

Enrollment No.....



Knowledge is Power

Faculty of Engineering

End Sem (Odd) Examination Dec-2017

CA5CO13 Theory of Computation

Programme: MCA Branch/Specialisation: Computer Application

**Duration: 3 Hrs.**

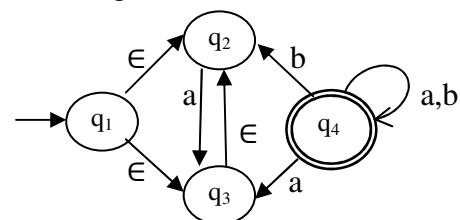
**Maximum Marks: 60**

Note: All questions are compulsory. Internal choices, if any, are indicated. Answers of Q.1 (MCQs) should be written in full instead of only a, b, c or d.

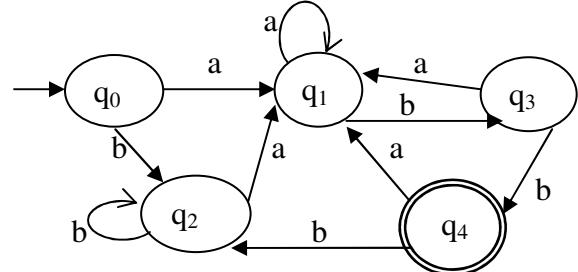
- Q.1 i. Which of the following is true? 1  
(a)  $(01)^*0 = 0(10)^*$   
(b)  $(0+1)^*0(0+1)^*1(0+1) = (0+1)^*01(0+1)^*$   
(c)  $(0+1)^*01(0+1)^*+1^*0^* = (0+1)^*$   
(d) All of these
- ii. A language is regular if and only if 1  
(a) Accepted by DFA (b) Accepted by PDA  
(c) Accepted by LBA (d) Accepted by Turing machine
- iii. Which of the following does not obey pumping lemma for context free languages? 1  
(a) Finite languages (b) Context free languages  
(c) Unrestricted languages (d) None of these
- iv. Every grammar in Chomsky Normal Form is: 1  
(a) Regular (b) Context sensitive  
(c) Context free (d) All of these
- v. The transition in Push down automaton makes is additionally dependent upon the: 1  
(a) Stack (b) Input tape (c) Terminals (d) None of these
- vi. PDA is more powerful than 1  
(a) Turing machine (b) Finite automata  
(c) Both (a) and (b) (d) None of these
- vii. A turing machine that is able to simulate other turing machines: 1  
(a) Nested Turing machines  
(b) Universal Turing machine  
(c) Counter machine  
(d) None of these

[2]

- viii. The value of n if turing machine is defined using n-tuples: 1
    - (a) 6      (b) 7      (c) 8      (d) 5
  - ix. A language L is said to be \_\_\_\_\_ if there is a turing machine M such that  $L(M)=L$  and M halts at every point. 1
    - (a) Turing acceptable      (b) Decidable
    - (c) Undecidable      (d) None of these
  - x. Decidable can be taken as a synonym to: 1
    - (a) Recursive      (b) Non recursive
    - (c) Recognizable      (d) None of these
- Q.2**
- i. What do you mean by principle of induction? 2
  - ii. Briefly explain the difference between DFA and NDFA. 3
  - iii. Convert the following NFA with  $\epsilon$  moves into DFA. 5



- OR** iv. Construct a minimum state automaton for the following DFA. 5



- Q.3**
- i. Define the following 3
    - (a) Chomsky Normal form      (b) Greibach Normal form
  - ii. Convert the given CFG to CNF 7

$$S \rightarrow aSa \mid bSb \mid a \mid b$$
- OR**
- iii. Remove all unit production, all useless productions and all  $\epsilon$  productions from the grammar. 7
- $S \rightarrow aA \mid aBB$   
 $A \rightarrow aaA \mid \epsilon$   
 $B \rightarrow bB \mid bbC$  And  $C \rightarrow B$

[3]

- Q.4
- i. What are the different types of languages accepted by a pushdown Automata and define them? 3
  - ii. Construct a PDA for the following set: 7

$$L = \{ a^{2n} b^n \mid n \geq 1 \}$$
- OR
- iii. Convert the following context free grammar into PDA : 7

$$S \rightarrow aS \mid aA$$
  

$$A \rightarrow bA \mid b$$

Take the input as aab:
- Q.5
- i. What is Turing Machine? Explain the configuration of Turing machine. 4
  - ii. Construct a Turing machine for  $L = \{ a^n b^n c^n \mid n \geq 1 \}$ . 6
- OR
- iii. Construct a Turing machine for the language of even number of 1's and even number of 0's over  $\Sigma = \{0,1\}$ . 6
- Q.6
- Attempt any two: 5
  - i. What do you mean by 'Decidable' and 'Undecidable' problems? Give example. 5
  - ii. Explain P And NP Class problem in detail with example. 5
  - iii. Write short note on the following:  
    - (a) Recursive enumerable set (b) Travelling Salesmen problem5

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NAME \_\_\_\_\_  
ENROLMENT NO. \_\_\_\_\_  
SUBJECT \_\_\_\_\_

(1)

## A-Endum (odd) Examinations

our Far do NC5CO13 - TOC will not (i).

any questions. I did it for

you A70 it was no problem with

Qn-1 i) All the mentioned different form

ii) Accepted by DFA. A70 in.

iii) Unrestricted language. A70 (ii)

iv) context Free. A70

v) stack. A70

(vi) Turing M/C. Finite automata A70 (iii)

(vii) Universal turing m/c. A70

(viii) 7. A70

(ix) Decidability. A70 (iv)

(X) Learning Far A70 in binary

in A70 in A70 (v)

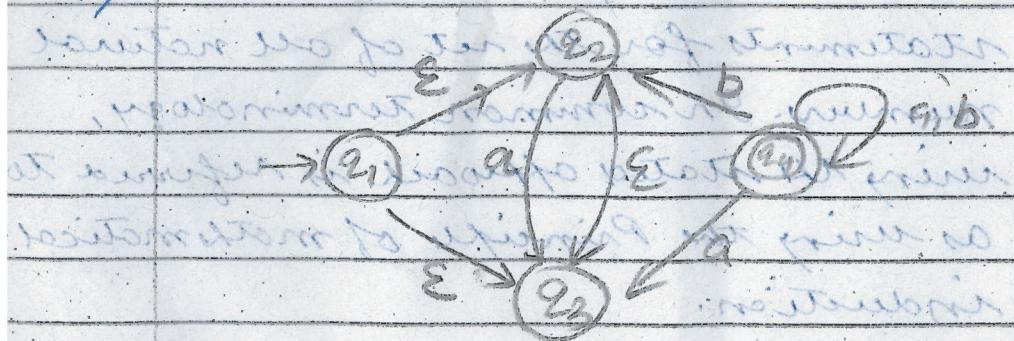
Qn-2 i) Mathematical Induction is a mathematical proof technique used to prove a given statement about all-well ordered set. Most commonly it is used to establish statements for the set of all natural numbers. In common terminology, every so stated approach is referred to as using the Principle of mathematical induction.

ii) The difference between DFA & NDFA are

(1) (2)

## DFA vs NFA

- (i) For every symbol of the alphabet, we do not need to specify how there is only one state the NFA next state transition according to the symbol in DFA.
- ii) DFA cannot have empty string transition. NFA can have empty string transition.
- iii) DFA can be understood as equivalent to multiple machines. NFA is equivalent to one machine.
- iv) Backtracking is allowed in DFA. not allowed in NFA
- v) DFA is more difficult to construct. NFA is easier to construct.
- vi) DFA is more powerful than NFA.



so a DFA & NFA are equivalent except if i)

(3)

$$\text{E-clique } (q_1) = \{q_1, q_2, q_3\} \text{ as } A.$$

$$\text{E-clique } (q_2) = \{q_2\}$$

$$\text{E-clique } (q_3) = \{q_2, q_3\}$$

$$\text{E-clique } (q_4) = \{q_4\}$$

Now it forms a small

$$S'(A, q) = \text{E-C}(S(A, q)).$$

$$= \text{E-C}(S(q, q_2 q_3), q).$$

$$= \text{E-C}(S(q, q) \cup S(q_2, q) \cup S(q_3, q))$$

$$= \text{E-C}(\emptyset \cup q_3 \cup \emptyset).$$

$$= \text{E-C}(q_3).$$

$$= \{q_2, q_3\}. \text{ call it as } B.$$

$$S'(A, b) = \text{E-C}(S(A, b)).$$

$$= \text{E-C}(S(q, q_2 q_3), b).$$

$$= \text{E-C}(S(q, b) \cup S(q_2, b) \cup S(q_3, b))$$

$$= \text{E-C}(\emptyset \cup \emptyset \cup \emptyset).$$

$$= \emptyset.$$

$$S'(B, q) = \text{E-C}(S(B, q))$$

$$= \text{E-C}(S(q_2 q_3), q))$$

$$= \text{E-C}(S(q_2, \emptyset) \cup S(q_3, q)).$$

$$= \text{E-C}(q_3 \cup \emptyset).$$

$$\text{Further we have } = \text{E-C}(q_3).$$

$$= \{q_2, q_3\}$$

$$S'(B, b) = \text{E-C}(S(B, b)).$$

$$= \text{E-C}(S(q_2 q_3), b).$$

$$= \text{E-C}(S(q_2, b) \cup S(q_3, b))$$

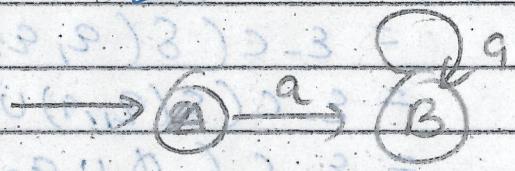
$$= \text{E-C}(\emptyset \cup \emptyset)$$

$$= \emptyset.$$

(3)

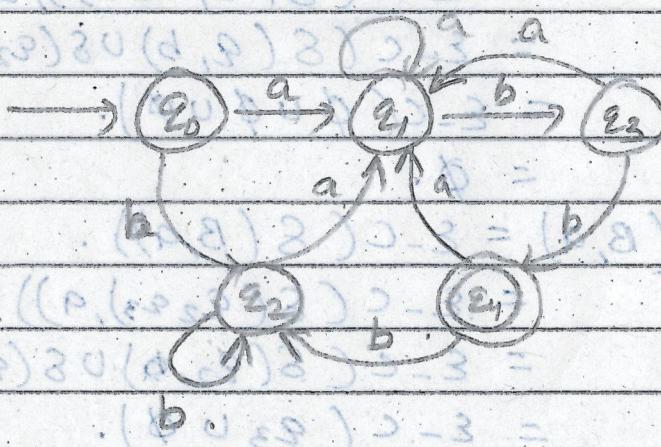
There is no final state because  
 $A = \{q_1, q_2, q_3\}$  and  $B = \{q_2, q_3\}$   
and actual final state is  $\{q_4\}$ .  
Neither A or B contains  $q_4$ .

Hence A and B cannot be final  
states required DFA will be



Thus this language accepts  $\emptyset$ .

#### (iv) Minimum state automata.



It will be easier if we construct  
a transition table for the  
finite automata.

(3)

(5)

STATE	I/O	a	b
$q_0$	$q_1$	$q_2$	
$q_1$	$q_1$	$q_3$	
$q_2$	$q_4$	$q_2$	
$q_3$	$q_4$	$q_4$	
( $q_4$ )	$q_4$	$q_2$	

Now we will first obtain  $Q_1^0$

$\therefore Q_1^0 = F = \{q_4\} \rightarrow$  Final state

$$Q_2^0 = Q - Q_1^0, \text{ i.e., } Q_2^0 = \{q_0, q_1, q_2, q_3\}$$

Hence  $\pi_0 = \{\{q_4\}, \{q_0, q_1, q_2, q_3\}\}$ .

As we can not partitioned  $Q_1^0 = \{q_4\}$  further  $Q_1^1 = \{q_4\}$ .

Now considered next  $\{q_0, q_1, q_2, q_3\}$  we will compare  $q_0$  with  $q_1, q_2, q_3$ .

S/I/O	a	b	S/I/O	a	b
$q_0$	$q_1$	$q_2$	$q_0$	$q_1$	$q_2$
$q_1$	$q_1$	$q_3$	$q_1$	$q_1$	$q_2$
$q_2$	$q_4$	$q_2$	$q_2$	$q_1$	$q_2$

1-equ.

equivalent

(2)

(6)

<del>10</del>	a	b.
20	21	(22)
23	21	(24)

$$22 \in Q_2^0 \notin Q_4^0.$$

Hence both are not 1-equiv.

$$\therefore Q'_2 = \{20, 21, 22\}$$

$$Q'_3 = \{23\}.$$

$$\text{Hence } \pi_1 = \{\{24\}, \{20, 21, 22\}, \{23\}\}.$$

Now we will compare 20 with 21, 22

<del>10</del>	a	b	<del>1</del>	a	b
20	21	(22)	20	21	22
21	20	(22)	22	21	22

As  $22 \in Q'_2 \& 22 \in Q'_3$  it is clearly not

both are not 2-equiv.  $\therefore$  are equivalent.

Hence we get two lines

$$\pi_2 = \{\{24\}, \{20, 21, 22\}, \{21\}, \{23\}\}$$

We can now state  $\{20, 23\}$  are  
3-equivalent and we cannot  
partition  $\{2\}, \& \{23\}$  further.

Hence . . .  $\text{R2A} \leftarrow 2$

$$\pi_3 = \{\{q_4\}, \{q_0 q_2\}, \{q_1\}, \{q_3\}\}.$$

$\text{R2B} \leftarrow 2$

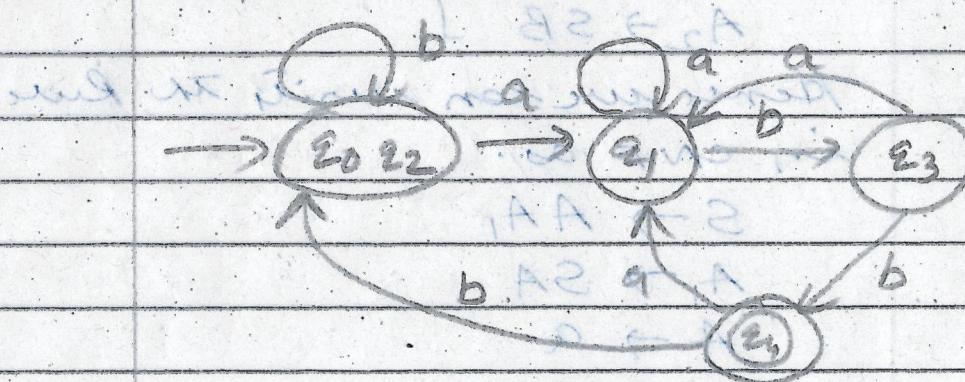
As  $\pi_3 = \pi_2$  and  $\pi_2$  gives equivalent classes we can construct MSA as

3. Construction of A2A  $\leftarrow 2$

S	a	b
$\{q_0 q_2\}$	$q_2 \leftarrow 2$	$\{q_0 q_2\}$
$q_1$	$q_1 \leftarrow 2$	$q_3$
$q_4$	$q_4 \leftarrow 2$	$q_4$
	$q_2 \leftarrow 2$	$\text{not}$

Let us draw

the state transition diagram  $\leftarrow 2$



Qn-3 i)

ii) convert the given CFG to CNF  
 $S \rightarrow aSa / bSb / a / b.$

Let us start adding new symbols for the terminals.

(5)

(8)

$$S \rightarrow ASA$$

$$A \rightarrow a$$

$$S \rightarrow BSB$$

$$B \rightarrow b$$

Let us take one more

$S \rightarrow ASA$  for converting to CNF.

$$S \rightarrow A [SA]$$

Replace it by  $A_1$

$$S \rightarrow AA_1 \quad \} \text{ Both are in CNF.}$$

$$A_1 \rightarrow SA$$

$$\text{Take } S \rightarrow B [SB]$$

Replace it by  $A_2$

$$S \rightarrow BA_2 \quad \} \text{ Both are in CNF.}$$

$$A_2 \rightarrow SB$$

Hence we can write the rule  
in CNF as.

$$S \rightarrow AA_1$$

$$A_1 \rightarrow SA$$

$$A \rightarrow a$$

$$S \rightarrow BA_2$$

$$A_2 \rightarrow SB$$

$$B \rightarrow b$$

$$S \rightarrow a^2d$$

$$S \rightarrow b$$

Normalise the set of rules

(9)

iii) Consider the grammar

$$S \rightarrow aA/aBB$$

$$A \rightarrow aaA/\epsilon$$

$$B \rightarrow bB/bbC$$

$$C \rightarrow B$$

The unit production is  $C \rightarrow B$ , to remove this production we will replace C by B and then eliminate  $C \rightarrow B$  production.

$$S \rightarrow aA/aBB$$

$$A \rightarrow aaA/\epsilon$$

$$B \rightarrow bB/bbB$$

Now consider the production rule

$$B \rightarrow bB/bbB$$

This will generate the string

$bB, bbB, bbbB, bbbbB, \dots$  This

will never terminate. Hence  $B \rightarrow bB$

$/ bbB$  is supposed to be on unless

production. Hence we will

eliminate the production containing

$B$ . Therefore the production rule

becomes

$$S \rightarrow aA$$

$$A \rightarrow aaA/\epsilon$$

Now to eliminate  $\epsilon$  production we will replace A by  $\epsilon$  and add.

(10)

those rule in existing production rules. Hence

$$S \rightarrow aA/a \quad \text{SAPP} \mid \text{APP} \leftarrow 2$$

$$A \rightarrow aaA/aa \quad \text{ADD} \leftarrow A$$

Thus we have a reduced grammar. The given grammar represents the language containing any number of a's. There must be at least single 'a' present in the language.

$$S \rightarrow aA/a$$

Qn-4(i)

$$A \rightarrow aA/a \quad \text{ADD} \mid \text{APP} \leftarrow 2$$

Qn(ii) construct a PDA for with

$$L = \{ a^{2n}b^n / n \geq 1 \}$$

For constructing model of PDA we will apply a simple logic.

That is, when we read a

initially, push all the a's

on to a stack. When we read

a single b, pop two a's from

the stack. This process will be

repeated. Finally we read a

the stack should be empty

The ID seen in given below.

The ID seen in given below

(5)

(11)

$$\{(q_0, a, q_0), (q_0, \epsilon, q_0)\} = \{q_0\}$$

$$\{(q_0, a, q_1), (q_0, \epsilon, q_1)\} = \{q_1\}$$

$$\{q_1\} = \{q_0\}$$

$$\{q_1\} = \{q_0\}$$

$$\{q_1\} = \{q_0\}$$

consider the string  $aab$

$$(q_0, d_1, q_0) + (q_0, d_2, q_0) + \dots$$

$$S(q_0, aab, q_0) \vdash (q_0, ab, q_0)$$

$$(q_0, ab, q_0) \vdash (q_0, b, q_0)$$

$$\vdash (q_0, \epsilon, q_0).$$

$$(q_0, \epsilon, q_0) \vdash (q_0, \epsilon).$$

$\vdash$  accept.

iii) convert the following CFG to PDA

$$S \rightarrow qS / aA$$

$$A \rightarrow bA / b.$$

The PDA

$$M = \{q_0\}, (q_0, a, q_0), (q_0, \epsilon, q_0), S, M = \{q_0\}, (q_0, a, q_0), (q_0, \epsilon, q_0), S, (q_0, S, \emptyset).$$

The mapping function  $S$  can be

(11)

$$\delta(q_0, \varepsilon, S) = \{(q_0, qS), (q_0, qA)\}$$

(12)

$$\delta(q_0, \varepsilon, A) = \{(q_0, bA), (q_0, b)\}$$

$$\delta(q_0, q, q) = \{(q_0, \varepsilon)\}$$

$$\delta(q_0, b, b) = \{(q_0, \varepsilon)\}$$

To illustrate the above DDA consider a string aab.

Step 1: Initial state

$$\delta(q_0, aab, S) \vdash (q_0, aab, qS)$$

$$\delta(q_0, aab, qS) \vdash (q_0, ab, qS) + (q_0, ab, S)$$

$$\delta(q_0, ab, qS) \vdash (q_0, ab, qA) + (q_0, qB, qA)$$

Step 2:

$$\vdash (q_0, b, A).$$

$$A \vdash (q_0, b, b).$$

$$\vdash (q_0, \varepsilon).$$

Step 3: Final state

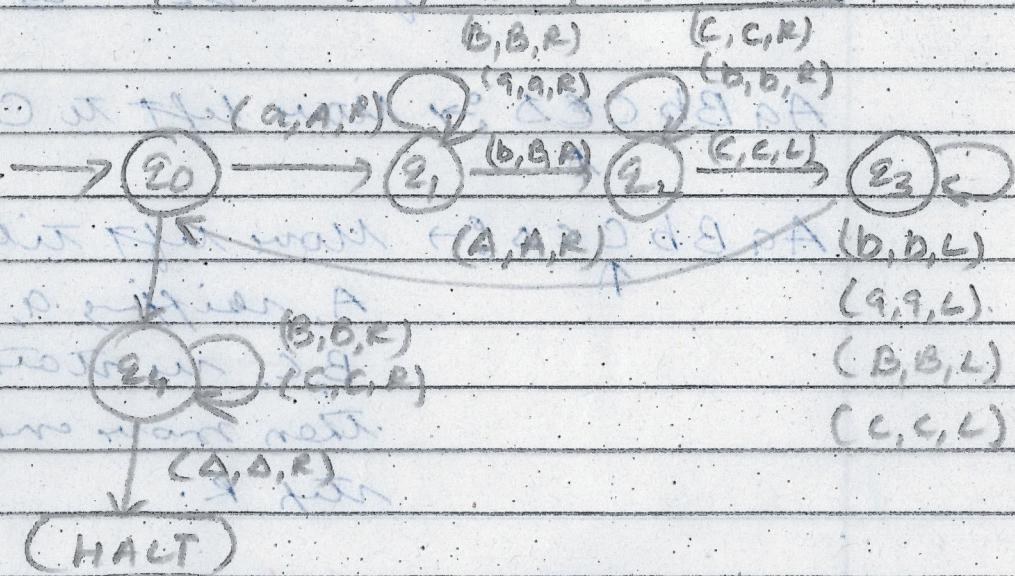
(\*) Accept.

Q4-5 is

ii) construct a TM for  $L = \{a^n b^n c^n | n \geq 1\}$ 

This problem cannot be solved even by PDA. we have solved this type of problem with turing machines.

so at aatb/b/c/c/0/0.....



The simulation for  $aabbcc$  can be shown as below.

$aabbcc \Rightarrow$  convert a to A,

$\uparrow$   $\Rightarrow$  move R transition from

$a$  move  $b$  to  $Q_0$  to  $Q_1$

$Aabbcc \Rightarrow$  Move R upto C.

$\uparrow$   $\Rightarrow$  move R

(14)

$Aabbcc\Delta \rightarrow$  convert b to B.

$\uparrow$  skip first move right.

Then go from  $q_1$  to  $q_2$ .

$AaBbCC\Delta \rightarrow$  Move R up to C.

$\uparrow$  move rightward to right till

$AaBbCC\Delta \rightarrow$  convert C to C,

$\uparrow$  move R transition  
from  $q_2$  to  $q_3$

$AaBbC\Delta \rightarrow$  Move left to C.

$\uparrow$

$AaBbC\Delta \rightarrow$  Move left till

$\uparrow$  A, skipping a, b,  
B, C, in state  $q_3$   
then move one  
step R.

$AaBbCc\Delta \rightarrow$  convert a to A

$\uparrow$  skip first move right.

Then go forward

$AaBbCc\Delta \rightarrow$  Move right

$\uparrow$  skip first move right

$AABbCc\Delta \rightarrow$  convert b to B

$\uparrow$  skip one move R.

Then go forward & transition from

$q_1$  to  $q_2$

(11)  $AABBC \Delta \rightarrow$  Move R.  
    ↑

$AABBCG \Delta \rightarrow$  connect e to C  
    ↑  
    move left till A,  
    refer  $q_3$  stat.

$AABBCC \Delta \rightarrow$  Move R, keep B  
    ↑  
    as it is refer  
    transition from  
    new state to old state  $q_0$  to  $q_4$ .

~~$AABBGG \Delta \rightarrow$  no on moving  
    ↑ R by ignoring  
    B, C refer  $q_4$  stat.~~

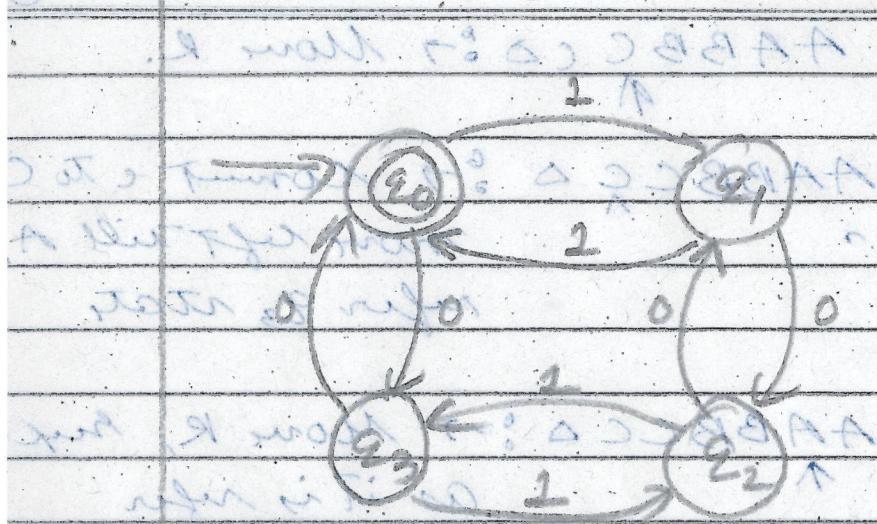
$AABBCC \Delta \rightarrow$  since  $\Delta$  is read  
    ↑ TM will move  
    to Next state.

$AABBCC \Delta \rightarrow$

Q4-5.iii) For this type of problem  
even we have drawn FSM.

1

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And now it will be very  
much easy for us to convert  
the FSM to TM.

