

Faculty of Engineering

End Semester Examination May 2025

EN3BS15 Engineering Mathematics -III

Programme	:	B.Tech.	Branch/Specialisation	:	All
Duration	:	3 hours	Maximum Marks	:	60

Note: All questions are compulsory. Internal choices, if any, are indicated. Assume suitable data if necessary.

Notations and symbols have their usual meaning.

Section 1 (Answer all question(s))				Marks CO BL
Q1. $(1+\Delta)(1-\nabla) = \underline{\hspace{2cm}}$.				1 1 2
<input type="radio"/> E ²			<input type="radio"/> $(1^2 - \Delta^2)$	
<input checked="" type="radio"/> 1			<input type="radio"/> None of these	
Q2. Let λ be the finite difference, then shifting operator is defined by-				1 1 1
<input checked="" type="radio"/> $Ef(x) = f(x + h)$			<input type="radio"/> $Ef(x) = f(x)$	
<input type="radio"/> $Ef(x) = f(x) - f(x - h)$			<input type="radio"/> None of these	
Q3. If the function $y = f(x)$ is defined in the interval [-3,3] which is divided into 7 equidistant ordinates then the value of h is-				1 1 2
<input type="radio"/> 0			<input checked="" type="radio"/> 1	
<input type="radio"/> 4/5			<input type="radio"/> None of these	
Q4. In geometrical meaning of Euler's modified method, the curve is approximated as a-				1 1 2
<input checked="" type="radio"/> Straight line			<input type="radio"/> Circle	
<input type="radio"/> Parabola			<input type="radio"/> None of these	
Q5. In the normal distribution the curve is symmetrical about the _____.				1 1 2
<input type="radio"/> Variance			<input checked="" type="radio"/> Mean	
<input type="radio"/> Standard deviation			<input type="radio"/> None of these	
Q6. In exponential distribution variance is-				1 1 3
<input type="radio"/> $\frac{2}{\lambda^2}$			<input checked="" type="radio"/> $\frac{1}{\lambda^2}$	
<input type="radio"/> $\frac{1}{\lambda}$			<input type="radio"/> None of these	
Q7. The coefficient of correlation is the _____ of the coefficient of regression.				1 1 1
<input checked="" type="radio"/> Geometric mean			<input type="radio"/> Arithmetic mean	
<input type="radio"/> Both (A) and (B)			<input type="radio"/> None of these	
Q8. The rank Correlation coefficient lies between _____.				1 1 1
<input type="radio"/> $-1/4 \leq r \leq 1/4$			<input type="radio"/> $-1/2 \leq r \leq 1/2$	
<input checked="" type="radio"/> $-1 \leq r \leq 1$			<input type="radio"/> None of these	
Q9. In chi-square test expected frequencies should not be-				1 1 1
<input checked="" type="radio"/> Less than 5			<input type="radio"/> Greater than 5	
<input type="radio"/> Equal to 5			<input type="radio"/> None of these	

Q10. In any statistic if calculated value is not less than the tabulated value then which of the following hypothesis is accepted? 1 1 1

- Null hypothesis
- Alternative hypothesis
- Both (A) and (B)
- None of these

Section 2 (Answer any 2 question(s))

Marks CO BL

Q11. Using Newton's forward interpolation formula, find the value of $f(1.6)$, if 5 2 3

x	1	1.4	1.8	2.2
y	3.49	4.82	5.96	6.5

Rubric	Marks
write the formula, calculation and final answer	5

Q12. If the values of the function $f(x)$ are $f(1) = 4, f(2) = 5, f(7) = 5, f(8) = 4$ then find the value of $f(6)$ using Newton's divided difference formula. 5 2 3

Rubric	Marks
Write the formula, calculations and final answer	5

Q13. Apply Bessel's formula to evaluate y_{25} given 5 4 4

x	20	24	28	32
$y = f(x)$	2854	3162	3544	3992

Rubric	Marks
Write the formula, Calculations, value of y_{25}	5

Section 3 (Answer any 2 question(s))

Marks CO BL

Q14. Calculate by Simpson's one third rule an approximate value of $\int_0^1 \frac{x^2}{1+x^3} dx$ by taking five equidistant ordinates. 5 2 3

Rubric	Marks
write the formula, find five equidistance ordinates, calculations	5

Q15. Use Picard's method to compute approximate the value of y when $x = 0.1$ given that $y = 1$ when $x = 0$ and $\frac{dy}{dx} = 3x + y^2$. 5 2 3

Rubric	Marks
Write the formula, find Third iteration and final answer	5

Q16. Solve the equation $\frac{dy}{dx} = x + y$, with initial condition $y(0) = 1$ by Runge-Kutta method, from $x = 0$ to $x = 0.1$ with $h = 0.1$. 5 2 3

Rubric	Marks
Write the complete formula, find the values and put the formula and final answer	5

Section 4 (Answer any 2 question(s))

Marks CO BL

Q17. Six dice are thrown 729 times. How many times do you expect at least three dice to show five or six?

5 1 1

Rubric	Marks
find probability of success and failure, at least three dice to show five or six, multiply by 729 then final answer	5

Q18. Derive mean and variance of Poisson distribution.

5 2 3

Rubric	Marks
write the formula of Poisson distribution and derive first and second moment	5

Q19. Define exponential distribution and prove that the total area of exponential distribution is unity.

5 2 3

Rubric	Marks
definition, write the formula and derive it	5

Section 5 (Answer any 2 question(s))

Marks CO BL

Q20. Fit a straight line to the following data regarding x as the independent variable:

5 4 4

x	0	1	2	3	4
y	1	1.8	3.3	4.5	6.3

Rubric	Marks
write the equation of straight line and its normal equation, find the values	5

Q21. Calculate the Karl Pearson's coefficient of correlation between X and Y series:

5 2 3

X	17	18	19	19	20	20	21	21	22	23
Y	12	16	14	11	15	19	22	16	15	20

Rubric	Marks
write the formula, put the values in formula from the table, then final answer	5

Q22. Prove that the arithmetic mean of the coefficient of regression is greater than the coefficient of correlation. Show that the product of regression coefficient is less than or equal to 1.

5 2 3

Rubric	Marks
proof of first and second part	5

Section 6 (Answer any 2 question(s))

Marks CO BL

Q23. Define type I error, type II error, level of significance, critical region, and critical value.

5 1 2

Rubric	Marks
assign 1 mark for each definition	5

Q24. A shampoo manufacturing company was distributed a particular brand of shampoo through a large number of retail shops. Before a heavy advertisement campaign, the mean sales per shampoo was 140 dozens. After the campaign a sample of 26 shampoo was taken and the mean sales figure was found to be 147 dozens with standard deviation 16. Can you consider the advertisement effective? (Given $t_{0.05,25} = 1.708$).

Rubric	Marks
consider null hypothesis, write the formula of t-test, calculate and compare with tabulated value for decision	5

Q25. In a test given two groups of students drawn from two normal populations, the marks obtained were as follows: 5 2 3

Group A	18	20	36	50	49	36	34	49	41
Group B	29	28	26	35	30	44	46		

Examine at 5% level, whether the two populations have the same variance. (Given that $F_{0.05,(8,6)} = 4.15$).

Rubric	Marks
consider null hypothesis, write formula, compare calculated and tabulated value and decision,	5

(1)

Faculty of Engineering
 End Semester Examination May 2025.
 EN3BS15, Engineering Mathematics-II
 Programme: B.Tech.

Branch/Specialisation: A

Section 1.

Q1	(c) 1	1
Q2	(a) $Ef(x) = f(x+h)$	1
Q3	(b) 1	1
Q4	(a) straight line	1
Q5	(b) Mean	1
Q6	(b) $\sqrt{d^2}$	1
Q7	(a) Geometric Mean	1
Q8	(c) $-1 \leq \gamma \leq 1$	1
Q9	(a) less than 5	1
Q10	(b) Alternative hypothesis	1

Section 2.

Q11. The table of forward differences i.e.:-

x	$y = f(x)$	$\Delta f(x)$	$\Delta^2 f(x)$	$\Delta^3 f(x)$
1	3.49	1.33		
1.4	4.82		-0.19	-0.41
1.8	5.96	1.14		+2
2.2	6.5	0.54	-0.60	

$$f(1.6) = ? \quad \text{so } x=1.6, \text{ Also } a=1, h=0.4$$

$$u = \frac{x-a}{h} = \frac{1.6-1}{0.4} = 1.5$$

formula

$$f(a+uh) = f(a) + u\Delta f(a) + \frac{u(u-1)}{2!} \Delta^2 f(a) + \dots + 1$$

Q 13. Taking the Origin at $x_0=24$, $h=4$

$$\therefore u = \frac{x-x_0}{h} = \frac{25-24}{4} = \frac{1}{4} \Rightarrow 0.25 \text{ which is lies b/w } \frac{1}{4} \text{ & } \frac{3}{4},$$

The Central difference table is:

x	$y = f(x)$	Δy	$\Delta^2 y$	$\Delta^3 y$
$x_1 = 20$	2854	308		
$x_0 = 24$	3162	382	74	-8
$x_1 = 28$	-3544	66		
$x_2 = 32$	3992	448		+2

The Bessel's formula is,

$$f(x) = y_0 + u\Delta y_0 + \frac{u(u-1)}{2!} [\frac{\Delta^2 y_{-1} + \Delta^2 y_0}{2}] + \frac{(u-\frac{1}{2})u(u-1)}{3!} \Delta^3 y_{-1} + 1$$

Putting all values from the table, we get.

$$f(25) = 3162 + (0.25) \times (382) + \frac{(0.25)(-0.75)}{2} \left[\frac{74+66}{2} \right] + \frac{(-0.25)(0.25)(-0.75)}{6} \times (-8) + 1$$

$$\text{or } y_{25} = 3162 + 95.5 - 6.5625 - 0.0625 = 3250.875. + 1$$

Section 3.

Q14. Here the range of integration $(0, 1)$ is subdivided into five equal parts. So $h = \frac{1-0}{5} = 0.2$. Now the

values of the given function $y = x^2/(1+x^3)$ computed for each point of subdivision are as follows:

$$x_k$$

$$y_k = \frac{x_k^2}{1+x_k^3}$$

Calculations for Simpson's $\frac{1}{3}$ rule.

$$x_0 = 0$$

$$y_0 = 0$$

$$y_0 = 0$$

$$x_1 = 0.2$$

$$y_1 = 0.0397$$

$$4y_1 = 0.1588$$

$$x_2 = 0.4$$

$$y_2 = 0.15037$$

$$2y_2 = 0.30074$$

$$x_3 = 0.6$$

$$y_3 = 0.2960$$

$$4y_3 = 1.184$$

$$x_4 = 0.8$$

$$y_4 = 0.4233$$

$$2y_4 = 0.8466$$

$$x_5 = 1$$

$$y_5 = 0.5$$

$$4y_5 = 0.5$$

Total

$$2.99014$$

$$\text{formula, } I = \frac{h}{3} [y_0 + y_n + 4(y_1 + y_3 + \dots) + 2(y_2 + y_4 + y_6 + \dots)]$$

+ 1

\therefore By Simpson's $\frac{1}{3}$ rule.

$$\int_0^1 \frac{x^2}{1+x^3} dx = 0.2 \left[\frac{2.99014}{3} \right] = 0.1993$$

+ 2

(3)

Q15

$$\frac{dy}{dx} = 3x + y^2 \Rightarrow f(x, y) = 3x + y^2, y_0 = 1, x_0 = 0$$

After, first

picard's formula $y^{(n)} = y_0 + \int_{x_0}^x f(x, y^{(n-1)}) dx$ +1

Now, first approximation,

$$\begin{aligned} y^{(1)} &= y_0 + \int_{x_0}^x f(x, y_0) dx = 1 + \int_0^x (3x+1) dx \\ &= 1 + x + \frac{3x^2}{2} = 1.11500 \text{ (at } x=0.1) \end{aligned}$$

Second approximation,

$$\begin{aligned} y^{(2)} &= y_0 + \int_{x_0}^x f(x, y^{(1)}) dx = 1 + \int_0^x [3x + (y^{(1)})^2] dx \\ &= 1 + \int_0^x \left[3x + \left(1 + x + \frac{3x^2}{2} \right)^2 \right] dx \\ &= 1 + \int_0^x \left(\frac{9}{4}x^4 + 3x^3 + 4x^2 + 5x + 1 \right) dx \\ &= \frac{9}{20}x^5 + \frac{3}{4}x^4 + \frac{4}{3}x^3 + \frac{5}{2}x^2 + x + 1 \\ &= 1.1264, \text{ at } x=0.1 \end{aligned}$$

+1

Third Approximation,

$$\begin{aligned} y^{(3)} &= y_0 + \int_0^2 f(x, y^{(2)}) dx = 1 + \int_0^2 [3x + (y^{(2)})^2] dx \\ &= 1 + \int_0^2 \left(\frac{81}{400}x^{10} + \frac{27}{40}x^9 + \frac{141}{80}x^8 + \frac{17}{4}x^7 + \frac{1157}{180}x^6 + \frac{136}{15}x^5 \right. \\ &\quad \left. + \frac{125}{12}x^4 + \frac{23}{3}x^3 + 6x^2 + 5x + 1 \right) dx \\ &= \frac{81}{4400}x^{11} + \frac{27}{400}x^{10} + \frac{47}{240}x^9 + \frac{17}{32}x^8 + \frac{1157}{1260}x^7 + \frac{62}{45}x^6 + \frac{26}{12}x^5 \\ &\quad + \frac{23}{12}x^4 + 2x^3 + \frac{5}{2}x^2 + x + 1 \end{aligned}$$

+1

$$= 1.12721, \text{ at } x=0.1$$

$$\therefore \text{at } x=0.1, y=1.127.$$

+1

Q16. The given differential eqn is $\frac{dy}{dx} = x+y \Rightarrow f(x,y) = x+y$
 and the given values are $h=0.1, x_0=0, y_0=1$.

$$S_1 = hf(x_0, y_0) = (0.1)(0+1) = 0.1 \quad +1$$

$$\begin{aligned} S_2 &= hf\left(x_0 + \frac{h}{2}, y_0 + \frac{S_1}{2}\right) = (0.1)f(0+0.5, 1+0.5) \\ &\quad = (0.1)f(0.05+1.05) \\ &\quad = (0.1)(0.05+1.05) = 0.11 \end{aligned} \quad +1$$

$$\begin{aligned} S_3 &= hf\left(x_0 + \frac{h}{2}, y_0 + \frac{1}{2}S_2\right) = (0.1)f(0.05+1+0.055) = (0.1)(0.05+1.055) \\ &\quad = 0.1105 \end{aligned} \quad +1$$

$$\begin{aligned} S_4 &= hf(x_0+h, y_0+S_3) = (0.1)f(0.1, 1+0.1105) = (0.1)(0.1+1.1105) \\ &\quad = 0.12105 \end{aligned} \quad +1$$

$$\text{Here } x_1 = x_0 + h = 0+0.1 = 0.1$$

$$y_1 = y(0.1) = y_0 + \frac{1}{6}(S_1 + 2S_2 + 2S_3 + S_4) = 1 + \frac{1}{6}[0.1 + 2(0.11) +$$

$$2(0.1105) + 0.12105] \quad +1$$

$$= 1 + \frac{1}{6}[0.1 + 0.22 + 0.2210 + 0.12105]$$

$$= 1 + \frac{1}{6}[0.66205] = 1 + 0.11034$$

$$y_1 = 1.11034$$

$$\text{Hence at } x=0.1, y = 1.11034 \quad +1$$

Remark:- for second order.

$$S_1 = hf(x_0, y_0)$$

$$S_2 = hf\left(x_0 + \frac{h}{2}, y_0 + \frac{S_1}{2}\right)$$

$$\therefore y_1 = y_0 + \frac{1}{2}(S_1 + S_2)$$

9

Q17. Let Success = showing 5 or 6

probability of success $p = \frac{2}{6} = \frac{1}{3}$, failure $= \frac{2}{3}$ +1

Let X ~ Binomial ($n=6, p=\frac{1}{3}$)

we need

$$P(X \geq 3) = P(3) + P(4) + P(5) + P(6)$$

+1

$$P(3) = {}^6C_3 \left(\frac{1}{3}\right)^3 \left(\frac{2}{3}\right)^3 = 20 \cdot \frac{1}{27} \cdot \frac{8}{27} = \frac{160}{729}$$

$$P(4) = {}^6C_4 \left(\frac{1}{3}\right)^4 \left(\frac{2}{3}\right)^2 = 15 \cdot \frac{1}{81} \cdot \frac{4}{9} = \frac{60}{729}$$

$$P(5) = {}^6C_5 \left(\frac{1}{3}\right)^5 \left(\frac{2}{3}\right)^1 = 6 \cdot \frac{1}{243} \cdot \frac{2}{3} = \frac{12}{729}$$

$$P(6) = {}^6C_6 \left(\frac{1}{3}\right)^6 = \frac{1}{729}$$

$$P(X \geq 3) = \frac{160 + 60 + 12 + 1}{729} = \frac{233}{729}$$

+2

Expected no. of times

$$E = \frac{233}{729} = 233$$

+1

Q18. In poisson distribution

$$P(X=\gamma) = \frac{e^{-m} m^\gamma}{\gamma!}, \gamma=0, 1, 2, 3, \dots$$

+1

$$\begin{aligned}
 \mu'_1 &= \sum_{r=0}^{\infty} e^{-m} \frac{m^r r!}{r!} \\
 &= e^{-m} \sum_{r=0}^{\infty} \frac{m^r}{(r-1)!} = e^{-m} \left(m + \frac{m^2}{1!} + \frac{m^3}{2!} + \dots \right) \\
 &= m e^{-m} \left(1 + \frac{m}{1!} + \frac{m^2}{2!} + \dots \right) \\
 &= m e^{-m} \cdot e^m \\
 \Rightarrow \boxed{\mu'_1 = m} \\
 \boxed{\text{mean} = m}
 \end{aligned}$$

+2

$$\begin{aligned}
 \mu'_2 &= \sum_{r=0}^{\infty} e^{-m} \frac{m^r r^2}{r!} \\
 &= \sum_{r=0}^{\infty} e^{-m} \frac{m^r}{r!} \{ r(r-1) + r \} \\
 &= \sum_{r=0}^{\infty} \frac{e^{-m} m^r}{(r-2)!} + \sum_{r=0}^{\infty} \frac{e^{-m} m^r}{(r-1)!} \\
 &= m^2 \sum_{r=0}^{\infty} \frac{e^{-m} m^{r-2}}{(r-2)!} + m \sum_{r=0}^{\infty} \frac{e^{-m} m^{r-1}}{(r-1)!}
 \end{aligned}$$

$$\boxed{\mu'_2 = m^2 + m}$$

+2

$$\mu''_2 = \mu'_2 - \mu'^2_1$$

$$= m^2 + m - m^2$$

$$\Rightarrow \boxed{\mu''_2 = m = \text{variance}}$$

~~2~~

(5)

Q19 Exponential Distribution:— The exponential distribution is a continuous probability distribution used to model the time between independent events that occurs at a constant average rate.

The Probability density function of an exponential distribution is given by:

$$f(x) = \begin{cases} \lambda e^{-\lambda x}, & x \geq 0 \\ 0, & x < 0 \end{cases}$$

+1

To prove the total area under the exponential distribution curve is unity. i.e,

$$\int_{-\infty}^{\infty} f(x) dx = 1$$

$\because f(x)=0$ for $x<0$, the integral becomes

$$\int_{-\infty}^{\infty} f(x) dx = \int_0^{\infty} \lambda e^{-\lambda x} dx$$

$$= \lambda \int_0^{\infty} e^{-\lambda x} dx, \text{ let } u = \lambda x \Rightarrow du = \lambda dx \Rightarrow dx = \frac{du}{\lambda}$$

Substituting

$$= \lambda \int_{u=0}^{\infty} e^{-u} \frac{du}{\lambda} = \int_0^{\infty} e^{-u} du$$

$$= [-e^{-u}]_0^{\infty} = 0 + 1$$

+2

Q20. Let the required line be $y = mx + c$
 we use the Least Square method with the following normal equations:

$$\sum y = m \sum x + nc \quad \text{--- (1)}$$

$$\sum xy = m \sum x^2 + c \sum x \quad \text{--- (2)} \quad +2$$

x	y	x^2	xy
0	1.0	0	0.0
1	1.8	1	1.8
2	3.3	4	6.6
3	4.5	9	13.5
4	6.3	16	25.2

$$\sum x = 10 \quad \sum y = 16.9 \quad \sum x^2 = 30 \quad \sum xy = 47.1$$

Here $n = 5$.

\therefore eqn (1) & (2) becomes

$$16.9 = m(10) + 5c \Rightarrow 10m + 5c = 16.9 \quad \text{--- (3)}$$

$$47.1 = m(30) + c(10) \Rightarrow 30m + 10c = 47.1 \quad \text{--- (4)}$$

Solving eqn (3) & (4) we get

$$m = 1.33, c = 0.72$$

\therefore the required line is

$$y = 1.33x + 0.72 \quad +1$$

Q21.

$$\sigma = \frac{n \sum xy - \sum x \sum y}{\sqrt{[n \sum x^2 - (\sum x)^2][n \sum y^2 - (\sum y)^2]}} \quad +1$$

(6)

X	Y	X^2	Y^2	$X \cdot Y$
17	12	289	144	204
18	16	324	256	288
19	14	361	196	266
19	11	361	121	209
20	15	400	225	300
20	19	400	361	380
21	22	441	484	462
21	16	441	256	336
22	15	484	225	330
23	20	529	400	460
$\sum X = 200 \quad \sum Y = 160 \quad \sum X^2 = 4030 \quad \sum Y^2 = 2668 \quad \sum XY = 3235$				

$$\Rightarrow \gamma = \frac{380}{568.32} \approx 0.676$$

+2

+2

Q22. The Arithmetic mean of the Coefficient of regression is greater than the Coefficient of Correlation.

we know that $b_{yx} = \gamma \frac{\sigma_y}{\sigma_x}$, $b_{xy} = \gamma \frac{\sigma_x}{\sigma_y}$

Now, the Arithmetic mean of the two Regression Coefficients is:

$$AM = \frac{b_{yx} + b_{xy}}{2} = \frac{\gamma \frac{\sigma_y}{\sigma_x} + \gamma \frac{\sigma_x}{\sigma_y}}{2} = \gamma \cdot \frac{1}{2} \left(\frac{\sigma_y}{\sigma_x} + \frac{\sigma_x}{\sigma_y} \right)$$

Let $K = \frac{\sigma_y}{\sigma_x} \Rightarrow \frac{\sigma_x}{\sigma_y} = \frac{1}{K}$ so,

$$AM = \gamma \cdot \frac{1}{2} \left(K + \frac{1}{K} \right)$$

we use the inequality: $k + \frac{1}{k} \geq 2$ (for all $k \geq 0$)

$$\therefore AM \geq \sqrt{\frac{1}{2} \cdot 2} = \sigma$$

$$\Rightarrow \boxed{AM \geq \sigma}$$

+2.5

Product of Regression Coefficient is less than or equal to 1.

we know that $b_{yx} = \sigma \cdot \frac{\tau_y}{\tau_x}$, $b_{xy} = \sigma \cdot \frac{\tau_x}{\tau_y}$

Multiply both:

$$b_{yx} \cdot b_{xy} = \left(\sigma \cdot \frac{\tau_y}{\tau_x} \right) \cdot \left(\sigma \cdot \frac{\tau_x}{\tau_y} \right)$$

$$= \sigma^2$$

$$\therefore -1 \leq \sigma \leq 1 \Rightarrow 0 \leq \sigma^2 \leq 1$$

$$\therefore b_{yx} \cdot b_{xy} = \sigma^2 \leq 1.$$

+2.5

Section 6.

Q23. Type I error: Type I error occurs when the null hypothesis H_0 is true But we reject it. +1

Type II error: Type II error occurs when the null hypothesis H_0 is false But we fail to reject it. +1

Level of Significance: it is the Probability of making a Type I error. +1

Critical region: it is the set of all values of the test statistic that leads to rejection of the null hypothesis H_0 . +1

Critical Value: The Critical value is the Boundary Value that separates the Critical region from the non-Critical region. +1

(7)

Q24. Given $n=26$ (small samples)mean = $\bar{x} = 147$; S.D., $\sigma = 16$ (Variance are known)of degree of freedom, $v=n-1=25$.Null Hypothesis, H_0 : There is no difference in between the sample mean and population mean. i.e,the advertisement is not effective. i.e., $H_0: \mu = 140$. +1

$$\text{we have, } t = \frac{(\bar{x} - \mu)\sqrt{n-1}}{\sigma} = \frac{(147 - 140)\sqrt{25}}{16} = 2.19. \quad +1$$

The tabulated value of t at 5% level of significance and for $v=25$ dof is 1.708.clearly, calculated value of $|t| = 2.19 >$ tabulated value of $t = 1.708$. +1 \Rightarrow Null Hypothesis H_0 is Rejected. \Rightarrow the advertisement is effective. +1Q25. Given that: $n_1=9$ and $n_2=7$

$$\bar{x} = \frac{\sum x}{n_1} = \frac{333}{9} = 37, \quad \bar{y} = \frac{\sum y}{n_2} = \frac{238}{7} = 34.$$

Null Hypothesis $H_0: \sigma_1^2 = \sigma_2^2$. i.e, two populations have the same variance. +1

Group A

x	$x - \bar{x}$	$(x - \bar{x})^2$
18	-19	361

Group B

y	$y - \bar{y}$	$(y - \bar{y})^2$
29	-5	25

36	-1	1	26	-8	64
50	13	169	35	1	1
49	12	144	30	-4	16
36	-1	1	44	10	100
34	-3	9	46	12	144
49	12	144			
41	4	16			

$$\sum x = 333 \quad \sum y = 238 \quad 1134 \quad 386$$

we have $s_1^2 = \frac{\sum (x - \bar{x})^2}{n_1 - 1} = \frac{1134}{8} = 141.75$ +1

$$s_2^2 = \frac{\sum (y - \bar{y})^2}{n_2 - 1} = \frac{238}{6} = 64.33$$
 +1

clearly $s_1^2 > s_2^2$, then $F = \frac{s_1^2}{s_2^2} = \frac{141.75}{64.33} = 2.203$ +1

\therefore Calculated value < tabulated value

\rightarrow the null hypothesis H_0 is accepted

\rightarrow the two population have the same variance.