

[4]

ii. From the following data of two groups of students A and B drawn from normal populations, the marks obtained were as follows:

A:	18	20	36	50	49	36	34	49	41
B:	29	28	26	35	30	44	46		

Examine by F-test at 5% level, whether the two populations have the same variance. (Given $F(8, 6) = 4.15$ at 5% LOS)

OR iii. From the following data, find whether the accidents are uniformly distributed over the week. (given $\chi^2_{0.05}$ at 6 d.f. at 0.05% level of significance is 12.6)

Days	Sun.	Mon.	Tue.	Wed.	Thu.	Fri.	Sat.
No. of accidents	14	16	8	20	11	9	14

* * * * *

7

Total No. of Questions: 6

Total No. of Printed Pages:4

Enrollment No.....



Knowledge is Power

Faculty of Management

End Sem (Odd) Examination Dec-2018

MS3C010 Quantitative Techniques

Programme: BBA

Branch/Specialisation: Management

Duration: 3 Hrs.

Maximum Marks: 60

Note: All questions are compulsory. Internal choices, if any, are indicated. Answers of O.1 (MCOs) should be written in full instead of only a, b, c or d.

P.T.O.

[2]

- ix. Most of the nonparametric methods utilise measurements on: 1
(a) Interval scale (b) Ratio scale
(c) Ordinal scale (d) Nominal scale

x. A hypothesis may be classified as: 1
(a) Simple (b) Composite (c) Null (d) All of these

Q.2 i. Distinguish between correlation and regression analysis. 3
ii. Obtain the Spearman's rank Correlation Coefficient for the following 10 set of data: 7

X:	68	64	75	50	64	80	75	40	55	64
Y:	62	58	68	45	81	60	68	48	50	70

OR iii. You are given below the following information about advertisement expenditure and sales: 7

	Sales (X)	Adv. Exp. (Y)
Mean	50	10
Standard deviation	10	2

Correlation Coefficient = 0.9

- Q.3 i. What is a time series? Discuss about secular trend and seasonal variation. 3

ii. Calculate the 4-yearly moving averages of the data given below: 7

Years:	1991	1992	1993	1994	1995	1996	1997	1998
Sales	36	43	43	34	44	54	34	24

OR iii. Determine the equation of a straight line which best fits the following data: 7

Year:	1984	1985	1986	1987	1988
Sales:	35	56	79	80	40

Compute the trend values for all the years from 1984 to 1988.

Compute the trend values for all the years from 1984 to 1988.

[3] Q.4 i. From the following data, construct price index number by simple aggregate method: 3

	Base year prices	Current year prices
Milk per litre	11	12.50
Wheat per kg.	15	16
Apple per kg.	30	35
House Rent 2 rooms	3500	4500

- ii. Define Index numbers. Write various characteristics and types of Index numbers? 7

OR iii. Calculate Fisher's ideal index number for the following data: 7

	Base year 2009		Current year 2010	
Commodity	Price (Rs.)	Quantity (kg.)	Price (Rs.)	Quantity (Kg.)
A	4.50	20	10.50	22
B	7	40	13	45
C	14	4	32	5
D	16.50	3	28	2
E	5	2	9	1.5

- Q.5 i. State the addition theorem of probability for two events: 3
(a) When they are mutually exclusive
(b) When they are not mutually exclusive.

ii. Define Binomial distribution and state its main characteristics. The mean of a Binomial distribution is 20 and standard deviation 4, calculate Number of trials (n), Probability of success (p), and Probability of failure (q). 7

OR iii. Define probability. A problem in statistics is given to five students whose chances of solving it are $1/2$, $1/3$, $1/4$, $1/5$ and $1/6$ respectively. What is the probability that the problem will be solved? 7

Q.6 i. Differentiate between parametric and non-parametric test. 3

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Answer - 1

Q.1

- Ans. (i) (b) Same +1
 (ii) (d) -1 to 1 +1
 (iii) (d) all of these +1
 (iv) (d) all of these +1
 (v) (c) both (a) and (b) +1
 (vi) (a) percentages +1
 (vii) (d) all of these +1
 (viii) (b) $\frac{4}{10}$ +1
 (ix) (c) ordinal scale +1
 (x) (d) all of these +1

Answer - 2

Ans. (i) At least three Difference: +1 Marks
 for each difference +3

Ans. (ii) Here Rank are not given So we give rank to the following data set.

X	Y	R_x	R_y	$D = R_x - R_y$	D^2
68	62	4	5	-1	1
64	58	6	7	-1	1
75	68	2.5	3.5	-1	1
50	45	9	10	-1	1
64	81	6	1	5	25
80	60	1	6	-5	25
75	68	2.5	3.5	-1	1
40	48	10	9	1	1
55	50	8	8	0	0
64	70	6	2	4	16
					$\sum D^2 = 72$

In X-series, 75 repeated 2 times $\therefore m=2$

In X-series, 64 repeated 3 times $\therefore m=3$

In Y-series, 68 repeated 2 times $\therefore m=2$

Spearman's Rank Correlation Coefficient

$$R = 1 - \frac{6 \left[\sum D^2 + \frac{1}{12} (m^3 - m) + \frac{1}{12} (m^3 - m) + \frac{1}{12} (m^3 - m) \right]}{n^3 - n}$$

$$R = 1 - \frac{6 \left[72 + \frac{1}{12} (2^3 - 2) + \frac{1}{12} (3^3 - 3) + \frac{1}{12} (2^3 - 2) \right]}{10^3 - 10}$$

$$R = 1 - \frac{6 [72 + 0.5 + 2 + 0.5]}{990}$$

$$R = 1 - \frac{6(75)}{990}$$

$$R = 1 - \frac{450}{990}$$

$$\boxed{R = 0.545}$$

Ans

+1

Ans (iii)

(a) Two Regression lines

Regression line Y on X

$$(Y - \bar{Y}) = r \frac{\sigma_y}{\sigma_x} (X - \bar{X})$$

$$(Y - 10) = 0.9 \times \frac{2}{10} (X - 50)$$

$$Y - 10 = 0.18X - 9$$

$$Y = 0.18X - 9 + 10$$

$$\boxed{Y = 0.18X + 1} \quad -①$$

+3

Regression line X on Y

$$(X - \bar{X}) = r \frac{\sigma_x}{\sigma_y} (Y - \bar{Y})$$

$$(X - 50) = 0.9 \times \frac{10}{2} (Y - 10)$$

$$X - 50 = 4.5 (Y - 10)$$

$$X - 50 = 4.5Y - 45$$

$$\boxed{X = 4.5Y + 5} \quad -②$$

+3

(b) Let $X = \text{Sales}$

$Y = \text{Advertising Expenditure} = 20 \text{ crore}$

Put $Y = 20$ in eqn ①

$$X = 4.5Y + 5$$

$$X = 4.5(20) + 5$$

$$\boxed{X = 95 \text{ (crores)}}$$

Ans
+1

+1

Answer - 3

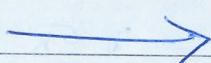
Ans(i) Time series : Definition +1 marks

secular Trend : Definition +1 marks

Seasonal variation : Definition +1 marks

+3

Ans(ii) 4-Yearly moving Averages



NOTE:- Student can find Trend or
Centred moving Average by
other method also but
final Centring should be
Same.

P.T.O.

(5)

MIRAJ

Page No.

Date:

PREMIUM

Year	Sales	4-Yearly moving Total (T)	4-Yearly moving Average (A)	4-Yearly moving average centered (C)
1991	36			
1992	43	156	39	
1993	43	164	41	$\frac{39+41}{2} = 40$
1994	34	175	43.75	42.375
1995	44	166	41.5	42.625
1996	54	156	39	40.25
1997	34			
1998	24			

$$\begin{array}{ccc} \uparrow & \uparrow & \uparrow \\ \boxed{+2} & \boxed{+2} & \boxed{+3} \end{array}$$

Ans(iii) Net eqn of straight line Trend be

$$Y = a + bX \quad \text{---(1)}$$

Normal eqn

$$\sum Y = n a + b \sum X \quad \text{---(2)}$$

$$\sum XY = a \sum X + b \sum X^2 \quad \text{---(3)}$$

+2

$$n = \text{no. of year} = 5$$

so we shift origin to middle year i.e. 1986

Year	Sales (Y)	$X = \text{Year} - 1986$	X^2	XY
1984	35	-2	4	-70
1985	56	-1	1	-56
1986	79	0	0	0
1987	80	1	1	80
1988	40	2	4	80
	$\sum Y = 290$	$\sum X = 0$	$\sum X^2 = 10$	$\sum XY = 34$

Put value from table in eqn ② & ③

$$290 = 5a$$

$$a = 58$$

$$34 = 10b$$

$$b = 3.4$$

Put value of a and b in ①
we get eqn of straight line
Trend.

$$Y = 58 + 3.4X \quad - ④$$

Trend values from 1984 to 1988

Year	X	$Y = 58 + 3.4(X)$ [Trend values]
1984	-2	$Y = 51.2$
1985	-1	$Y = 54.6$
1986	0	$Y = 58$
1987	1	$Y = 61.4$
1988	2	$Y = 64.8$

Answer - 4

Ans-(i)

	P_o	P_L	
milk	11	12.5	
wheat	15	16	
Apple	30	35	
House Rent	3500	4500	
	$\sum P_o = 3556$	$\sum P_L = 4563.5$	+1

Simple Aggregate method

$$P_{oL} = \frac{\sum P_L \times 100}{\sum P_o}$$

$$P_{oL} = \frac{4563.5}{3556} \times 100$$

$$\boxed{P_{oL} = 128.33} \quad \text{Ans}$$

+1

+1

Ans-(ii) Index-number : Definition

+1 marksTypes : Three Types
definition+1 for eachtype def.

Characteristics : At least three characteristics for each described.

+7

or

Ans(iii)

	P_0	q_{r_0}	P_1	q_{r_1}	$P_0 q_{r_0}$	$P_0 q_{r_1}$	$P_1 q_{r_0}$	$P_1 q_{r_1}$
A	4.5	20	10.5	22	90	99	210	231
B	7	40	13	45	280	315	520	585
C	14	4	32	5	56	70	128	160
D	16.5	3	28	2	49.5	33	84	56
E	5	2	1	1.5	10	7.5	18	13.5
					$\sum P_0 q_{r_0}$ = 485.5	$\sum P_0 q_{r_1}$ = 524.5	$\sum P_1 q_{r_0}$ = 960	$\sum P_1 q_{r_1}$ = 1048.5

Fisher's Ideal Index number

$$P_{01} = \sqrt{\frac{\sum P_1 q_{r_0}}{\sum P_0 q_{r_0}} \times \frac{\sum P_1 q_{r_1}}{\sum P_0 q_{r_1}}} \times 100$$

+2

$$P_{01} = \sqrt{\frac{960}{485.5} \times \frac{1048.5}{524.5}} \times 100$$

$$\boxed{P_{01} = 198.34}$$

Ans

+1

Answer - 5

- (a) ~~to~~ Addition Theorem when
Events are mutually
Exclusive

$$P(A \cup B) = P(A) + P(B)$$

+1.5

- (b) Addition Theorem when
Events are not mutually Exclusive

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

+1.5

+3

Ans(iii) Binomial Distribution: Definition +2 +2

Characteristics : At least four +0.5

for each

$$= 4 \times 0.5 \\ = \boxed{2}$$
+2

Given mean, $np = 20$ +1

$$\text{s.d.}, \sqrt{npq} = 4 \quad \text{---(2)}$$

On squaring both sides of eqn (2)

$$npq = 16 \quad \text{---(3)}$$

divide eqn (3) by eqn (1) we get

$$\frac{npq}{np} = \frac{16}{20}$$

$$q = 0.8$$

~~1~~

+1

w.k.t

$$P + q = 1$$

$$P + 0.8 = 1$$

$$P = 1 - 0.8$$

$$\boxed{P = 0.2}$$

+1

$$\therefore np = 20 \quad \text{from (1)}$$

$$\therefore n(0.2) = 20$$

$$\boxed{n = 100}$$

+1

$$n = 100, \quad P = 0.2, \quad q = 0.8 \quad *$$

Ans(iii) Let A, B, C, D, E be the event

that problem solved by five students respectively.

$$\therefore P(A) = \frac{1}{2}, P(B) = \frac{1}{3}, P(C) = \frac{1}{4}, P(D) = \frac{1}{5}$$

$$P(E) = \frac{1}{6}$$

+1

Prob. that A fails to solve the problem

$$P(\bar{A}) = 1 - P(A) = 1 - \frac{1}{2} = \frac{1}{2}$$

Prob. that B fails to solve the problem

$$P(\bar{B}) = 1 - P(B) = 1 - \frac{1}{3} = \frac{2}{3}$$

Prob. that C fails to solve the problem

$$P(\bar{C}) = 1 - P(C) = 1 - \frac{1}{4} = \frac{3}{4}$$

Prob. that D fails to solve the problem

$$P(\bar{D}) = 1 - P(D) = 1 - \frac{1}{5} = \frac{4}{5}$$

Prob. that E fails to solve the problem

$$P(\bar{E}) = 1 - P(E) = 1 - \frac{1}{6} = \frac{5}{6}$$

+2

\therefore Prob. that none of them will able to solve problem

$$= \frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \frac{4}{5} \times \frac{5}{6}$$

$$= \frac{1}{6}$$

+1

(11)

MIRAJ

Page No.

Date:

PREMIUM

Problem will be solved if any of them
will solve it

i.e. $P(A \cup B \cup C \cup D \cup E) = 1 - P(\text{None of them will solve})$

$$= 1 - \frac{1}{6}$$

$P(A \cup B \cup C \cup D \cup E) = \frac{5}{6}$	+
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+3

Answer-6

Ans(i) Difference between

Parametric and non-parametric test

[+1 for each difference]

At least three differences

+3

Ans(ii) First group (A)

x_1	$(x_1 - \bar{x}_1)$	$(x_1 - \bar{x}_1)^2$
18	-19	361
20	-17	289
36	-1	1
50	13	169
49	12	144
36	-1	1
34	-3	9
49	2	144
42	4	16

Second Group (B)

x_2	$x_2 - \bar{x}_2$	$(x_2 - \bar{x}_2)^2$
29	-5	25
28	-6	36
26	-8	64
35	1	1
30	-4	16
44	10	100
46	12	144

+3

$$\sum x_1 = 333 \quad \sum (x_1 - \bar{x}_1) = 0 \quad \sum (x_1 - \bar{x}_1)^2 = 1134$$

$$\sum x_2 = 238 \quad \sum (x_2 - \bar{x}_2) = 0 \quad \sum (x_2 - \bar{x}_2)^2 = 386$$

$$\text{Mean of } A, \bar{X}_1 = \frac{\sum X_1}{n_1} = \frac{333}{9} = 37$$

$$\text{Mean of } B, \bar{X}_2 = \frac{\sum X_2}{n_2} = \frac{238}{7} = 34$$

$$\text{Variance of } A, S_1^2 = \frac{\sum (X_1 - \bar{X}_1)^2}{n_1 - 1}$$

$$S_1^2 = \frac{1134}{9-1} = 141.75$$

+1

$$\text{degree of freedom (d.f.)} = n_1 - 1 = 9 - 1 = 8$$

$$\text{Variance of } B, S_2^2 = \frac{\sum (X_2 - \bar{X}_2)^2}{n_2 - 1}$$

$$S_2^2 = \frac{386}{7-1} = 64.34$$

+1

$$\text{d.f.}_2 = n_2 - 1 = 7 - 1 = 6$$

$$\therefore F\text{-test} = \frac{S_1^2}{S_2^2} \quad \because S_1^2 > S_2^2$$

$$F(8, 6) = \frac{141.75}{64.34} = 2.20$$

+2

Given

$$\text{Tabulated } F_{(8, 6)} = 4.15$$

Here Calculated F is less than tabulated F.

So we accept null hypotheses.
 \therefore population have same variance.

Ans(iii) Let us set up null hypothesis that accidents are uniformly distributed over the week.

Under null hypothesis Expected frequencies is given by = $\frac{14+16+8+20+11+9+14}{7}$

$$= \frac{92}{7} = 13.14$$

Calculation of χ^2

No. of accidents	Expected freq.	$f_o - f_e$	$(f_o - f_e)^2$	$(f_o - f_e)^2 / f_e$	
f_o	f_e	$f_o - f_e$	$(f_o - f_e)^2$	$(f_o - f_e)^2 / f_e$	
14	13.14	0.86	0.7396	0.0563	
16	13.14	-2.86	8.1796	0.6225	
8	13.14	-5.14	26.4196	2.0106	
20	13.14	6.86	47.0596	3.5814	+3
11	13.14	-2.14	4.5796	0.3485	
9	13.14	-4.14	17.1396	1.3044	
14	13.14	0.86	0.7396	0.0563	
				$\sum (f_o - f_e)^2 / f_e$	
				= 7.98	

$$\chi^2 = \sum (f_o - f_e)^2 / f_e = 7.98 \quad +3$$

$$d.f. = n-1 = 7-1 = 6$$

Given
Calculated Tabulated

$$\chi^2 = 12.6 \text{ at } 6 \text{ d.f.}$$

Here $\chi^2_{\text{calculated}}$ is less than $\chi^2_{\text{tabulated}}$,

so we accept null hypothesis.

1. accidents are uniformly distributed.