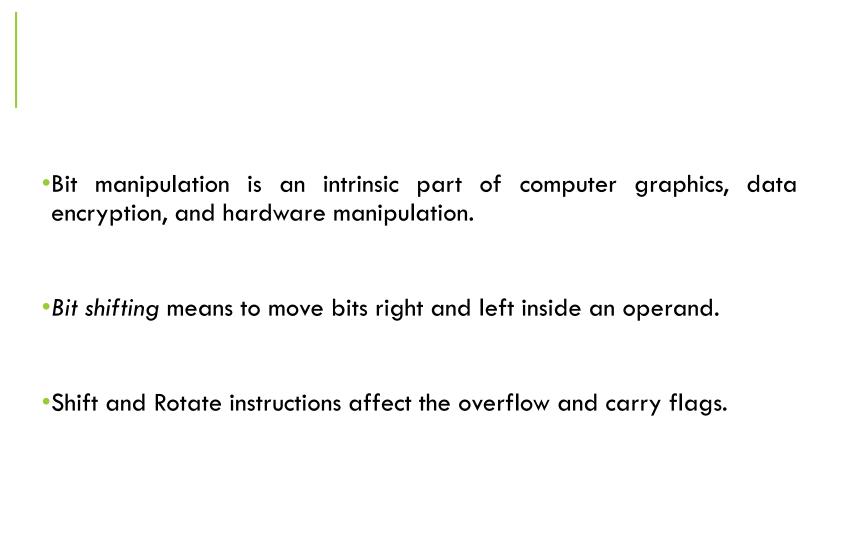
# INTEGER ARITHMETIC

# **OUTLINES**

Shift and Rotate Instructions

Multiplication and Division Instructions

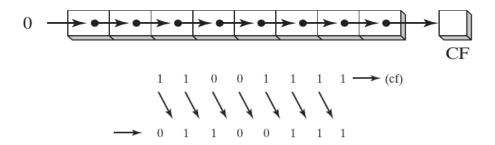


# 7.1 SHIFT AND ROTATE INSTRUCTIONS

- •Bit shifting means to move bits right and left inside an operand.
- Shift and Rotate instructions affect the overflow and carry flags.

#### **Logical Shifts and Arithmetic Shifts**

- There are two ways to shift an operand's bits.
- 1. Logical Shift fills the newly created bit position with zero.
  - each bit is moved to the next lowest bit position, and the newly created bit position is filled with zero.



2. Arithmetic Shift: The newly created bit position is filled with a copy of the original number's sign bit:

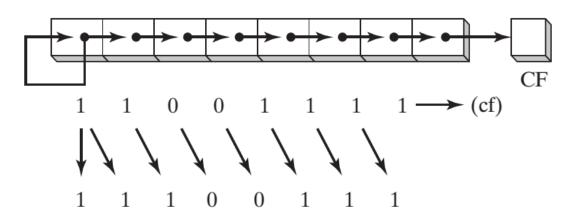


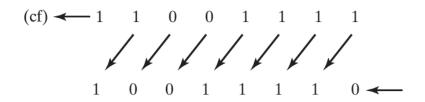
Table 7-1 Shift and Rotate Instructions.

| SHL  | Shift left                   |  |
|------|------------------------------|--|
| SHR  | Shift right                  |  |
| SAL  | Shift arithmetic left        |  |
| SAR  | Shift arithmetic right       |  |
| ROL  | Rotate left                  |  |
| ROR  | Rotate right                 |  |
| RCL  | Rotate carry left            |  |
| RCR  | Rotate carry right           |  |
| SHLD | Double-precision shift left  |  |
| SHRD | Double-precision shift right |  |

# SHL INSTRUCTION

SHL Instruction performs a logical left shift on the destination operand, filling the lowest bit with 0.

 The highest bit (msb) is moved to the Carry flag, and the bit that was in the Carry flag is discarded



Operand types for SHL:

SHL reg, imm8
SHL mem, imm8
SHL reg, CL
SHL mem, CL

#### E.g.

```
mov bl,8Fh; BL = 10001111b; CF = 1, BL = 00011110b; mov al,10000000b; CF = 0, AL = 00000000b
```

Bitwise multiplication is performed when you shift a number's bits in leftward direction (toward the MSB).

mov dl,5 Before: 
$$0\ 0\ 0\ 0\ 1\ 0\ 1 = 5$$
shl dl,1 After:  $0\ 0\ 0\ 0\ 1\ 0\ 1\ 0 = 10$ 

- •SHL can perform multiplication by powers of 2.
- •Shifting any operand left by n bits multiplies the operand by  $2^n$ .
- •For example, shifting the integer 5 left by 1 bit yields the product of 5  $\times$  2  $^{1}$  = 10.
- •If binary 00001010 (decimal 10) is shifted left by two bits, the result is the same as multiplying 10 by  $2^2$

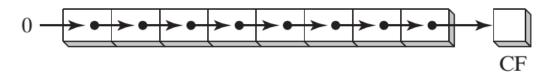
```
mov dl,10 ; before: 00001010 

shl dl,2 ; after: 00101000
```

# SHR INSTRUCTION

**SHR Instruction** performs a logical right shift on the destination operand, replacing the highest bit with a 0.

• The lowest bit is copied into the Carry flag.



```
mov al,0D0h ; AL = 11010000b ; AL = 01101000b, CF = 0 mov al,00000010b ; AL = 00000000b, CF = 1
```

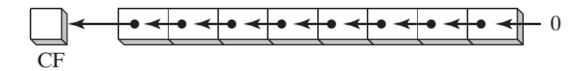
- •Bitwise division is accomplished when you shift a number's bits in a rightward direction (toward the LSB).
  - Shifting an unsigned integer right by n bits divides the operand by  $2^n$ . In the following statements, we divide 32 by  $2^1$ , producing 16:

```
mov dl,32 Before: 0010000 = 32
shr dl,1 After: 0001000 = 16
```

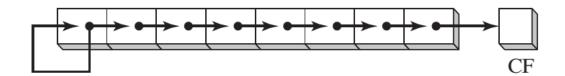
```
mov al,01000000b ; AL = 64 shr al,3 ; divide by 8, AL = 00001000b
```

# SAL AND SAR INSTRUCTION

•The **SAL** (**shift arithmetic left**) Instruction works the same as the SHL instruction.



•The **SAR** (shift arithmetic right) instruction performs a right arithmetic shift on its destination operand:



•The operands for SAL and SAR are identical to those for SHL and SHR.

```
mov al,0F0h ; AL = 11110000b (-16) 

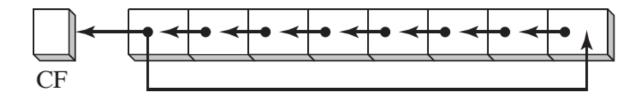
sar al,1 ; AL = 11111000b (-8), CF = 0
```

You can divide a signed operand by a power of 2

```
mov dl,-128 ; DL = 10000000b ; DL = 11110000b (-16)
```

### ROL INSTRUCTION

- \*Bitwise rotation occurs when you move the bits in a circular fashion.
- •The **ROL** (rotate left) instruction shifts each bit to the left. The highest bit is copied into the Carry flag and the lowest bit position.



```
mov al, 40h ; AL = 01000000b 

rol al,1 ; AL = 10000000b, CF = 0 

rol al,1 ; AL = 00000001b, CF = 1 

rol al,1 ; AL = 00000010b, CF = 0
```

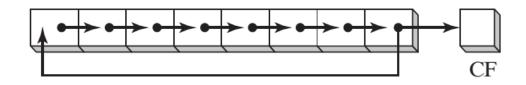
•When using a rotation count greater than 1, the Carry flag contains the last bit rotated out of the MSB position

```
mov al,00100000b

rol al,3 ; CF = 1, AL = 00000001b
```

#### ROR INSTRUCTION

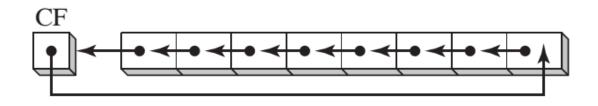
**ROR Instruction** shifts each bit to the right and copies the lowest bit into the Carry flag and the highest bit position (MSB).



```
mov al,01h ; AL = 00000001b ; AL = 10000000b, CF = 1 ror al,1 ; AL = 01000000b, CF = 0
```

#### RCL AND RCR INSTRUCTIONS

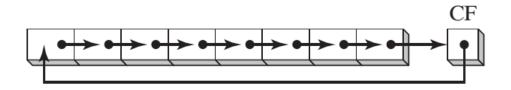
•The **RCL** (**rotate carry left**) instruction shifts each bit to the left, copies the Carry flag to the LSB, and copies the MSB into the Carry flag.



```
mov bl,88h
rcl bl,1
rcl bl,1
```

```
; CF = 0
; CF,BL = 0 10001000b
; CF,BL = 1 00010000b
; CF,BL = 0 00100001b
```

**RCR Instruction:** The RCR (rotate carry right) instruction shifts each bit to the right, copies the Carry flag into the MSB, and copies the LSB into the Carry flag:

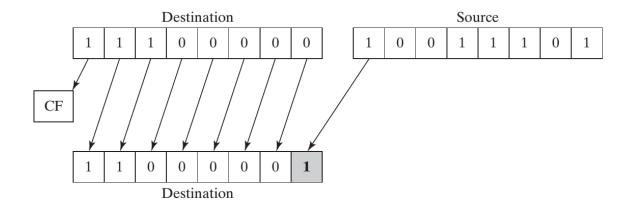


```
mov ah, 10h
rcr ah, 1
```

## SHLD AND SHRD INSTRUCTIONS

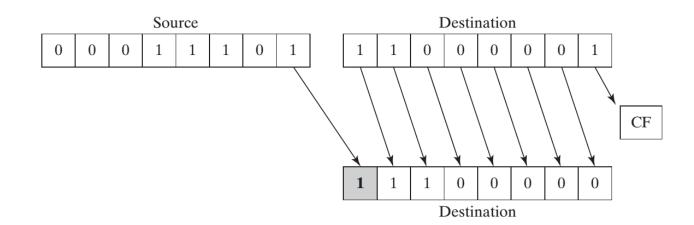
- •The **SHLD** (shift left double) instruction shifts a destination operand a given number of bits to the left.
- •The bit positions opened up by the shift are filled by the most significant bits of the source operand.

SHLD dest, source, count



- •The **SHRD** (shift right double) instruction shifts a destination operand a given number of bits to the right.
- •The bit positions opened up by the shift are filled by the least significant bits of the source operand:

SHRD dest, source, count



- •The source operand is not affected, but the Sign, Zero, Auxiliary, Parity, and Carry flags are affected.
- •The following instruction formats apply to both SHLD and SHRD:

SHLD reg16, reg16, CL/imm8

SHLD mem16, reg16, CL/imm8

SHLD reg32, reg32, CL/imm8

SHLD mem32, reg32, CL/imm8

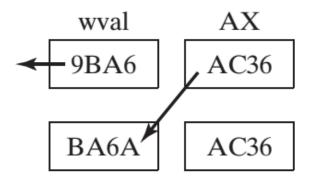
.data

wval WORD 9BA6h

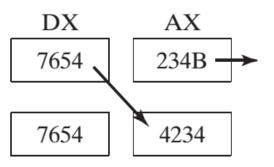
.code

mov ax,0AC36h
shld wval,ax,4

; wval = BA6Ah



mov ax,234Bh mov dx,7654h shrd ax,dx,4



# 7.3 MULTIPLICATION AND DIVISION INSTRUCTIONS

- In 32-bit mode, integer multiplication can be performed as a 32-bit, 16-bit, or 8-bit operation.
- •The process of multiplication and division is different for signed and unsigned numbers, so there are different Instructions for signed and unsigned multiplication and division.
  - The MUL and IMUL instructions perform unsigned and signed integer multiplication, respectively.
  - The DIV instruction performs unsigned integer division, and IDIV performs signed integer division

#### Signed Vs Unsigned Multiplication

Suppose we want to multiply the eight-bit numbers 1000000 and 11111111.

•Interpreted as unsigned numbers, they represent 128 and 255; respectively. The product is 32,640.

•However, taken as signed numbers, they represent-128 and -1, respectively; and the product is 128.

•Thus signed and unsigned numbers must be treated differently.

### MUL INSTRUCTION

- •In 32-bit mode, the **MUL** (unsigned multiply) instruction comes in three versions:
- 1. The first version multiplies an 8-bit operand by the AL register.
- 2. The second version multiplies a 16-bit operand by the AX register
- 3. Third version multiplies a 32-bit operand by the EAX register.
- •The multiplier and multiplicand must always be the same size, and the product is twice their size.

```
MUL reg/mem8 ; byte form

MUL reg/mem16 ; word form

MUL reg/mem32 ; DWORD form
```

| Multiplicand | Multiplier | Product |
|--------------|------------|---------|
| AL           | reg/mem8   | AX      |
| AX           | reg/mem16  | DX:AX   |
| EAX          | reg/mem32  | EDX:EAX |

- •When AX is multiplied by a 16-bit operand, for example, the product is stored in the combined DX and AX registers.
  - the high 16 bits of the product are stored in DX, and the low 16 bits are stored in AX.
- •The Carry flag is set if DX is not equal to zero, which lets us know that the product will not fit into the lower half of the implied destination operand.
- •After MUL, CF/OF=0; if upper half of the result is zero; 1 otherwise.

# IMUL INSTRUCTION

- •The IMUL (signed multiply) instruction performs signed integer multiplication.
- •Unlike the MUL instruction, IMUL preserves the sign of the product.

- •It does this by sign extending the highest bit of the lower half of the product into the upper bits of the product.
- •The x86 instruction set supports three formats for the IMUL instruction: one operand, two operands, and three operands.

# SINGLE OPERAND IMUL

•The one-operand formats store the product in AX, DX:AX, or EDX : EAX

```
IMUL reg/mem8 ; AX = AL * reg/mem8

IMUL reg/mem16 ; DX:AX = AX * reg/mem16

IMUL reg/mem32 ; EDX:EAX = EAX * reg/mem32
```

## TWO OPERAND IMUL

**Two-Operand Formats (32-Bit Mode):** stores the product in the first operand, which must be a register. The second operand (the multiplier) can be a register, a memory operand, or an immediate value:

```
IMUL reg16, reg/mem16
IMUL reg16, imm8
IMUL reg16, imm16
IMUL reg32, reg/mem32
IMUL reg32, imm8
IMUL reg32, imm8
```

The two-operand formats truncate the product to the length of the destination. If significant digits are lost, the Overflow and Carry flags are set.

## THREE OPERAND IMUL

•The three-operand formats in 32-bit mode store the product in the first operand. The second operand can be a 16-bit register or memory operand, which is multiplied by the third operand, an 8- or 16-bit immediate value:

```
IMUL reg16, reg/mem16, imm8
IMUL reg16, reg/mem16, imm16
IMUL reg32, reg/mem32, imm8
IMUL reg32, reg/mem32, imm32
```

- •After IMUL, CF/OF = 0, if the upper half of the result is the **sign extension** of the lower half; CF/OF = 1 otherwise
  - This means that the bits of the upper half are the same as the sign bit of the lower half.

• The following instructions multiply 48 by 4, producing +192 in DX:AX. DX is a sign extension of AX, so the Overflow flag is clear:

```
mov ax,48 mov bx,4 imul bx ; DX:AX = 000000C0h, OF = 0
```

# **DIV INSTRUCTION**

•In 32-bit mode, the DIV (unsigned divide) instruction performs 8-bit, 16-bit, and 32-bit unsigned integer division.

DIV reg/mem8

DIV reg/mem16

DIV reg/mem32

- •Where the single reg/mem operand is divisor.
- •When division is performed, we obtain two results, the **quotient** and the **remainder**.
  - Quotient and remainder have the same size as the divisor.

| Dividend | Divisor   | Quotient | Remainder |
|----------|-----------|----------|-----------|
| AX       | reg/mem8  | AL       | АН        |
| DX:AX    | reg/mem16 | AX       | DX        |
| EDX:EAX  | reg/mem32 | EAX      | EDX       |

mov ax,0083h

mov bl,2

div bl

; dividend

; divisor

; AL = 41h, AH = 01h

Quotient Remainder

•In word (16-bit) division, the dividend is in **DX:AX** even if the actual dividend will fit in AX. In this case DX should be cleared:

Quotient Remainder

## SIGNED INTEGER DIVISION

- •Signed integer division is nearly identical to unsigned division, with one important difference: The dividend must be **sign-extended** before the division takes place.
  - Sign extension is the term used for copying the highest bit of a number into all of the upper bits of its enclosing variable or register.

#### Sign Extension Instructions (CBW, CWD, CDQ)

- •The CBW instruction (convert byte to word) extends the sign bit of AL into AH.
- •The CWD (convert word to doubleword) instruction extends the sign bit of AX into DX.
- •The CDQ (convert doubleword to quadword) instruction extends the sign bit of EAX into EDX.

# IDIV INSTRUCTION

•The IDIV (signed divide) instruction performs signed integer division, using the same operands as DIV.

•Before executing 8-bit division, the dividend (AX) must be completely sign-extended.

.data

byteVal SBYTE -48

.code

mov al, byteVal

cbw

mov bl, +5

idiv bl

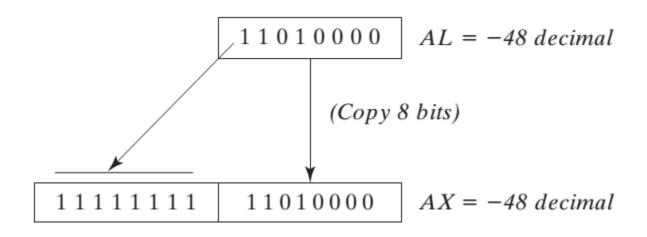
; D0 hexadecimal

; lower half of dividend

; extend AL into AH

; divisor

; AL = -9, AH = -3



### WHY SIGN EXTENSION IS NECESSARY

## 7.4 EXTENDED ADDITION AND SUBTRACTION

#### **ADC** Instruction

- •The ADC (add with carry) instruction adds both a source operand and the contents of the Carry flag to a destination operand.
- •The instruction formats are the same as for the ADD instruction, and the operands must be the same size:

```
ADC reg, reg
```

ADC mem, reg

ADC reg, mem

ADC mem, imm

ADC reg, imm

mov dl,0

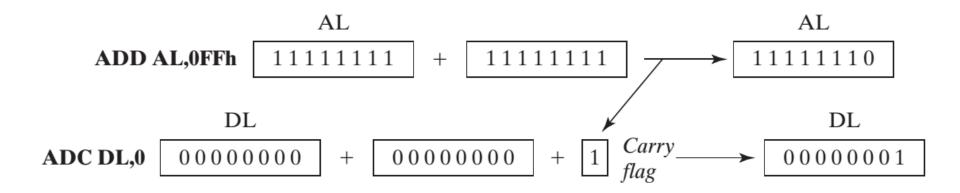
mov al, 0FFh

add al, 0FFh

adc dl,0

; AL = FEh

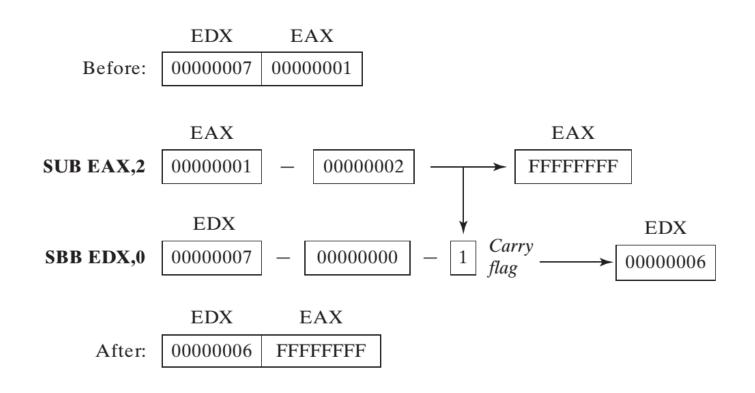
; DL/AL = 01FEh



# SBB INSTRUCTION

- •The SBB (subtract with borrow) instruction subtracts both a source operand and the value of the Carry flag from a destination operand
- •The possible operands are the same as for the ADC instruction

mov edx,7 ; upper half
mov eax,1 ; lower half
sub eax,2 ; subtract 2
sbb edx,0 ; subtract upper half



#### SUMMARY

- Shift and Rotate Instructions
  - SHL, SHR, SAL, SAR, ROL, ROR, RCL, RCR, SHLD, SHRD

- Multiplication and Division Instructions
  - MUL
  - IMUL
  - DIV
  - IDIV
- Sign Extension Instructions (CBW, CWD, CDQ)
- •ADC, SBB