1) Was the advertising campaign effective? Did additional consumers convert as a result of the ad campaign? Use an appropriate statistical test to support your conclusion. (5 points)

The p-value is less than .05. We can conclude that the campaign had a significant impact on conversion rates.

2) What is the minimum sample size of the control group (test=0) required to have a power of 0.8? Is the statistical test performed in the above question well powered? (5 points)

```
Difference of proportion power calculation for binomial distribution (arcsine transformation) h = 0.05300255 n = 5587.828 sig.level = 0.05 power = 0.8 alternative = two.sided
```

## The minimum sample size required is 5588.

•	test <sup>‡</sup>	sample_size
1	0	23524
2	1	564577

The test is well powered, as the sample sizes exceed the minimum sample size.

3) Based on the total impressions (tot\_impr) the customers received, the randomization done in the above A/B test is valid. Justify the statement using an appropriate test. (5 points)

```
Welch Two Sample t-test
data: test_group$tot_impr and control_group$tot_impr
t = 0.218, df = 25608, p-value = 0.8274
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
                                                                      test `mean(tot_impr)`
-0.4972735 0.6217286
                                                                     <int> <dbl>
sample estimates:
                                                                   1
                                                                        0
                                                                                        24.8
mean of x mean of y
                                                                   2
                                                                         1
                                                                                        24.8
24.82337 24.76114
```

I used a two sample t test to check the randomization. The p-value was .8, indicating that the randomization is valid and there is not a difference in mean total impressions among the groups. Additionally, the mean tot impr was the same for both groups.

4) How much more money did AdVert make by running the campaign (excluding advertising costs)? (5 points)

\$180957.50. This was calculated by applying both conversion rates to the entire population, subtracting those from test 0 from test 1 to account for users who would have converted regardless of the ad. Then, I multiplied by 40\$.

5) What was the cost of the ad campaign? (5 points)

## \$131374.64. This is total impressions \* 9\$ per 1000 impressions

- 6) Calculate the Return on Investment (ROI) of the campaign. Was the campaign profitable? (5 points)
- 32.23%. Yes, the campaign was profitable as ROI is positive.
- 7) What was the opportunity cost of including a control group, i.e., how much more could have AdVert made by not having a control group at all? (5 point)

\$7238.291. This was calculated by applying the conversion rate from test 1 to the control group, then subtracting the converts and multiplying by 40.

8) What is the naïve Average Treatment Effect (ATE) of medication on side effects (ignore Age<18 column)? (5 points)

## 0.5041

9) What is the marginal causal effect of medication on side effects, considering the Age<18 attribute as well? Use the standardized mean (weighted average) technique or the mean potential outcome (E[Y] = E[Y1] - E[Y0]) framework to answer this question. (10 points) **0.3022789**