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Examiner

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PRACTICAL NO. 1

Aim: Basics of R-software

- 1) R is a software for statistical analysis and data computing.
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display.
- 4) It is a free software.

Q.1 Solve the following:

$$\begin{aligned} 1) & 4+6+8 \div 2 - 5 \\ & > 4+6+8/2-5 \\ & [1] 9 \end{aligned}$$

$$\begin{aligned} 2) & 2^2 + 1 - 3 + \sqrt{45} \\ & > 2^2 + \text{abs}(-3) + \sqrt{45} \\ & [1] 13.7082 \end{aligned}$$

$$\begin{aligned} 3) & 5^3 + 7 \times 5 \times 8 + 4 \sqrt{5} \\ & > 5^3 + 7 * 5 * 8 + 46/5 \\ & [1] 417.2 \end{aligned}$$

4) $\sqrt{4^2 + 5 \times 3 + 71^2}$
 $> \text{sqrt}(4^2 + 5 * 3 + 71^2)$
 $[1] 5.671567$

5) round off $46 \div 7 + 9 \times 8$
 $> \text{round}(46 / 7 + 9 * 8)$
 $[1] 79$

Q.2

a) $> c(2, 3, 5, 7) * 2$
 $[1] 461014$

b) $> c(2, 3, 5, 7) * c(2, 3)$
 $[1] 4 \ 9 \ 10 \ 21$

c) $> c(2, 3, 5, 7) * c(2, 3, 6, 2)$
 $[1] 4 \ 9 \ 30 \ 14$

d) $> c(1, 4, 2, 3) * c(-2, -3, -4, -1)$
 $[1] -2 \ -18 \ -8 \ -3$

e) $> c(2, 3, 5, 7)^{1/2}$
 $[1] 4 \ 9 \ 25 \ 49$

f) $> c(4, 6, 8, 9, 4, 5)^{1/4} c(1, 2, 3)$
 $[1] 4 \ 36 \ 512 \ 9 \ 16 \ 125$

g) $> c(6, 2, 7, 5) / c(4, 5)$
 $[1] 1.50 \ 0.40 \ 1.75 \ 1.00$

Q.3 $> x = 20 \quad > y = 30 \quad > z = 2$

$> x^2 + y^3 + z$
 $[1] 2240$

$> \text{sqrt}(x^2 + y)$
 $[1] 20.73647$

$> x^z + y^z$
 $[1] 1300$

Q. 4) $x < -\text{matrix}(\text{nrow} = 4, \text{ncol} = 2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

x
 $\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}$

04

Q. 5) Find $x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 3 \\ 9 & -5 & 3 \end{bmatrix}$

$y = \begin{bmatrix} 10 & -5 & 1 \\ 12 & -4 & 9 \\ 15 & -6 & 3 \end{bmatrix}$

$x < -\text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(4, 7, 9, -2, 8, -5, 6, 2, 3))$

x
 $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

$\begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 3 \\ 9 & 5 & 3 \end{bmatrix}$

$-1 < -\text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(10, 12, 15, -5, -4, -6, 7, 9, 5))$

-1
 $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

$\begin{bmatrix} 10 & -5 & 1 \\ 12 & -4 & 9 \\ 15 & 6 & 5 \end{bmatrix}$

$x+y$
 $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

$\begin{bmatrix} 19 & -7 & 13 \\ 19 & -4 & 16 \\ 24 & -4 & 9 \end{bmatrix}$

> $2*x + 3*y$

10

[1] [2] [3]

| | | | |
|-----|----|-----|----|
| [1] | 38 | -19 | 33 |
| [2] | 50 | -12 | 41 |
| [3] | 43 | -28 | 21 |

Q.6 Marks of statistics of CS Batch A

x = c(58, 20, 35, 24, 44, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 52, 34, 29, 35, 39)

> x = c(data)

> breaks = seq(20, 60, 5)

> a = cut(x, breaks, right = FALSE)

> b = table(a)

> c = transform(b)

> c

| | a | freq |
|---|----------|------|
| 1 | [20, 25) | 3 |
| 2 | [25, 30) | 2 |
| 3 | [30, 35) | 1 |
| 4 | [35, 40) | 4 |
| 5 | [40, 45) | 1 |
| 6 | [45, 50) | 3 |
| 7 | [50, 55) | 2 |
| 8 | [55, 60) | 5 |

Practical No. 02.

Topic : Probability distribution.

i) Check whether the following are p.m.f. or not

| n | $p(n)$ |
|-----|--------|
| 0 | 0.1 |
| 1 | 0.2 |
| 2 | -0.5 |
| 3 | 0.4 |
| 4 | 0.3 |
| 5 | 0.5 |

ii) If the given data is p.m.f. Then :

$$\sum p(n) =$$

$$\begin{aligned} & \therefore p(0) + p(1) + p(2) + p(3) + p(4) + p(5) = p(n) \\ & = 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ & = 1.0 \end{aligned}$$

$\therefore p(2) = -0.5$, it can't be a probability mass function

$$\therefore p(n) \geq 0 \quad \forall n$$

| n | 1 | 2 | 3 | 4 | 5 |
|--------|-----|-----|-----|-----|-----|
| $p(x)$ | 0.2 | 0.2 | 0.3 | 0.1 | 0.2 |

The condition for p.m.f is $\sum p(n) = 1$

$$\begin{aligned}\sum p(x) &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.1 \\ &= 1.1\end{aligned}$$

∴ The given data is not a pmf because
 $p(x) \neq 1$

3)

| | | | | | |
|--------|-----|-----|------|------|-----|
| x | 10 | 20 | 30 | 40 | 50 |
| $p(x)$ | 0.2 | 0.2 | 0.35 | 0.15 | 0.1 |

The condition for p.m.f is

- 1) $p(x) \geq 0$ *it satisfies*
- 2) $\sum p(x) = 1$

$$\begin{aligned}\sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1\end{aligned}$$

∴ The given data is p.m.t.

Code

> prob = c(0.2, 0.1, 0.35, 0.15, 0.1)
> sum(prob)

06

Q.2 Find the c.d.f. for the following p.m.f. 8
sketch the graph.

| | | | | | |
|------|-----|-----|------|------|-----|
| x | 10 | 20 | 30 | 40 | 50 |
| p(x) | 0.2 | 0.2 | 0.35 | 0.15 | 0.1 |

$$\begin{aligned}F(x) &= 0 & x < 10 \\&= 0.2 & 10 \leq x < 20 \\&= 0.4 & 20 \leq x < 30 \\&= 0.75 & 30 \leq x < 40 \\&= 0.90 & 40 \leq x < 50 \\&= 1.0 & x \geq 50\end{aligned}$$



Q.3 Find

| | | | | | | |
|------|------|------|-----|-----|-----|-----|
| X | 1 | 2 | 3 | 4 | 5 | 6 |
| P(X) | 0.15 | 0.25 | 0.1 | 0.2 | 0.2 | 0.1 |

$$F(x) = 0 \quad n < 1$$
$$= 0.15 \quad 1 \leq n < 2$$
$$= 0.40 \quad 2 \leq n < 3$$
$$= 0.55 \quad 3 \leq n < 4$$
$$= 0.70 \quad 4 \leq n < 5$$
$$= 0.90 \quad 5 \leq n < 6$$
$$= 1.00 \quad n \geq 6$$

> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(prob)

→ [1] 1

> cumsum(prob)

[1] 0.15, 0.40, 0.55, 0.70, 0.90, 1.00

> x = c(1, 2, 3, 4, 5, 6)

> plot(x, cumsum(prob), "s", xlab = "Value",
ylab = "Cumulative probability",
main = "CDF graph", col = "brown")

Q.7 Check that whether the following is p.d.f or not.

$$\text{i) } f(n) = 3 - 2n, \quad 0 \leq n \leq 1$$

$$f(n) = 3n^2, \quad 0 < n < 1$$

$$\begin{aligned} f(n) &= 3 - 2n \\ &= \int_0^1 f(n) \\ &= \int (3 - 2n) dn \\ &= \left[3n - \frac{2n^2}{2} \right]_0^1 \end{aligned}$$

$$= 3 - 1$$

$$= 2 \neq 1$$

∴ It is not a p.d.f

$$\cancel{\int f(n) \neq 1}$$

ii)

$$f(n) = 3n^2$$

$$\int_0^1 3n^2 \, dn$$

$$= \left[\frac{3n^3}{3} \right]_0^1$$

$$= 1$$

The $\int_0^1 f(n) \, dn = 1$, it is a pdf.

Q



PRACTICAL AB. 3

08

Topic : Binomial

$$\text{# } P(X=x) = \text{dbinom}(n, n, p)$$

$$\text{# } P(X \leq n) = \text{pbinom}(n, n, p)$$

$$\text{# } P(X > n) = 1 - \text{pbinom}(n, n, p)$$

If n is unknown

$$P_r = P(X \leq n) = \text{qbinom}(P_r, n, p)$$

i) Find the probability of exactly 10 success in hundred trials with $p=0.1$

ii) Suppose there are 12 mcq, each question has 5 options out of which 1 is correct.

iii) Find the probability of having exactly 4 correct answers.

iv) Atmost 4 correct answers.

v) More than 5 correct answers.

vi) Find the complete distribution when $n=10$ and $p=0.1$

vii) $n=12, p=0.25$, find the following probabilities

$$\text{i) } P(X=5) \quad \text{iii) } P(X>7)$$

$$\text{ii) } P(X \leq 5) \quad \text{iv) } P(5 < X < 7)$$

80
1) $>x = dbinom(10, 120, 0.1)$

$>x$
[1] 0.1318653

2) i) $>x = dbinom(4, 12, 0.4)$

$>x$
[1] 0.1328758

ii) $>x = pbisnom(4, 12, 0.4)$

$>x$
[1] 0.92234445

iii) $1 - pbisnom(5, 12, 0.4)$

[1] 0.01940528

4) $x = dbinom(0:5, 5, 0.1)$

0 = 0.59049

1 = 0.32705

2 = 0.07280

3 = 0.00810

4 = 0.00045

5 = 0.00000

5) 1) $dbinom(5, 12, 0.25)$

[1] 0.1032417

2) $pbisnom(5, 12, 0.25)$

[1] 0.9458918

3) $1 - pbisnom(7, 12, 0.25)$

[1] 0.00238157

a) $dbinom(6, 12, 0.25)$

[1] 0.04014945

b) $> dbinom(0, 10, 0.15)$

[1] 0.1968747

$> 1 - pbisnom(2, 20, 0.15)$

[1] 0.3522718

c) $qbinom(0.88, 30, 0.2)$

[1] 9

d) $> n = 10$

$> p = 0.3$

$> x = 0:n$

$> prob = dbinom(x, n, p)$

$> compprob = pbisnom(x, n, p)$

$> d = data.frame("x values" = x, "probability" = prob)$

$> print(d)$

eo

| | X values | probability |
|----|----------|-------------|
| 1 | 0 | 0.0282 |
| 2 | 1 | 0.1210 |
| 3 | 2 | 0.2334 |
| 4 | 3 | 0.2668 |
| 5 | 4 | 0.2001 |
| 6 | 5 | 0.1029 |
| 7 | 6 | 0.0367 |
| 8 | 7 | 0.0090 |
| 9 | 8 | 0.0014 |
| 10 | 9 | 0.0001 |
| 11 | 10 | 0.0000 |

Q) The probability of a salesman making a sale to a customer is 0.15. Find the probability

- i) No sales out of 10 customers
ii) More than 3 sales

8

Practical No. : 4

Ques: Normal Distribution.

i) $P(z=x)$, domain (z, μ, σ)

ii) $P(x \leq z)$, $p_{\text{norm}}(\mu, \sigma)$

iii) $P(x > z) = 1 - p_{\text{norm}}(\mu, \sigma)$

iv) To generate random number from a normal distribution (n random number) the R code is $p_{\text{norm}}(m, \mu, \sigma)$

- Q.1 A random variable x follows normal distribution with mean, $\mu = 12$ & $\sigma = 3$. Find i) $P(x \leq 15)$
 ii) $P(10 \leq x \leq 13)$ iii) $P(x > 14)$
 iv) Generate 5 observation (random number)

Code:

```
> p1 = pnorm(15, 12, 3)
> p1
[1] 0.8413447
> cat("P(x <= 15) = ", p1)
P(x <= 15) = 0.8413447
> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)
> p2
[1] 0.3780611
> cat("P(10 < x <= 13) = ", p2)
P(10 < x <= 13) = 0.3780611
> p3 = 1 - pnorm(14, 12, 3)
```

```

> p3
[1] 0.2524905
> cat ("P(x > 14) = ", "P3")
[1] P(x > 14) = 0.2524905
> p4 = rnorm(5, 12, 3)
> p4
[1] 15.284728 16.548505 11.280515 6.419849
[4] 12.272460

```

- 2) x follows normal distribution with $\mu=10$, $\sigma=2$
- find i) $P(x \leq 7)$ ii) $15 < x < 12$ iii) $P(x > 14)$
- iv) generate 10 observations v) find k such that $P[x < k] = 0.4$

Code :

```

> a1 = pnorm(7, 10, 2)
> a1
[1] 0.668072
> a2 = pnorm(5, 10, 2) - pnorm(12, 10, 2)
> a2
[1] 0.835135
> a3 = 1 - pnorm(12, 10, 2)
> a3
[1] 0.164864
> a4 = rnorm(10, 10, 2)
> a4
[1] 12.345678 10.987654 13.123456 8.765432 11.234567
[6] 9.876543 14.567890 10.123456 11.987654 13.234567

```

```
[1] 11.600931 9.120417 12.637741 8.073359  
[1] 8.72180 9.193721 9.366824 11.907104 12  
[1] 9.537584 10.715006
```

> $a_5 = \text{qnorm}(0.4, 10, y)$

> a_5

```
[1] 9.95330
```

Q.3 Generate 5 random no. from a normal distribution $\mu=15$, $\sigma=4$ find sample mean, median, s.d. & point it.

Code :

```
> rnorm(5, 15, y)
```

```
[1] 10.7649 7.393249  
[1] 12.50968
```

9.953444

13.345307

> am = mean(x)

am

```
[1] 11.87345
```

> cat("sample mean is = ", am)
sample mean is = 11.87345

> me = median(x)

> me

```
[1] 10.76499
```

> cat("Median is = ", me)
median is = 10.76499

> n = 5

> v = (n - 1) * var(t) / n

> v

```
[1] 11.09965
```

> sd = sqrt(v)

> SD

```
[1] 3.33163
```

```

> cat ("SD is = ", SD)
SD is = 3.33163
Q.4  $x \sim N(30, 10)$ ,  $\sigma = 10$ 
1)  $P(x \leq 40)$ 
2)  $P(x \geq 35)$ 
3)  $P(25 < x < 35)$ 
4) Find  $k$  such that  $P(x < k) = 0.6$ 
> F1 = pnorm(40, 30, 10)
> F1
[1] 0.8413447
> F2 = 1 - pnorm(35, 30, 10)
> F2
[1] 0.3085325
> F3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)
> F3
[1] 0.3085325
> F4 = qnorm(0.6, 30, 10)
f4
[1] 32.53347
Q.5 Plot the standard normal graph
> x = seq(-3, 3, by = 0.1)
> y = dnorm(x)
> plot(x, y, xlab = "xvalues", ylab = "probability",
       main = "standard normal graph")

```

Practical: 5

Topic: Normal & t-test

$$i) H_0: \mu = 15 \quad H_1: \mu \neq 15$$

↳ null ↳ alternative

Test the hypothesis:

Random sample of size 400 is drawn and it is calculated. The sample mean is 14 and S.D. is 3. Test the hypothesis at 5% level of significance.

$\not\models 0.05 >$ accept the z-value

$\models 0.05 <$ less than reject.

$> m_0 = 15$

$> m_x = 14$

$> s_d = 3$

$> n = 400$

$> z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$

$> z_{cal}$

[1] -6.6667

$> cat("calculated value of z is ", z_{cal})$

calculated value of z is -6.6667

$> pvalue = 2 * (1 - pnorm(abs(z_{cal})))$

$> pvalue$

[1] 2.61679e-11

\therefore The value is less than 0.05 we will reject the value of $H_0: \mu = 15$.

2) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$.
 A random sample size of 400 is drawn
 with sample mean = 10.2 & S.D. = 2.25.
 Test the hypothesis at

$$> m_0 = 10$$

$$> n = 400$$

$$> m_x = 10.2$$

$$> s_d = 2.25$$

$$> z_{\text{cal}} = (m_x - m_0) / (s_d / (\sqrt{n}))$$

$$> z_{\text{cal}}$$

$$[1] 1.7778$$

$$> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p\text{value}$$

$$[1] 0.07544036$$

\therefore The value pvalue is greater than 0.05

\therefore The value is accepted.

3) Test the hypothesis $H_0: \text{proportion of smokers in college is } 0.2$. A sample is collected & calculated the sample proportion as 0.125. Test the hypothesis at 5% level of significance (sample size is 400)

$$> p = 0.2$$

$$> p = 0.125$$

$$> n = 400$$

$$> Q = 1 - p$$

$$> z_{\text{cal}} = (p - p) / (\sqrt{p * Q / n})$$

> cat("calculated value of 2 -g = ", zcal)

[1] calculated value of z is = -3.75

> pvalue = 2 * (1 - pnorm(abs(zcal)))

14

> pvalue

[1] 0.0001768346 (Reject)

4) Last year farmer's lost 20%. of their crops.
A random sample of 60 fields are collected.
And it is found that field crops are insect
polluted. Test the hypothesis at 1% level of
significance.

> p = 0.2

> p = 9 / 60

> n = 60

> zcal

[1] -0.9682458

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.3329216

∴ The value is 0.01. So value is accepted

5) Test the hypothesis $H_0: \mu = 12.5$ from the
following sample at 5% level of significance

> x = c(12.25, 11.97, 12.15, 12.08, 12.31, 11.94, 11.89,
12.11, 12.01)

> n = length(x)

> n

[1] 10

> mx = mean(x)

> mx

[1] 12.107

> variance = $(n-1) * \text{var}(x) / n$

> variance

[1] 0.019521

> sd = sqrt(variance)

> sd

[1] 0.1397174

> mo = 12.5

> t = $(mx - mo) / (sd / \sqrt{n})$

> t

[1] 8.894504

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(t)))$

> pvalue

[1] 0

∴ The value is less than 0.05 the
value is accepted.

Practical : 06

Ques: Large sample test.

- 1) Let the population mean (the amount spent per customer in a restaurant) is μ_0 .
A sample of 100 customers selected the sample mean is calculated as 275 & S.D. 30.
Test the hypothesis, that the population mean is 250 or not, on 5% level of significance.

```
> m0 = 250  
> mx = 275  
> sd = 30  
> n = 100  
> zcal = (mx - m0) / (sd / (sqrt(n)))  
> cat("Calculated values of z is ", zcal)  
[1] Calculated value of z is 8.33333  
> pvalue = 2 * (1 - pnorm(abs(zcal)))  
> pvalue  
[1] 0  
: The value is less than 0.05 we will reject the value of the  $H_0: \mu = 250$ 
```

In a random sample of 1000 students it is found that 750 use blue pen. test the hypothesis that the population proportion is 0.7 at 1% level of significance.

$$> p = 0.7$$

$$> q = 1 - p$$

$$> p = \frac{750}{1000}$$

$$> n = 1000$$

$$> z_{\text{cal}} = (p - p) / \sqrt{p * q / n}$$

> cat ("calculated value of Z is : ", zcal)

[1] calculated value of Z is : -3.952847

$$> pvalue = 2 * (1 - pnorm(abs(zcal[1])))$$

$$> pvalue$$

$$[1] 7.72267 - 0.5$$

The value is less than 0.01 we reject!

3) To random sample of size 1000 & 2000 are drawn from two population with same sd 2.5. The sample means are 67.5 & 68. Test the hypothesis $\mu_1 = \mu_2$ at 5% level of significance.

$$> n_1 = 1000$$

$$> n_2 = 2000$$

$$> mx_1 = 67.5$$

$$> mx_2 = 68$$

$$> sd_1 = 2.5$$

$$> sd_2 = 2.5$$

$$>z_{\text{cal}} = (m_{x_1} - m_{x_2}) / \sqrt{(s_{d_1}^2/n_1) + (s_{d_2}^2/n_2)}$$

$$>z_{\text{cal}}$$

$$[1] -5.163978$$

$$>p\text{value} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

$$>p\text{value}$$

$$[1] 2.41754e-07 \therefore (\text{Rejected})$$

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y) A study of noise level in 2 hospital is given below test the claim that 2 hospital have same level of noise at 1% level of significance.

Hos. A

87

61.2

7.9

Hos. B

84

59.4

7.5

$$>n_1 = 87$$

$$>n_2 = 34$$

$$>m_{x_1} = 61.2$$

$$>m_{x_2} = 59.4$$

$$>s_{d_1} = 7.9$$

$$>s_{d_2} = 7.5$$

$$>z_{\text{cal}} = (m_{x_1} - m_{x_2}) / \sqrt{(s_{d_1}^2/n_1) + (s_{d_2}^2/n_2)}$$

$$>z_{\text{cal}}$$

$$[1] 1.162828$$

$$>p\text{value}$$

$$[1] 0.245021$$

\because The value is greater than 0.01 we accept the value.

Q) In a sample of 600 students it is dg from a sample of 400 students that 31 used blue ink. In another sample of 500 students 450 use blue ink. Test the hypothesis that the preparation of students using blue ink in two colleges are equal or not at 1% level of significance

$$H_0: p_1 = p_2 \text{ against } H_1: p_1 \neq p_2$$

$$> n_1 = 600$$

$$> n_2 = 400$$

$$> p_1 = 400 / 600$$

$$> p_0 = 450 / 500$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

$$[1] 0.566062$$

$$> q = 1 - p$$

$$> q$$

$$[1] 0.4333$$

$$> z_{\text{cal}} = (p - p_0) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}}$$

$$[1] 6.381534$$

$$> p\text{ value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p\text{ value}$$

$$[1] 1.75322e-10$$

\therefore value is less than 0.01 the value is rejected.

g) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$
 > $n_1 = 200$
 > $n_2 = 200$
 > $p_1 = 44 / 200$
 > $p_2 = 30 / 200$
 > $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 > p
 [1] 0.185
 > $q = 1 - p$
 > q
 [1] 0.815
 > $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$
 > z_{cal}
 [1] 1.802741
 > $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 > $p\text{value}$
 [1] 0.0714288
 "Accept" greater than 0.05.

Topic: small sample test

Q.1 The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from a population with average marks "65".

$$\text{Soln: } H_0: \mu = 65$$

$$> x = [(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)]$$

> t-test(x)

one sample t-test

data: x

$$t = 6.8319, df = 9, p\text{-value} = 1.558e-13$$

alternative hypothesis: true mean is not equal to 65 percent confidence interval:

65.65171

sample

70.14829

estimates:

mean of n

67.9

since p-value is less than 0.05.

we reject hypothesis at 5%.

level of significance -

$$> \alpha = 0.05$$

$$> p\text{-value} = 1.558e-13$$

> if (pvalue > 0.05) { cat ("accept H₀") }
 else { cat ("reject H₀") }
 reject H₀

Q.2 Two groups of students score the following marks. test the hypothesis that there is no significant difference between the two groups.

group 1 = 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

group 2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21.

so H_0 : There is no difference between two groups.

> $x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

> $y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

> t.test(x, y)

which does sample t-test

data : x & y

t = 2.2513, df = 16.314, p-value = 0.03798

alternative hypothesis: true difference may
it is not equal to 0.

95 percent confidence interval:

0.128205

5.0371295

sample estimates:

mean of x mean of y:

20.1

17.5

> pvalue = 0.03798

> if(pvalue > 0.05) {cat("accept H₀")}

else {cat("reject H₀")}

reject H₀

since p-value is less than 0.05 we reject hypothesis at 5% level of significance.

Q.3 The sales data of 6 shops before & after a special campaign are given below:

Before : 53, 28, 31, 48, 50, 42

After : 57, 29, 30, 55, 52, 45

Test the hypothesis that the campaign is effective or not.

form: H_0 : There is no significant difference of sales before & after the campaign.

$> u = c(53, 28, 31, 48, 50, 42)$

$> y = c(57, 29, 30, 55, 52, 45)$

$> t.test(u, y, paired = T, alternative = "greater")$
paired t-test.

data: u & y

$t = -2.2815$, $df = 5$, $p\text{-value} = 0.9805$

alternative hypothesis: the difference in mean is greater than 0.

95 percent confidence interval

-6.035332 to

sample estimate:

mean of the difference

ef

PRACTICAL No.8
Large & small sample test

1) $H_0: \mu = 55$

$H_1: \mu \neq 55$

$>n = 10$

$>m_x = 52$

$>m_o = 55$

$>\sigma_d = 7$

$>z_{cal} = (m_x - m_o) / (\sigma_d / \sqrt{n})$

$>z_{cal}$

[1] -4.285714

>zcal ("calculated z value is" = "zcal")

calculated z value is = -4.285714

>pvalue = 2 * (1 - pnorm (abs (zcal)))

>pvalue

[1] 1.82153e-05

since pvalue is less than 0.05
we reject the hypothesis of 5%).
level of significance.

2) $H_0: \mu =$
 $\geq p = 0.5$
 $\geq q = 1 - p$
 $\geq p = 350 / 700$
 $\geq n = 700$
 $\geq z_{\text{cal}} = (p - p_0) / \sqrt{p * q / n}$
 $\geq z_{\text{cal}} (" \text{calculated } z\text{-value is } = ", z_{\text{cal}})$
 Calculated z -value is = 0.
 $\geq p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $\geq p\text{value}$
 $[1]$

Since $p\text{value}$ is greater than 0.05
 we so accept hypothesis at 1% level
 of significance.

3) $H_0: p_1 = p_2$ or $H_1: p_1 \neq p_2$
 $\geq n_1 = 1000$
 $\geq n_2 = 1500$
 $\geq p_1 = 0.02$
 $\geq p_2 = 0.01$
 $\geq p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 $\geq p$
 $[1] 0.014$
 $\geq q = 1 - p$
 $\geq q^2 0.98$

$$> z_{\text{cal}} = (p_1 - p_0) / \sqrt{p_0 q_0 (1/n_1 + 1/n_2)}$$

> z_{cal}

[1] 2.084842

> $z_{\text{abs}} / \text{"calculated } z \text{ value is } = ", z_{\text{cal}})$

Calculated z value is = 2.084842

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.03708369

Since pvalue is less than 0.05 we reject the hypothesis at 5% level of significance.

9) $H_0: \mu = 100$

> $m_x = 99$

> $m_0 = 100$

> $sd = 8$

> $n = 400$

> $z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$

> z_{cal}

[1] -2.5

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.01241933

Since pvalue is less than 0.05 we rejected the hypothesis at 5% level of significance.

$$H_0: \mu = 66$$

$$\rightarrow x = [63, 63, 68, 69, 71, 71, 74]$$

\rightarrow r-test (x)

one sample z-test

data 8x

$$f = 47.94, df = 6, p\text{-value} = 5.522e-09$$

alternative hypothesis : true mean is not equal to 0

95 percent confidence interval:

$$64.6479$$

$$71.42092$$

sample estimate :

mean of x

$$68.14281$$

since pvalue is less than 0.05
we reject the hypothesis at 1%
level of significance.

7) $H_0: \mu_S = 1200$
 > $m_s = 1200$
 > $m_x = 1150$
 > ~~n~~ $n = 100$
 > $s_d = 15$
 > $z_{\text{cal}} = (m_x - m_0) / (s_d / (\sqrt{n}))$
 > $\text{cat}["\text{calculated } z\text{ value is } = 11; z_{\text{cal}}]$
 calculated z value is $= -4$
 > $p\text{value} = 2 * (1 - \text{pnorm}(\text{obs}(z_{\text{cal}})))$
 [1] $6.334248e-05$

since $p\text{value}$ is less than 0.05 we
 reject hypothesis

8) $H_0: p_u = p_1 \neq p_2$
 > $n_1 = 200$
 > $n_2 = 300$
 > $p_1 = 44/200$
 > $p_2 = 38/300$
 > $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 > p

[1] 0.1

$$\geq q = 1 - p$$

$$\geq z_{\text{cal}} = \left(p_1 - p_2 \right) / \sqrt{p_1 p_2 \left(1/n_1 + 1/n_2 \right)}$$

$\geq z_{\text{cal}}$

[1] 0.9128709

$\geq z_{\text{cal}}$ ("calculated z-value is" , z_{cal})

calculated value is = 0.9128709

$\geq p\text{value} = 2 * \left(1 - \text{pnorm} \left(\text{abs} \left(z_{\text{cal}} \right) \right) \right)$

$\geq p\text{value}$

[1] 0.3613107

Since p value is greater than 0.05 we accept the hypothesis.

Practical No. 9

Topic: Chi-square Test & ANOVA

Q.1 Use the following data to test whether the condition of the home & contribution of child are independent or not.

| | Clean | dirty |
|--------------|-------|-------|
| Clean | 70 | 50 |
| fairly clean | 80 | 20 |
| dirty | 35 | 45 |

Sol: H_0 : Condition of home & child are independent

$$x = (70, 80, 35, 50, 20, 45)$$

$$M = 3$$

$$n = 2$$

$$y = \text{matrix}(x, nrow = m, xcol = n)$$

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

| | |
|----|----|
| 70 | 50 |
| 80 | 20 |
| 35 | 45 |

> $p < \text{chisq.test}(y)$

> $p <$

Pearson's Chi-squared test

24

data by

χ^2 -square 25.64, df = 2, p-value = 7.698

Pvalue is less than 0.05 we reject the hypothesis at 5% level of significance

Q.2 Test the hypothesis that the vaccination & disease are independent or not.

| Differ | Disease | Aff | | Not Aff. | |
|--------|----------|-----|----------|----------|----------|
| | | Aff | Not Aff. | Aff | Not Aff. |
| | Aff | 70 | 46 | 70 | 46 |
| | Not Aff. | 35 | 37 | 35 | 37 |
| N.A. | | | | | |

Sol: H_0 : Disease independent

of vaccination or

> $x = c(70, 35, 46, 37)$

> $m = 2$

> $n = 2$ ($m \times n = m \times n$)

> $y = \text{matrix}(x, mow = m, nrow = n)$

Q.2

$$\begin{bmatrix} 1, \\ 2, \end{bmatrix}$$

1, 11 1, 1
2 4
35 37

$$> p_v = \text{ch}^2_{\text{sq}} \cdot \text{f}_{\text{v}}(y)$$

> p_v

Pearson's ch² squared test
with Fisher continuity correction

data : y
 $x - \text{squared} = 2.0275$, $\text{df} = 1$, pvalue
 $= 0.01545$

\because Pvalue is more than 0.05 we
accept the hypothesis at 5% level of
significance

Q.3 Perform a ANOVA for the following
data

Type
A

Obs

50, 52

B

53, 55, 53

C

60, 58, 75, 52

D

52, 54, 54, 55

Sol: H₀: The means are equal for A, B, C, D

```

> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 58, 57, 56)
> x4 = stack(list(b1 = x1, b2 = x2, b3 = x3,
+                  b4 = x4))
> names(d)
[1] "values"   "ind"
> oneway.fst(values ~ ind, data = d,
+ var.equal = T)

```

One-way analysis of meay

data: values and ind

F = 11.735, num df = 3, denon df = 9
 pvalue = 0.00183

```

> anova = aov(values ~ ind, data = d)
> summary(anova)

```

since p-value is less than 0.05 we
reject the hypothesis at 5% level
of significance

Q.7 - The following data given the life of
tyres of your brand

Type Life

A - 20, 23, 18, 17, 18, 22, 24

B - 19, 15, 17, 20, 16, 17

C - 21, 19, 22, 17, 20

D - 15, 17, 16, 18, 17, 16

H₀: The average life of tyre is equal for (A, B, C; D)

```
> x1 = c(20, 23, 18, 17, 18, 22, 24)
> x2 = c(19, 15, 17, 20, 16, 17)
> x3 = c(21, 19, 22, 17, 20)
> x4 = c(15, 17, 16, 18, 17, 16)
> d = stack / list / b, = x1, b2 = x2, b3 = x3
   by = n1))
> named(d)
[1] "values" ";;;"
```

> oneway.test(values ~ ind, data = d,
var.equal = T)

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One-way analysis of variance

data: values and ind

F = 6.8445, num df = 3, denom df = 20,
p-value = 0.002349

Since pvalue is less than 0.05 we
reject the hypothesis at 5% level of
significance

PRACTICAL - 10

Q5. Topic : Non Parametric Test

Q.1 Following are the amounts of sulphur oxid emitted by a industry in 20 days. Apply sign test, to test the hypothesis that the population median is 21.5 at 5% level of significance.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 21, 14, 15, 23, 24, 21.

$$H_0: \text{median} = 21.5$$

Population median is 21.5

$$\text{Soln: } n = (17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 21, 14, 15, 23, 24, 21)$$

$$> m_e = 21.5$$

$$> s_p = \text{length}(x [x > m_e])$$

$$> s_n = \text{length}(x [x < m_e])$$

$$> n = s_p + s_n$$

$$> n$$

$$[1]^{20}$$

> $p_{\text{v}} = \text{pbiv}(\text{sp}, n, 0.05)$

> p_{v}
[1] 0.4119015

Since p-value is more than 0.05 we accept the hypothesis at 5% level of significance.

Q. L Following is a data obtained by observations apply sign test to the hypothesis that the population median is 625 against the alternative it is more than 625.

612, 619, 631, 628, 643, 640, 655, 649,
670, 623.

Sol: H₀: Rep Population median is 625

> $x = c(612, 619, 631, 628, 643, 640, 655, 649,$
 $670, 623)$

> $me = 625$

> $sp = \text{length}(x[x > me])$

> $sn = \text{length}(x[x < me])$

> $n = sp + sn$

> n

[1] 10

$$\begin{aligned} &> p_v = pbinc(s_n, n, 0.5) \\ &> p_v \\ &[1] 0.054875 \end{aligned}$$

since p-value is greater than 0.85
we accept the hypothesis at 5% level of significance.

Q.3 Following are value of a sample test the hypothesis that the population median is 60 against the alternative it is more than 60 at 5% level of significance using Wilcoxon signed rank test.

63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 71, 59, 48, 66, 71, 63, 87, 69.

Sol:- H_0 : population median = 60
 H_1 : population median > 60
 $> x = (f(63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 71, 59, 48, 66, 71, 63, 87, 69))$
 $> \text{wilcox-test}(x, \text{altv} = "greater", n = 60)$

wilcox signed Rank Test
with continuity correction.

28

data: x
 $\nu = 145$, p-value = 0.0298
alternative hypothesis: true location
is greater than 60.

Since p-value is less than 0.05 we reject the hypothesis at 5% level of significance.

Q.4 Using WS.R. test

population median is 12 or less than 12

15, 13, 24, 15, 20, 21, 32, 28, 12, 25, 24, 26.

Sol": H₀: population median is 12

H_a: population median $\neq 12$

$>x = c(15, 12, 24, 25, 20, 21, 32, 28, 12, 25)$

24, 26)

85
> wilcox.test(x, after = "test", mu = 12)
wilcoxon signed Rand Test
with continuity correction

data: x

n = 66, p-value = 0.996

alternative hypothesis: true location is less than 12.

Since pvalue is greater than 0.05 we accept the hypothesis at 5% level of significance.

Q.8. The weights of students before & after they stop smoking are given below. Using WSRT test check there is no significant change.

| Before | After |
|-----------------|-----------------|
| 61, 71, 75, 62, | 71, 74, 72, 60, |
| 72 | 73. |

for H_0 : Before & after there is no significant change

H_1 : There is a change -

> $x = c(65, 75, 75, 62, 72)$

> $y = c(71, 74, 72, 66, 73)$

> $d = x - y$

> wilcox.test(x, alter = "two.sided", mu = 0)

wilcox signed RANK Test with continuity correction

data = x

$n = 15$, p-value = 0.0579,

alternative hypothesis: true location
is not equal to 0.

Since pvalue is greater than 0.05
we accept the hypothesis at 5%
level of significance