

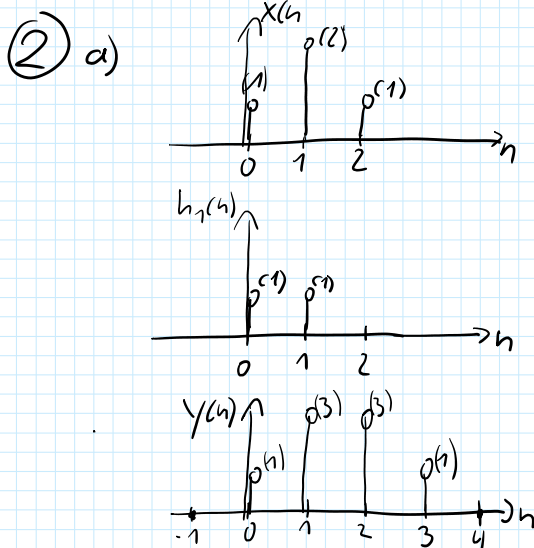
$$h(n) = \delta(n+1) + \sum_{k=0}^{\infty} 2^k \delta(n-k)$$

$$\delta(n-k) \begin{cases} 1 & \text{für } n=k \\ 0 & \text{sonst} \end{cases}$$

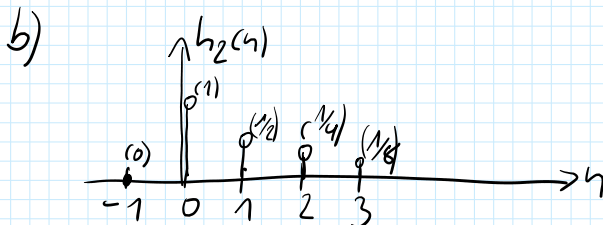
$$\delta(n+1) \begin{cases} 1 & \text{für } n=-1 \\ 0 & \text{sonst} \end{cases}$$

b) stabil wenn: $\sum_{n=-\infty}^{\infty} |h(n)| < \infty \Rightarrow |a| < 1$
 stable if:

c) anticausal für $a=0$, weil $h(n) = \delta(n+1)$ anticausal
 anticausal for, because anticausal



$$y(n) = \delta(n) + 3\delta(n-1) + 3\delta(n-2) + \delta(n-3)$$



$$\sum_{k=0}^{\infty} (0.5)^k \delta(n-k) = a^n \cdot \varepsilon(n)$$

c) $H_2(f) = \sum_{n=-\infty}^{\infty} h_2(n) \cdot e^{-j2\pi n f T}$

$$= \sum_{n=0}^{\infty} 0.5^n \cdot e^{-j2\pi n f} = \sum_{n=0}^{\infty} \overbrace{(0.5 \cdot e^{-j2\pi f})^n}^a \quad c=1$$

$$= \frac{1}{1 - 0.5 e^{-j2\pi f}}$$

$$\sum_{n=0}^{\infty} c \cdot a^n = \frac{c}{1-a}, \text{ für } |a| < 1$$

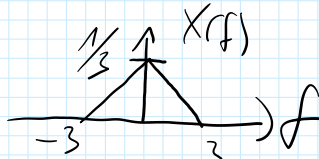
nl4

$$1 - 0.5 e^{-x/4}$$

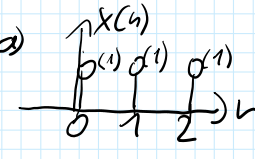
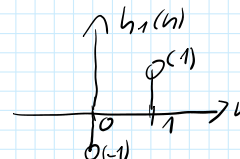
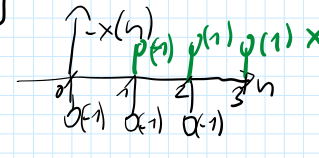
$$n=0$$

alt.

$$h_2(n) = \sum_{k=0}^{\infty} 0.5^k \delta(n-k) = 0.5^n \cdot \varepsilon(n) \rightarrow \frac{1}{1-0.5} e^{-j2\pi f} = H_2(f) \quad (\text{Tab. 18})$$

d)  $\Rightarrow T = 1/6$
da $\frac{1}{T} \geq 2 \cdot 3$ Abtasttheorem
sample theor.

e) $H(f) = a \cdot \text{rect}(f/6)$
 $X_a(f) = \frac{1}{T} \sum_{k=-\infty}^{\infty} X(f - \frac{k}{T})$ $\left. \begin{array}{l} a \cdot \frac{1}{T} \stackrel{!}{=} 1 \\ \Rightarrow a = T = 1/6 \end{array} \right\}$

③ a)  * 
 $y(n) = x(n) * h_1(n)$
 $= x(n) * [-\delta(n) + \delta(n-1)]$
 $= -x(n) + x(n-1)$
 $\underline{y(n) = -\delta(n) + \delta(n-3)}$


b) $h_1(n) \rightarrow H_1(f)$
 $H_1(f) = \frac{1}{T} \sum_{n=-\infty}^{\infty} h_1(n) e^{-j2\pi n f T} \quad |T=1$
 $= \sum_{n=-\infty}^{\infty} h_1(n) e^{-j2\pi n f}$
 $= \sum_{n=-\infty}^{\infty} [-\delta(n) + \delta(n-1)] e^{-j2\pi n f}$
 $= -e^{-j2\pi f \cdot 0} + e^{-j2\pi f \cdot 1} = \underline{\underline{-1 + e^{-j2\pi f}}}$

alt.: $\left[\begin{array}{l} \delta(n) \rightarrow 1 \\ x(t-t_0) \rightarrow X(f) \cdot e^{-j2\pi f t_0} \end{array} \right]$

$$H_1(f) = e^{-j2\pi f} \cdot 1 = \cos(2\pi f) - 1 - j \sin(2\pi f)$$

$$H_1(f) = e^{-j2\pi f} \cdot 1 = \cos(2\pi f) - 1 - j\sin(2\pi f)$$

$$\operatorname{Re}\{H_1(f)\} = \cos(2\pi f) - 1$$

$$\operatorname{Im}\{H_1(f)\} = -\sin(2\pi f)$$

c) $b = 0$

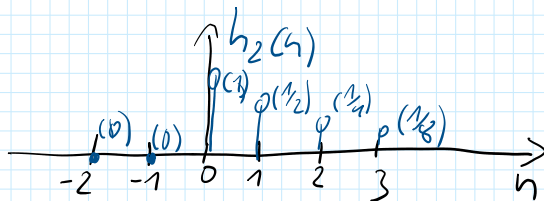
a beliebig, da alle Impulse bei $n < 0$
in diesem Fall verschwinden

a arbitrary, because all impulses at $n < 0$
disappear in this case

d) b : beliebig arbitrary

$|a| < 1$ in diesem Fall konvergiert die geom. Reihe
in this case the geom. series converges

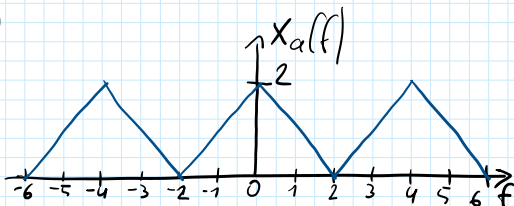
e)



f) $h_2(n) = \sum_{k=0}^{\infty} 0.5^k \cdot \delta(n-k) = 0.5^n \cdot \mathcal{E}(n)$ (Tab. 18)

$$0.5^n \mathcal{E}(n) \rightarrow \frac{1}{1 - 0.5 e^{-j2\pi f}} = H_2(f)$$

④ a)



$$X_b(f) = X(f) * \frac{1}{4} \cdot \sum_{k=-\infty}^{\infty} \delta(f - \frac{k}{4})$$

b) $H(f) = \frac{1}{4} \cdot \operatorname{rect}(f/4) \rightarrow \operatorname{sinc}(4\pi f) = h(t)$

$$b) |h(f)| = \frac{1}{4} \cdot \text{rect}\left(\frac{f}{4}\right) \rightarrow \underline{\underline{\text{si}(4\pi f) = \text{sinc}(f)}}$$

$$c) \underline{s(0)} = b \cdot \underline{s(0)} = 1$$

$$d) a=0$$

$b = \text{beliebig, arbitrary}$

weil bei $a=0$ kein Impuls von $n < 0$
because with $a=0$ no impulse before $n < 0$

$$e) s(n) = \sum_{k=0}^{\infty} \left(\frac{3}{10}\right)^k \delta(n-k)$$

$$= \left(\frac{3}{10}\right)^k \cdot \epsilon(n) \rightarrow \frac{1}{1 - \frac{3}{10} \cdot e^{j2\pi f}}$$

$$⑤ a) \text{ min. Periode: } \frac{1}{f_0} = \frac{2}{3}$$

min. period:

$$\text{nächste Periode: } \frac{1}{f_1} = \frac{4}{3} \Rightarrow T_1 = \frac{3}{4}$$

$$\text{next period: } \frac{1}{f_2} = \frac{6}{3} \Rightarrow T_2 = \frac{1}{2}$$

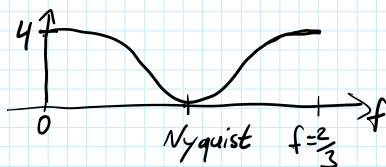
$$b) |H(f)| = 2 \cos(3\pi f) + 2$$

$$f(f) = 0$$

$$c) \text{ ja, weil } p(f) = c \cdot f \text{ hier: } c=0$$

yes, because $p(f) = c \cdot f$ here: $c=0$

$$d) H(f) = 2 \cos(3\pi f) + 2$$



Tiefpass, da Maximum bei $f=0$
und Minimum bei $f = \frac{1}{2T_0}$

Low-Pass, because maximum at $f=0$
and minimum at $f = \frac{1}{2T_0}$

$$e) H(f) = 2 \cos(3\pi f) + 2$$

$$\delta(n+n_0) + \delta(n-n_0) \rightarrow 2 \cos(2\pi f n_0 T)$$

$$\Rightarrow 2n_0 T_0 = 3 \Rightarrow n_0 = \frac{3}{2T_0} = \frac{3}{2} \cdot \frac{2}{3} = 1$$

$$\Rightarrow h(n) = 2\delta(n) + \delta(n-1) + \delta(n+1)$$

$$f) \text{ min. d. } |h(n)| \neq 0 \text{ für } n \neq 0$$

$$\Rightarrow h(n) = 2\delta(n) + \delta(n-1) + \delta(n+1)$$

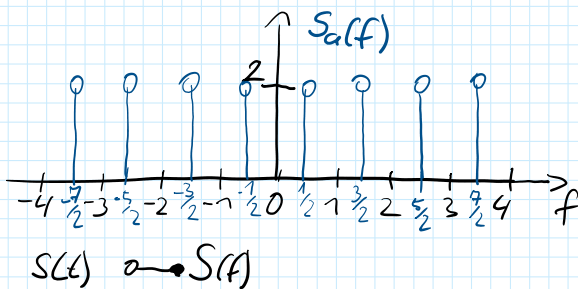
f) nein, da $h(n) \neq 0$ für $n < 0$
 no, because $h(n) \neq 0$ for $n < 0$

⑥ a) $3\pi t = 2\pi \frac{3}{2} t \Rightarrow T_0 = \frac{2}{3}$

b) $\int_{-\infty}^{\infty} 2 \cos(3\pi t) dt \rightarrow \infty$

\Rightarrow Leistungssignal, power signal

c)



$$s(t) = 2 \cos(3\pi t) \longleftrightarrow \delta(f + \frac{3}{2}) + \delta(f - \frac{3}{2}) = S(f)$$

$$\begin{aligned} S_a(f) &= S(f) * \frac{1}{0.5} \sum_{k=-\infty}^{\infty} \delta(f + \frac{k}{0.5}) \\ &= S(f) * 2 \sum_{k=-\infty}^{\infty} \delta(f + 2k) \end{aligned}$$

d) Ja, da die Signalfrequenz ($\frac{3}{2}$) $> \frac{1}{2}$ Abtastfrequenz (1)
 \Rightarrow Abtasttheorem $2f_g \leq \frac{1}{T}$ nicht erfüllt

Yes, because signal frequency ($\frac{3}{2}$) $> \frac{1}{2}$ sampling frequency (1)
 \Rightarrow sampling theorem $2f_c \leq \frac{1}{T}$ not fulfilled

e) $H(f) \longleftrightarrow h(t)$
 $\text{rect}(\frac{f}{4}) \longleftrightarrow 4 \text{si}(4\pi t)$

$$\begin{cases} \text{rect}(f) \longleftrightarrow \text{si}(\pi t) \\ \frac{1}{6} \text{rect}(\frac{f}{6}) \longleftrightarrow \text{si}(\pi 6t) \end{cases}$$

f) Signalausschnitt durch $H(f)$: $H(f) \cdot S(f)$

f) Signalauschnitt durch $H(f)$: $H(f) \cdot S_a(f)$
signal output due to $H(f)$:

$$2 [\delta(f + \frac{1}{2}) + \delta(f - \frac{1}{2})] + 2 [\delta(f + \frac{3}{2}) + \delta(f - \frac{3}{2})]$$

$$\downarrow$$
$$4 \cos(2\pi \frac{1}{2} t) + 4 \cos(2\pi \frac{3}{2} t)$$

$$\Rightarrow g(t) = 4 [\cos(\pi t) + \cos(3\pi t)]$$