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## **Behavior of Embedded Systems**

Part A: Petri Nets



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**Group Discussion** 

Why is Structure not enough?

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## **Formal Languages**

Behavior is typically described using formal languages.

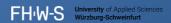
The use of formal languages allows (among others)

- Formal **Proof of Concept**
- Simulation
- Analyses (e.g. **Deadlock** and **Lifelock** detection, finding an **Equilibrium**)
- Verification
- Test Case Generation
- .



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## **Automata Theory**



#### **Finite State Machines**

Automata typically have

- A formal representation
- A graphical representation

Automata foremost consist of

- States
- **Transitions**

Further concepts include:

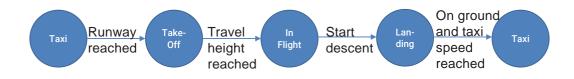
- Start/initial states
- Final/accepting states
- **Events and Conditions**

Depending on the language the focus is either on

- the States
- the **Transitions**
- or **Both**

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### **State vs Transition**





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What is an Alphabet?

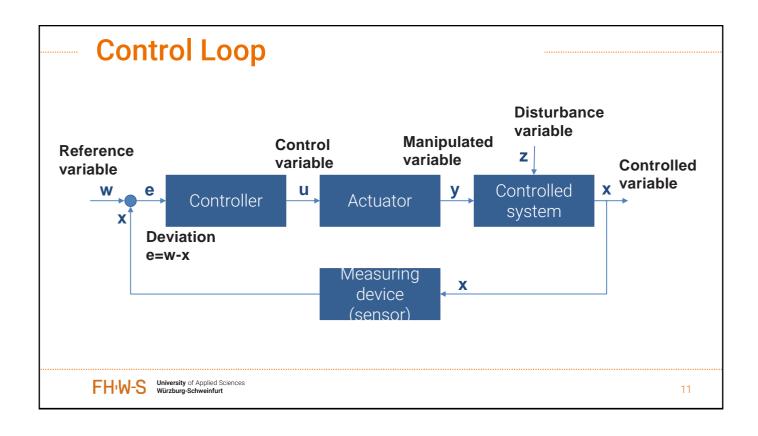
What are basic Operators?

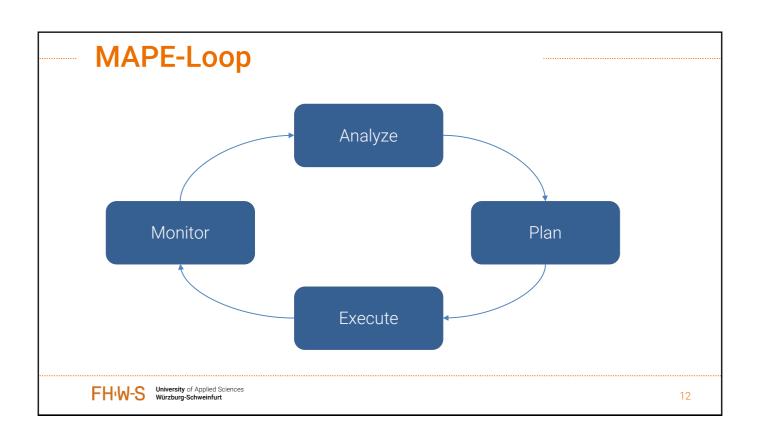
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# Remember Control- and MAPE-Loops

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## **Petri Nets**

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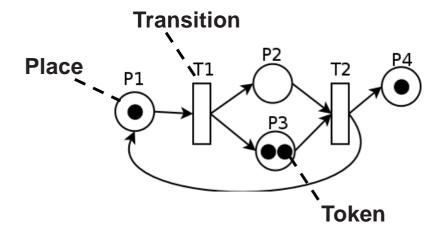
#### **Online-Materials**

Introduction videos to Petri Nets can be found at:

https://youtu.be/GCsVxWh9950 https://youtu.be/WGSAi9-QUwk https://youtu.be/1IPOIE0PvQY

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## **Elements**

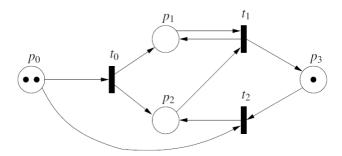


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#### Petri nets

Is transition  $t_2$  of the petri net shown below enabled? (Capacity of places is  $\infty$ ) What is the marking after  $t_2$  fires?



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## Model a Traffic Light using Petri Nets

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## **Analysis**

#### Terms:

A transition is dead, if it is not enabled in any marking.

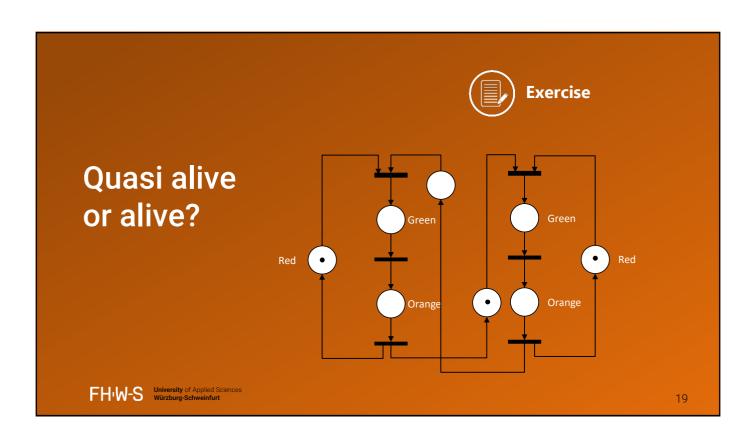
A transition t is potentially **fireable**, when there is at least one marking reachable, which enables t.

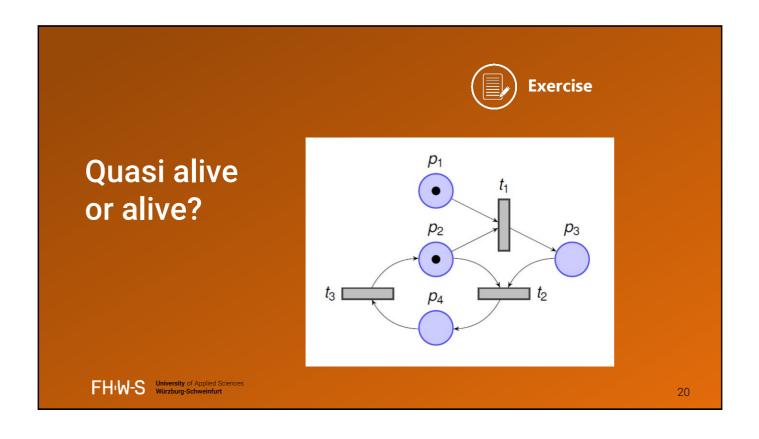
A petri net is dead, if no transition is able to fire in a given marking.

A petri net is quasi alive, if not dead under any future marking.

A petri net is **alive**, when all transitions are potentially fireable for all future markings.

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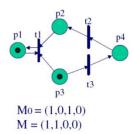


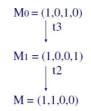


## **Reachability Graph**

Firing sequence for a petri net G and initial marking M0 is a sequence of transitions  $t_0, \dots, t_n$ , such that  $M_0 \xrightarrow[G,t_0]{} M_1 \xrightarrow[G,t_n]{} M_n$ 

Reachability graph: The reachability graph of G is the transition relation  $\underset{G}{\rightarrow}$  restricted to its reachable markings R(G). It is the state space of the net.

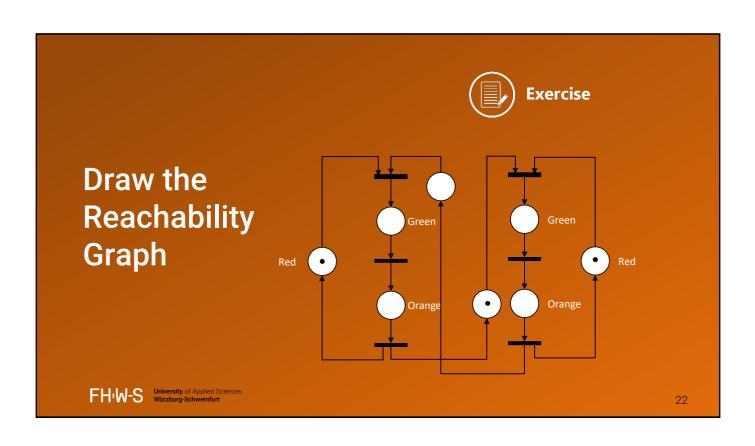


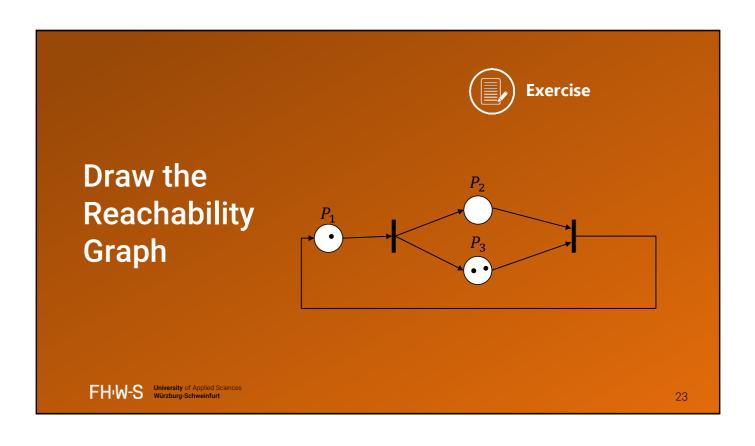


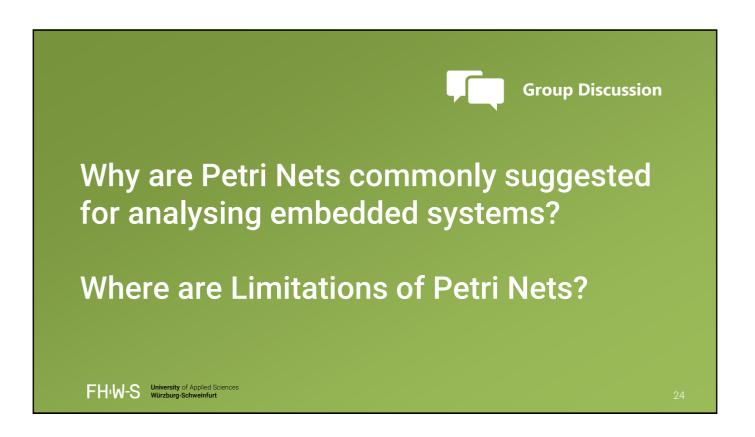
Nassar, K., & Casavant, A. (2008). Analysis of timed Petri nets for reachability in construction applications. *Journal of Civil Engineering and Management*, 14(3), 189-198.

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## For home: Google the Dining Philosophers Problem and Model it with Petri Nets

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## **Questions for Self-Assessment**

What are the basic concepts of automata theory?

What is a petri net?

When does a petri net fire?

Are petri nets deterministic?

When is a petri net dead, alive, quasi alive?

What is a reachability graph?

What are shortcomings of petri nets?

Why are petri nets often suggested for modelling embedded systems?

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## Literature

Introduction to Automata Theory, Languages, and Computation. 3<sup>rd</sup> Edition, Pearson Education, 2006. [Hopcroft et al. 2006]

Reisig, W.: Petri Nets and Algebraic Specifications. In: Theoretical Computer Science, 80(1), 1991, pp. 1-34. [Reisig 1991]

