

Exam in "Digital Signal Processing and State Space Control" (Part: State Space Control)								
10 Pages		Examiners:	Dr. B. Müller Dr. T. Rommel					
Date:	11/02/2023		•		WS 22/23			
Duration:	90 Minutes (both parts)	Points / Grade:		/				
Name:		Matriculation no.:						

Task:	1	2	3	Σ
Max. Points:	13	13	15	41
Achieved Points:				

Authorized aids: - non-programmable calculator

Please note:

- The examination is to be done independently and without any help. Cheating and attempted cheating will always be sanctioned.
- Mobile phones, notebooks or programmable calculators are not permitted.
- Mobile phones must be switched off and put on a desk in the front row.
- Please write down your name and matriculation no. on the task sheets.
- Write your solutions directly on the respective task sheet.
- Only if your approach to a solution/answer is written down comprehensibly and transparently, it is marked and graded. If you give more than one approach to a solution, only the one that is highlighted is marked and graded.
- Please hand back all task sheets and write your name on them!

Please do not use a red pen.

Good luck!

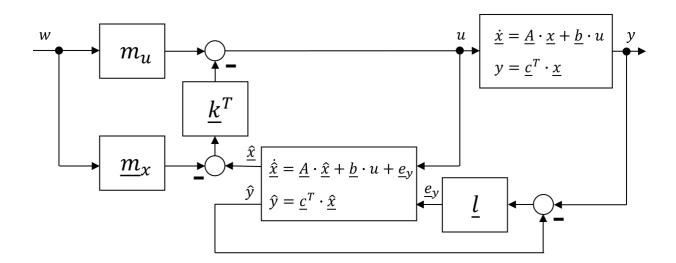




Task 1: Questions 13 Points

- a) Consider the block diagram below showing a state-space-controlled system. Mark the following subsystems in the block diagram:
 - plant
 - observer
 - state feedback controller
 - static feedforward

Note: Your solution must clearly and uniquely assign <u>each</u> component of the block diagram to one of the subsystems above. One subsystem may consist of more than one block.





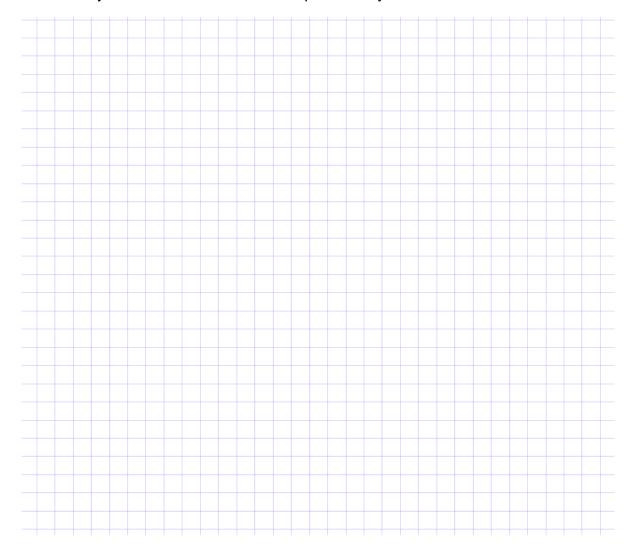
b) A system is described by the state equations

$$\dot{x}_1 = -2x_1 + 3.7x_2 + 1.2u$$

$$\dot{x}_2 = 0.3x_1 + 7.12x_2 - 0.25u$$

$$y = 12u + 2(x_1 + x_2)$$

What is the order of the system? Is the system linear or nonlinear? Explain briefly!





c) One of the following three transfer functions

•
$$F_1(s) = \frac{(s+4)}{(s+2)(s+3)(s+5)}$$

•
$$F_2(s) = \frac{(s+20)}{(s+2)(s+7)}$$

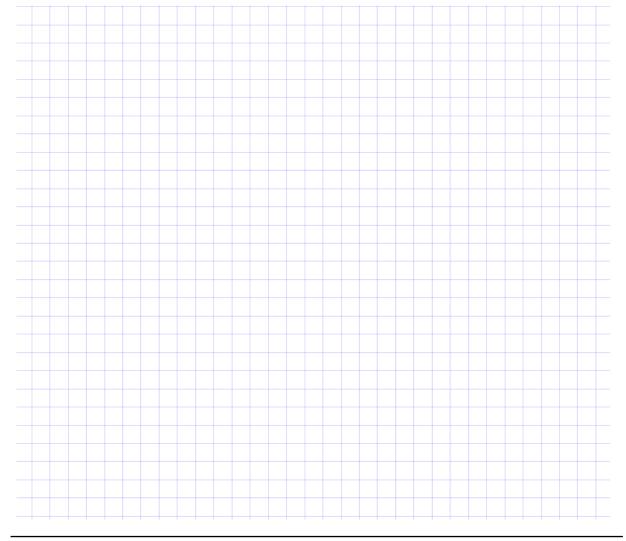
•
$$F_3(s) = \frac{1}{(s+2)(s+3)(s+4)}$$

describes the input-output behavior of the plant with the state equations

$$y = \begin{bmatrix} 1 & 4 & 2 \end{bmatrix} \underline{x}$$

Specify which one is the correct transfer function by excluding the other two given possibilities. Explain (briefly)!

Hint: There is no calculation needed in order to answer this question!





Task 2: Solution of the State Equations

13 Points

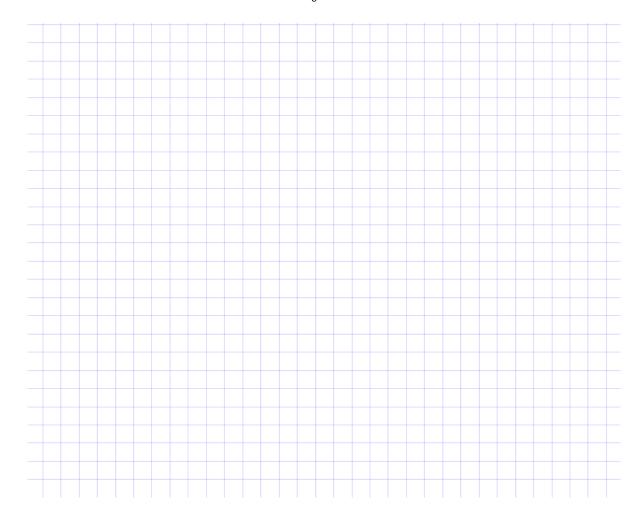
A system is given by the following state equations:

$$\dot{x} = 3x + 3u$$
$$y = -3x$$

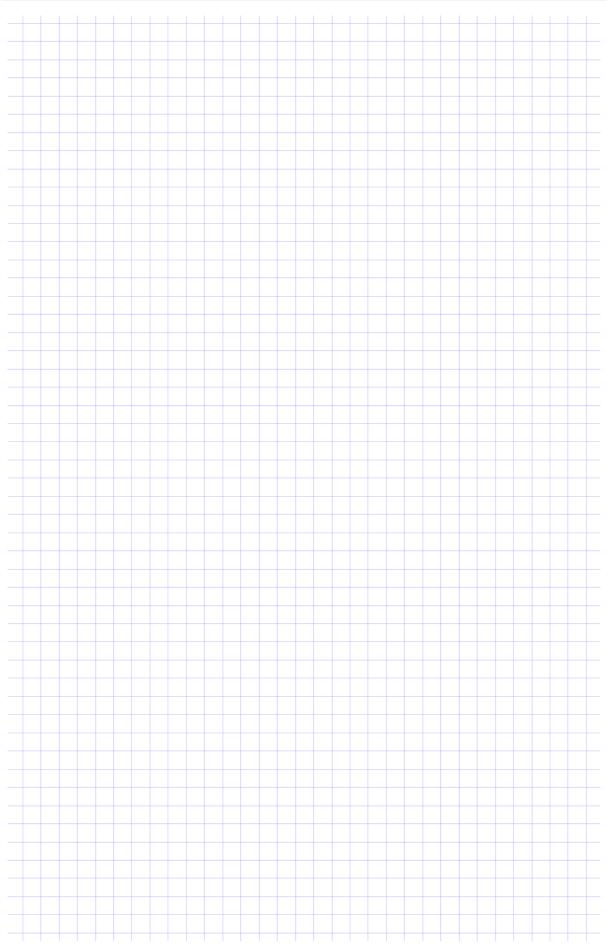
- a) What is the order of the system?
- b) Is the system asymptotically stable? Why (not)?
- c) Determine the output signal y(t) for $t \ge 0$ assuming the initial state $x_0 = x(0) = 1$ and the constant input u(t) = -2 for $t \ge 0$.

Hint: The general solution formula for an LTI SISO system in state space form is

$$\underline{x}(t) = \underline{e}^{\underline{A}t}\underline{x}_0 + \int_0^t \underline{e}^{\underline{A}(t-\tau)}\underline{b}u(\tau)d\tau$$





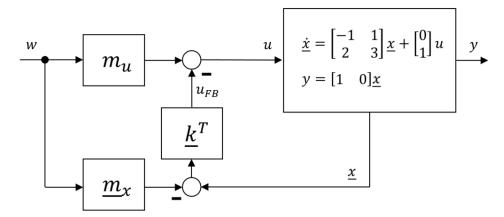




Task 3: State Space Controller Design

15 Points

Consider the state-space-controlled system



- a) Show that the <u>plant</u> in this block diagram is completely controllable!
- b) Calculate \underline{k}^T , m_u and \underline{m}_x such that
 - the closed-loop system has the eigenvalues $\lambda_{C,1} = -1$ and $\lambda_{C,2} = -2$;
 - y = w and $u_{FB} = 0$ holds in steady state for arbitrary constant inputs w.

Hint:
$$\begin{bmatrix} -1 & 1 & 0 \\ 2 & 3 & 1 \\ 1 & 0 & 0 \end{bmatrix}^{-1} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 1 \\ -3 & 1 & -5 \end{bmatrix}$$

