

[4]

- ii. Sketch the bode plot for the transfer function 7
- $$G(s) = \frac{1000}{s(1 + 0.1s)(1 + 0.001s)}$$
- Determine:
- (a) Gain cross over frequency (b) Phase cross over frequency  
(c) G.M and P.M (d) Stability of the given system
- OR iii. Draw the root locus for a system whose open loop transfer function is 7
- given by  $G(s)H(s) = \frac{K}{s(s+4)(s^2+4s+20)}$ . Show all the salient points on the locus.
- Q.5 i. Describe different type of compensator used in control system 3
- ii. Compare the characteristics of phase lead and phase lag networks used for control system compensation 7
- OR iii. Design the lag compensator for a system whose open loop transfer function is  $G(s) = \frac{K}{s(s+1)(s+4)}$  7
- To meet the following specifications:
- (a) Damping ratio=0.5 (b) Settling time  $t_s=10$  sec  
(c) Velocity error constant  $K_v \geq 5$ .
- Q.6 i. Consider the following matrix 3
- $$\dot{x} = \begin{bmatrix} 0 & 1 \\ -6 & -5 \end{bmatrix} x(0) = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$
- Find the state transition matrix, also determine  $x(t)$ .
- ii. Write the state equations  $\frac{d^3c}{dt^3} + 6\frac{dc}{dt} + 5c(t) = r(t)$ . Also draw the state variable diagram. 7
- OR iii. A system characterized by the transfer function  $\frac{y(s)}{u(s)} = \frac{2}{(s^3+6s^2+11s+6)}$  7
- Find the state and output equation in matrix form and also test the controllability and observability of the system.

\*\*\*\*\*

Total No. of Questions: 6

Total No. of Printed Pages: 4

Enrollment No.....



Faculty of Engineering  
End Sem (Odd) Examination Dec-2019  
EE3CO15 / EX3CO15 Linear Control System  
Programme: B.Tech. Branch/Specialisation: EE/EX

Duration: 3 Hrs.

Maximum Marks: 60

Note: All questions are compulsory. Internal choices, if any, are indicated. Answers of Q.1 (MCQs) should be written in full instead of only a, b, c or d.

- Q.1 i. A system can be completely described by a transfer function if it is 1
- (a) Nonlinear and continuous  
(b) Linear and time-varying  
(c) Nonlinear and time invariant  
(d) Linear and time invariant
- ii. A.C. servomotor resembles 1
- (a) Two phase induction motor (b) Three phase induction motor  
(c) Direct current series motor (d) Universal motor
- iii. The velocity error constant of a stable canonical feedback system is 1
- given by  
(a)  $\lim_{s \rightarrow 0} G(s)$  (b)  $\lim_{s \rightarrow 0} sG(s)$  (c)  $\lim_{s \rightarrow 0} s^2G(s)$  (d) None of these
- iv. The solution of differential equation  $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + 2y = 3$  1
- (a) Oscillatory (b) Overdamped  
(c) Underdamped (d) Critically damped
- v. Using Routh's criterion, the number of roots in the right half s-plane 1
- for the characteristic equation:  $s^4 + 2s^3 + 2s^2 + 3s + 6 = 0$  is  
(a) One (b) Two (c) Three (d) Four
- vi. Which of the following describes correctly the effect of adding a zero 1
- to the system?  
(a) System becomes oscillatory.  
(b) Root locus shifts toward imaginary axis.  
(c) Relative stability of the system increases  
(d) Operating range of K for stable operation decreases

P.T.O.

[2]

- vii. The transfer function of a phase-lead compensator is given by:  $G(s) = \frac{1+3Ts}{1+Ts}$  Where  $T > 0$  What is the maximum shift provided by such a compensator? (a)  $90^\circ$  (b)  $60^\circ$  (c)  $45^\circ$  (d)  $30^\circ$  **1**
- viii. Consider the following statements: I. Bandwidth is increased II. Peak overshoot in the step response is increased Which of these are the effects of using lead compensation in a feedback system? (a) I only (b) II only (c) Both I and II (d) Neither I nor II **1**
- ix. The system  $\dot{x} = Ax + Bu$  with  $A = \begin{bmatrix} -1 & 2 \\ 0 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$  is (a) Stable and controllable. (b) Stable but Uncontrollable. (c) Unstable but controllable. (d) Unstable and uncontrollable. **1**
- x. The system matrix of a linear time invariant continuous time system is given by  $A = \begin{bmatrix} 0 & 1 \\ -3 & -5 \end{bmatrix}$  (a)  $s^2 + 5s + 3 = 0$  (b)  $s^2 - 3s + 5 = 0$  (c)  $s^2 + 3s + 5 = 0$  (d)  $s^2 + s + 2 = 0$  **1**

- Q.2 i. Obtain the system equation and find the value of  $X_2(s)/F(s)$  for the system shown in Fig.1 **3**

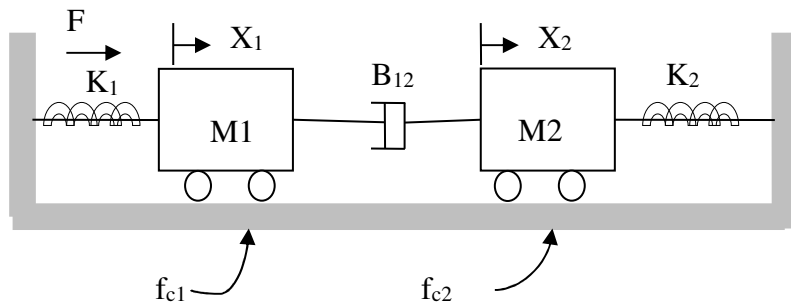


Fig .1

- ii. Determine the transfer function  $C_1/R_1$ ,  $C_2/R_2$ ,  $C_1/R_2$ ,  $C_2/R_1$  from the block diagram shown in Fig.2 **7**

[3]

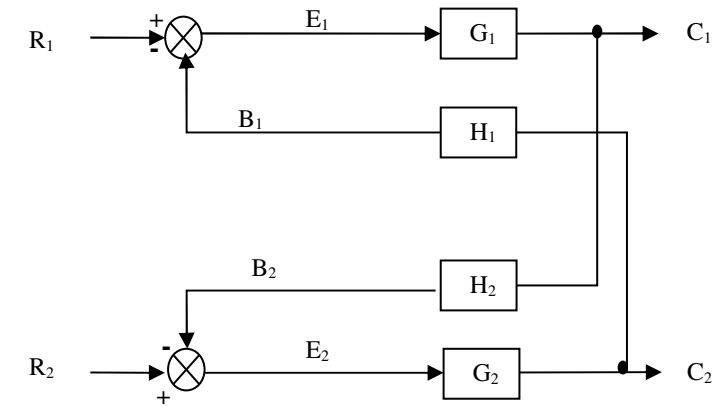


Fig.2

- OR iii. Draw the block diagram and signal flow graph and find out the transfer function of the circuit shown in Fig.3 **7**

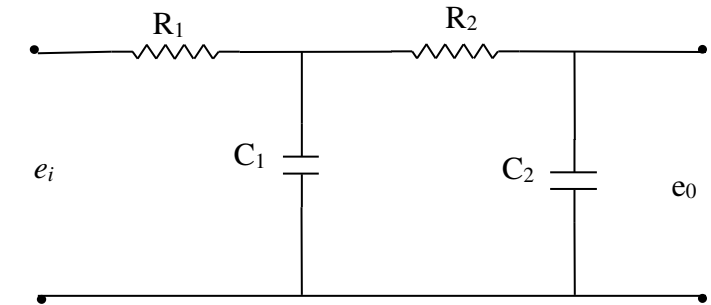


Fig.3

- Q.3 i. Define static error coefficients in control system. **3**  
 ii. A unity feedback system is characterized by an open loop transfer function  $G(s) = \frac{K}{s(s+20)}$ . Determine the gain K so that the system will have a damping ratio of 0.6. For this value of K calculate settling time, peak overshoot and time to peak overshoot for a unit step input. **7**
- OR iii. Derive the expression and response of the first order system with unit step input. **7**
- Q.4 i. Define resonant peak, resonant frequency and bandwidth. **3**

## Marking Scheme

### EE3CO15 / EX3CO15 Linear Control System

Q.1	i.	A system can be completely described by a transfer function if it is	1
		(d) Linear and time invariant	
	ii.	A.C. servomotor resembles	1
		(a) Two phase induction motor	
	iii.	The velocity error constant of a stable canonical feedback system is given by	1
		(b) $\lim_{s \rightarrow 0} sG(s)$	
	iv.	The solution of differential equation $\frac{d^2y}{dt^2} + 2\frac{dy}{dx} + 2y = 3$	1
		(c) Underdamped	
	v.	Using Routh's criterion, the number of roots in the right half s-plane for the characteristic equation: $S^4+2S^3+2S^2+3S+6=0$ is	1
		(b) Two	
	vi.	Which of the following describes correctly the effect of adding a zero to the system?	1
		(c) Relative stability of the system increases	
	vii.	The transfer function of a phase-lead compensator is given by:	1
		$G(s) = \frac{1+3Ts}{1+Ts}$ Where $T>0$	
		What is the maximum shift provided by such a compensator?	
		(d) $30^\circ$	
	viii.	Consider the following statements:	1
		I. Bandwidth is increased	
		II. Peak overshoot in the step response is increased	
		Which of these are the effects of using lead compensation in a feedback system?	
		(a) I only	
	ix.	The system $\dot{x}=Ax + Bu$ with $A=\begin{bmatrix} -1 & 2 \\ 0 & 2 \end{bmatrix}$ , $B=\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ is	1
		(c) Unstable but controllable.	
	x.	The system matrix of a linear time invariant continuous time system is given by $A=\begin{bmatrix} 0 & 1 \\ -3 & -5 \end{bmatrix}$	1
		(a) $s^2+5s+3=0$	
Q.2	i.	Derive system equation	1.5 marks
		Value of $X_2(s)/F(s)$	1.5 marks
	ii.	Determine the transfer function $C_1/R_1$ ,	1.5 marks
		$C_2/R_2$ ,	1.5 marks
		$C_1/R_2$	2 marks
		$C_2/R_1$	2 marks

OR	iii.	Draw the block diagram	2 marks	7
		Signal flow diagram	2 marks	
		Transfer function of the circuit	3 marks	
Q.3	i.	Define static error coefficients in control system.		3
		Position error coefficient	1 mark	
		Velocity error coefficient	1 mark	
		Acceleration error coefficient	1 mark	7
	ii.	Value of K	2 marks	
		Settling time	2 marks	
		Peak overshoot	2 marks	
		Time to peak overshoot	1 mark	
	OR	iii.	Derive the expression	7
			Response of the first order system	
Q.4	i.	Definition of		3
		Resonant peak	1 mark	
		Resonant frequency	1 mark	
		Bandwidth	1 mark	7
	ii.	Determine:		
		Sketch of bode plot	4 marks	
		Gain cross over frequency	0.5 mark	
		Phase cross over frequency	0.5 mark	
		G.M and P.M	1 mark	
		Stability of the given system	1 marks	
OR	iii.	Show all the salient points on the locus.		7
		Stepwise marking		
Q.5	i.	Type of compensator used in control system		3
		Series compensation	1 mark	
		Feedback compensation	1 mark	
		Load compensation	1 mark	7
	ii.	Compare the characteristics of phase lead and phase lag networks used for control system compensation		
	OR	iii.	Root locus plot	7
			Design	
Q.6	i.	State transition matrix	2 marks	3
		Determine $x(t)$	1 mark	

OR	ii.	State equations	4 marks	<b>7</b>
		State variable diagram	3 marks	
	iii.	Find the state and output equation	3 marks	<b>7</b>
		Test controllability	2 marks	
		Test observability of the system	2 marks	

\*\*\*\*\*