q: 4(i) The following Relation R are Reflexive, symmetric and transitive on the set $A = \{1, 2, 3, 4\}$

$$R = \{(2, 2), (3, 3), (4, 4), (2, 3), (3, 4)\}$$

Marks

① Reflexive: $\forall x \in A$ Then

$$(x, x) \in R \Rightarrow (2, 2) \in R$$

$$(2, 2) \in R \Rightarrow (2, 2) \in R$$

$$(3, 3) \in R \Rightarrow (3, 3) \in R$$

$$(4, 4) \in R \Rightarrow (4, 4) \in R$$

Hence R is reflexive on A .

② Symmetric: $\forall x, y \in A$

$$xRy \Rightarrow yRx$$

$$(2, 3) \in R \Rightarrow (3, 2) \notin R$$

$$(3, 4) \in R \Rightarrow (4, 3) \notin R$$

$$(2, 3) \in R \Rightarrow (3, 2) \notin R$$

Clearly, R is not symmetric on A .

③ Transitive: $\forall x, y, z \in A$

Marks

$$2R4 \text{ \& } 4R2 \Rightarrow 2R2$$

$$(2,4) \in R \text{ \& } (4,2) \in R \Rightarrow (2,2) \in R \quad 1$$

$$(2,3) \in R \text{ \& } (3,4) \in R \Rightarrow (2,4) \notin R$$

R is not Transitive on A.

→ *

Q:4 (ii) In The given problem, production cost of a book is Rs 30 if there are x books, Therefore,

$$\text{Variable cost} = \text{price} \cdot \text{quantity}$$

$$V(x) = 30x \quad \text{--- (1)}$$

Fixed cost function

$$C(x) = F(x) + V(x)$$

$$= 15,000 + 30x$$

--- (2)

Revenue function. Let x be Mo. of units of books sold if each book is sold at a rate of Rs 45-

$$R(x) = 45x$$

Profit Function -

Marks

$$P(x) = R(x) - C(x)$$

$$P(x) = 50x - (25000 + 30x)$$

$$P(x) = 20x - 15000$$

Break - Even point.

$$P(x) = 0$$

$$20x - 15000 = 0$$

$$x = 15000/20$$

$$x = 750 \text{ Rs}$$

Cost Function

$$C(x) = 15000 + 30 \times 750$$

$$C(x) = 15000 + 22,500$$

$$C(x) = \text{Rs } 37,500$$

Q:4 (iii) Define function:-

Marks

Function is the relationship between two variables, for example $y = f(x)$ where y is the dependent variable and x is independent variable. In mapping form, we can define function as:-

2

Let A and B be two non empty sets

Then

$$f: A \xrightarrow{\text{into}} B$$

Where A is domain and B is Codomain of f .

Types -

i) Algebraic function :- An algebraic function which consists of a finite number of terms involving powers and roots of the variable x and the mathematical operations like that addition, subtraction, multiplication and division.

Ex: $f(x) = x^3 + 6x^2 - 5x + 4$

ii) Transcendental function: - The functions which are not algebraic are called transcendental function in other words the functions which involved trigonometric, exponential, logarithm etc.

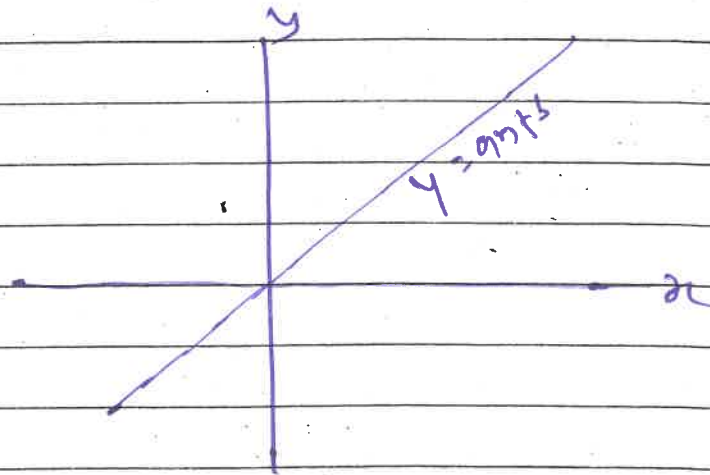
Ex: $f(x) = x \sin x + x^2 \log x$

Marks

iii) Linear function:- A function $f(x)$ defined by

$$f(x) = ax + b$$

Where a and b are constants and x, y are variables is called linear function. Its graph is always a straight line.

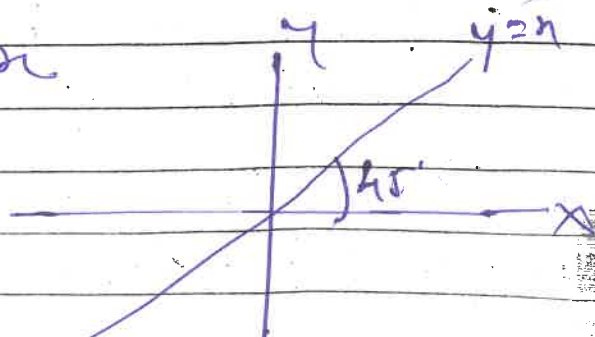


iv) Identity function:- It's special case of linear function with $a=1$ and $b=0$

$$y = ax + b \quad (a=1, b=0)$$

$$y = x \quad (y = f(x))$$

$$f(x) = x$$



Q:5(i) Apply formula of combinations

Marks

$$nCr = \frac{n!}{(n-r)! \cdot r!}$$

given that,

10 test books and 8 other books.

In how many ways can be selected 4 test books and 3 other books are -

$${}^{10}C_4 \times {}^8C_3$$

$$= \frac{10!}{6! \cdot 4!} \times \frac{8!}{5! \cdot 3!}$$

$$= 210 \times 56$$

$$= 11760 \text{ ways}$$

ii) Q:5(ii) Find the middle term in the expansion -

Q) $\left(x^2 - \frac{1}{x}\right)^6$ to compare

Marks

$(a+b)^n$ where $a = x^2$ $b = -\frac{1}{x}$
 $n = 6$ (even)

The only one middle term.

$$\frac{n}{2} + 1 = \frac{6}{2} + 1 = 4$$

$\therefore T_{r+1} = {}^nC_r a^{n-r} b^r$

$$T_{3+1} = {}^6C_3 (x^2)^{6-3} \left(-\frac{1}{x}\right)^3$$

$$= -20 x^6 \cdot \frac{1}{x^3}$$

$$\boxed{T_4 = -20x^3}$$

Q) $\left(x - \frac{1}{x}\right)^{11}$ where $a = x$

$b = -\frac{1}{x}$ $n = 11$ (odd)

Two middle terms

$n+1/2$ & $n+3/2$ $n=11$

6 & 7

$$\therefore T_{r+1} = n C_r a^{n-r} b^r$$

$$n = 6$$

$$T_{5+1} = {}^{11}C_5 x^{11-5} \left(-\frac{1}{x}\right)^5$$

2

$$T_6 = -462x$$

$$n = 7$$

$$T_{6+1} = {}^{11}C_6 (x)^{11-6} \left(-\frac{1}{x}\right)^6$$

$$T_7 = \frac{462}{x}$$

Q: 5 (iii) Binomial expansion.

$$(x+29)^5$$

$$\therefore (a+b)^n = a^n + n C_1 a^{n-1} b + n C_2 a^{n-2} b^2 + \dots + b^n$$

Where $a = x$ $b = 29$ $n = 5$

$$(x+29)^5 = x^5 + 5 C_1 x^4 (29) + 5 C_2 x^3 (29)^2 + 5 C_3 x^2 (29)^3 + 5 C_4 x (29)^4 + 5 C_5 (29)^5$$

$$(21+29)^5 = 21^5 + 10 \cdot 21^4 \cdot 29 + 40 \cdot 21^3 \cdot 29^2 + 80 \cdot 21^2 \cdot 29^3 + 80 \cdot 21 \cdot 29^4 + 32 \cdot 29^5$$

Marks

2

Q: 6 (i)

The Sequence

25, 30, 35 ----- AP

$$a = 25 \quad d = 5$$

General term of AP.

$$T_n = a + (n-1)d$$

$$n = 21$$

$$T_{21} = a + (21-1)d$$

$$T_{21} = a + 20d$$

$$\text{put } a = 25 \quad d = 5$$

$$T_{21} = 25 + 20 \times 5$$

$$T_{21} = 125$$

Q: 6 (ii)

given 3rd and 6th term
of h.p are

Marks

General term: $[T_n = ar^{n-1}]$ 1.

$$T_3 = ar^2 = 24 \quad \text{--- (1)}$$

$$T_6 = ar^5 = 192 \quad \text{--- (2)}$$

3

Dividing (2)/(1)

$$\frac{ar^5}{ar^2} = \frac{192}{24}$$

$$r^3 = 8$$

$$r^3 = 2^3$$

$$\boxed{r = 2}$$

$$a \cdot 4 = 24$$

$$\boxed{a = 6}$$

10th term

$$T_{10} = ar^9$$

$$a = 6 \cdot 2^9$$

$$\boxed{T_{10} = 3072}$$

3

Q. 8 (iii)

The sum of $1 + \frac{1}{2} + \frac{1}{4} + \dots$

$$1 - \frac{1}{2} + \frac{1}{4} - \dots$$

$$a = 1, \quad r = -\frac{1}{2} < 1$$

$$r < 1$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_n = \frac{1(1-(-1/2)^n)}{1+1/2}$$

$$S_n = \frac{2}{3} \left[1 - \frac{(-1)^n}{2^n} \right]$$

$$S_n = \frac{2^{1-n}}{3} \left[2^n - (-1)^n \right]$$