

[4]

OR iii What is a lag compensator? Describe its characteristics and applications in control systems. **6** 03 01, 02 01, 04 01, 02

Q.6 Attempt any two:
i Discuss the concepts of controllability and observability in state-space systems. **5** 02 01, 02 01, 02 01, 02
ii Given the state-space representation of a system: **5** 03 01, 02 01, 03 01, 02

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -5 & -4 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)$$

Determine the State Transition Matrix $\Phi(t)$ for this system.

iii Given the state-space representation: **5** 03 01, 02 01, 03 01, 02

$$A = \begin{bmatrix} 0 & 1 \\ -4 & -5 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

a) Compute the controllability matrix $C = [B, AB]$.

Determine whether the system is controllable based on the rank of the controllability matrix.

Total No. of Questions: 6

Total No. of Printed Pages: 4

Enrollment No.....



Faculty of Engineering
End Sem Examination Dec 2024
EE3CO34 Control Systems

Programme: B.Tech.

Branch/Specialisation: EE

Duration: 3 Hrs.

Maximum Marks: 60

Note: All questions are compulsory. Internal choices, if any, are indicated. Answers of Q.1 (MCQs) should be written in full instead of only a, b, c or d. Assume suitable data if necessary. Notations and symbols have their usual meaning.

Q.1 i. The transfer function has how many poles-

$$G(s)H(s) = \frac{2}{s^2 + 2s + 5}$$

- (a) 1 (b) 2
(c) 3 (d) 0

ii. What is the main characteristic that differentiates open-loop systems from closed-loop systems?

- (a) Feedback (b) Input signal
(c) Transfer function (d) Output signal

iii. For a second-order system with a damping ratio of 0.5, what is the overshoot percentage?

- (a) 10% (b) 20%
(c) 25% (d) 35%

iv. The root locus of a system shows that the poles move from the open-loop poles to which point-

- (a) Zero (b) Infinity
(c) The real axis (d) The imaginary axis

v. For a transfer function given below, what will be the phase-

$$G(s)H(s) = \frac{2}{s^3}$$

- (a) 0° (b) -90° (c) -180° (d) -270°

Marks	PO	CO	PSO
1	01	01	01

1	01	01	01	01
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1	02	01, 02	01, 02	01
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1	01	01	01	01
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1	02	01, 02	01, 02	01
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[2]

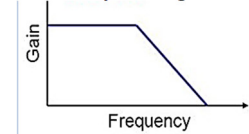
- vi. For a stable system -
 (a) GM & PM both are negative.
 (b) GM and PM both are positive.
 (c) GM is +Ve and PM -Ve
 (d) GM is negative and PM is Positive

vii The transfer function $G_c(s) = \frac{(1+0.5s)}{(1+s)}$

represents-

- (a) lag network
 (b) lead network
 (c) lag-lead network
 (d) Proportional controller

vii Identify the given characteristic is suitable for -



- (a) Lead compensator
 (b) Lag compensator
 (c) Lead lag compensator
 (d) RC feedback network

ix. Which property must be satisfied for a system to be controllable?

- (a) All poles on the right half of the plane
 (b) The ability to reach any desired state
 (c) Minimal phase shift
 (d) No steady-state error

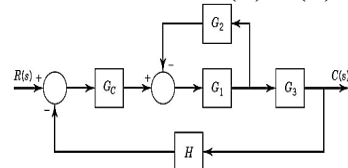
x. Which of the following properties ensures a system can be brought to any desired state using an input?

- (a) Observability (b) Stability
 (c) Controllability (d) Diagonalization

Q.2 i. Define the transfer function of a linear system.

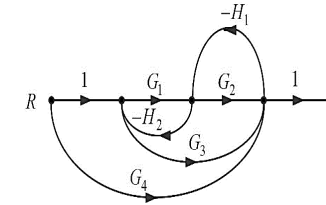
ii. Explain the differences between open-loop and closed-loop systems.

iii For the system represented in the given figure, determine transfer function $C(S)/R(S)$.



[3]

OR iv. Using Mason's gain formula calculate the transfer function of the given diagram



Q.3 i. What is stable and marginally stable system?

ii. With the help of Routh's stability criterion find the stability of the following systems represented by the characteristic equations-
 $s^5 + 2s^4 + 3s^3 + 4s^2 + 5s + 6 = 0$

iii. Given a second-order system with the transfer function:

$$H(s) = \frac{25}{s^2 + 10s + 25}$$

Find the natural frequency ω_n and damping ratio ζ

OR iv. Explain the various rules to sketch the root locus.

Q.4 i. What is the nyquist stability criterion? Explain how it is used to determine the stability of a control system.

ii. Construct the Bode plot and determine the gain margin and phase margin.

$$G(s) = \frac{10}{s^2 + 4s + 8}$$

OR iii. For a given transfer function;

$$G(s)H(s) = \frac{12}{s(s+1)(s+2)}$$

Draw the polar plot and find the system's stability.

Q.5 i. Explain the role of Bode plots in the design and analysis of compensators.

ii. Explain the physical realization of a lag-lead compensator and its effect on system performance.

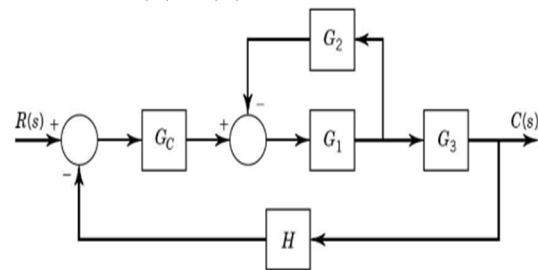
[2]

[3]

Marking Scheme
EE3CO34 (T) Control Systems (T)

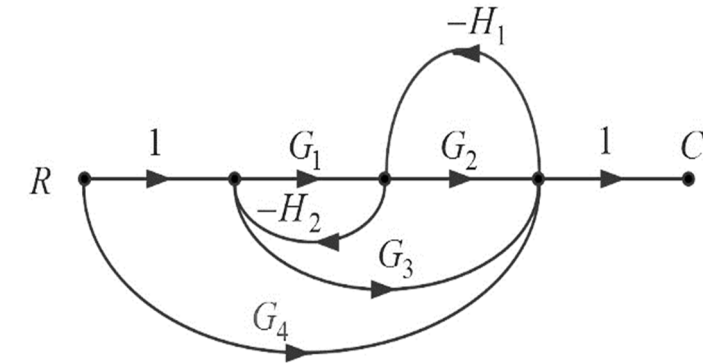
- Q.1
- | | | |
|-------|---|---|
| i) | b) 2 | 1 |
| ii) | a) Feedback | 1 |
| iii) | c) 25% | 1 |
| iv) | b) Infinity | 1 |
| v) | (d) -270° | 1 |
| vi) | (b) GM and PM both are Positive | 1 |
| vii) | (b) lead network | 1 |
| viii) | (b) Lag compensator | 1 |
| ix) | b) The ability to reach any desired state | 1 |
| x) | c) Controllability | 1 |

- Q.2
- | | | |
|------|---|---|
| i. | Define the transfer function of a linear system.
Definition- 2 Marks | 2 |
| ii. | Explain the differences between open-loop and closed-loop systems.
Differences- 1 point each | 3 |
| iii. | For the system represented in the given figure, determine transfer function $C(S)/R(S)$. | 5 |



determine transfer function $C(S)/R(S)$ - 5 marks

- OR
- | | | |
|-----|---|---|
| iv. | Using Mason's gain formula calculate the transfer function of the given diagram | 5 |
|-----|---|---|



Mason's gain formula- 1 Marks

Steps- 2 Marks

Calculation- 2 Marks

- Q.3
- | | | |
|-----|--|---|
| i. | What is stable and marginally stable system?
1 mark each | 2 |
| ii. | With the help of Routh's stability criterion find the stability of the following systems represented by the characteristic equations:
$s^5 + 2s^4 + 3s^3 + 4s^2 + 5s + 6 = 0$ | 3 |

Routh's stability criterion solution- 2 marks

Stability – 1 mark

- OR
- | | | |
|------|---|---|
| iii. | Given a second-order system with the transfer function: | 5 |
|------|---|---|

$$H(s) = \frac{25}{s^2 + 10s + 25}$$

Find the natural frequency ω_n and damping ratio ζ

the natural frequency ω_n - 3 Marks

damping ratio- 2 Marks

- | | | |
|-----|--|---|
| iv. | Explain the various rules to sketch the root locus.
Step- 1 mark each | 5 |
|-----|--|---|

- Q.4
- | | | |
|-----|--|---|
| i. | Nyquist stability criterion – 2 Marks
determine the stability – 2 Marks | 4 |
| ii. | Construct the Bode plot and determine the gain margin and phase margin. | 6 |

$$G(s) = \frac{10}{s^2 + 4s + 8}$$

[2]

Bode plot- 4 Marks

Gain Margin- 1 Mark

Phase Margin- 1 Mark

- OR iii. For a given transfer function $G(s)H(s) = \frac{12}{s(s+1)(s+2)}$, draw the polar plot and find the system's stability. **6**

polar plot- 4 Marks

system's stability -2 Marks

- Q.5 i. Explanation – 2 Marks **4**
 Analysis - 2 Marks
 ii. Explanation – 3 Marks **6**
 effect on system performance - 3 Marks
 OR iii. lag compensator - 3 Marks **6**
 characteristics -2 Marks
 Applications - 1 Mark

Q.6

- i. Discuss the concepts of controllability and observability in state-space systems. **5**
 controllability and observability- 2.5 Marks each
 ii. Given the state-space representation of a system: **5**

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -5 & -4 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)$$

Determine the State Transition Matrix $\Phi(t)$ for this system.the State Transition Matrix $\Phi(t)$ - 5 Marks

- iii. Given the state-space representation: **5**

$$A = \begin{bmatrix} 0 & 1 \\ -4 & -5 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

- a) Compute the controllability matrix $C=[B,AB]$.
 3 Marks

[3]

- b) Determine whether the system is controllable based on the rank of the controllability matrix.- 2 Marks
