

## **School of Computer Science and Engineering**

## **Department of Computer Science and Engineering**

Engineering Mathematics IV | MA2201| 3 Credits | 2 1 0 3

Session: January 2024– May 2024 | Faculty: Dr Alka Choudhary | Class: B.Tech. IV Sem

- **A. Introduction:** This course is offered by Dept. of Mathematics & Statistics as a regular course to make the students acquainted with the subject of probability and statistics at an early stage. Probability and statistics is an important foundation for computer science fields such as machine learning, artificial intelligence, computer graphics, randomized algorithms, image processing, and scientific simulations. In this course, students will expand their knowledge of probabilistic methods and apply them to diverse computational problems. The first part of the course offers in depth knowledge of probability theory (random event, probability, characteristics of random variables, probability distributions and moment generating functions) which is necessary for simulation of random processes. In the second part, sampling theory is discussed. Each concept is explained through various examples and application-oriented problems.
- **B.** Course Outcomes: At the end of the course, students will be able to
  - [2201.1] Apply the concept of probability and related theorems in solving various real-world problems.
  - [2201.2] Understand the key concept of random variable, its probability distributions including mean, expectation, variance and moments.
  - [2201.3] Implement the variation and the relation between two random variables by using the concept of correlation.
  - [2201.4] Comprehend the concept of random sample and its sampling distribution which will enhance the logical & analytical skills.
  - [2201.5] Apply the statistics for testing the significance of the given large and small sample data by using t-test, F-test and Chi-square test.

#### C. PROGRAM OUTCOMES AND PROGRAM SPECIFIC OUTCOMES

**PO1. Engineering knowledge:** Apply the knowledge of mathematics, computer science, and communication engineering fundamentals to the solution of complex engineering problems.

- **PO2. Problem analysis:** The sophisticated curriculum would enable a graduate to identify, formulate, review research literature, and analyse complex engineering problems reaching substantiated conclusions using basic principles of mathematics, computing techniques and communication engineering principles.
- **PO3.** Design/development of solutions: Upon analysing, the B Tech CSE graduate should be able to devise solutions for complex engineering problems and design system components or processes that meet the specified requirements with appropriate consideration for law, safety, cultural & societal obligations with environmental considerations.
- **PO4.** Conduct investigations of complex problems: To imbibe the inquisitive practices to have thrust for innovation and excellence that leads to use research-based knowledge and research methods including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions.
- **PO5. Modern tool usage:** Create, select, and apply appropriate techniques, resources, and modern engineering and IT tools including prediction and modelling to complex engineering activities with an understanding of the limitations.
- **PO6.** The engineer and society: The engineers are called society builders and transformers.

  B. Tech CSE graduate should be able to apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal and cultural issues, and the consequent responsibilities relevant to the professional engineering practice.
- **PO7.** Environment and sustainability: The zero effect and zero defect is not just a slogan, it is to be practised in each action. Thus, a B Tech CSE should understand the impact of the professional engineering solutions in societal and environmental contexts, and demonstrate the knowledge of, and need for sustainable development.
- **PO8.** Ethics: Protection of IPR, staying away from plagiarism are important. Student should be able to apply ethical principles and commit to professional ethics, responsibilities, and norms of the engineering practice.
- **PO9.** Individual and teamwork: United we grow, divided we fall is a culture at MUJ. Thus, an outgoing student should be able to function effectively as an individual, and as a member or leader in diverse teams, and in multidisciplinary settings.
- **PO10. Communication:** Communicate effectively for all engineering processes & activities with the peer engineering team, community and with society at large. Clarity of thoughts, being able to comprehend and formulate effective reports and design documentation, make effective presentations, and give and receive clear instructions.
- **PO11. Project management and finance:** Demonstrate knowledge and understanding of the engineering and management principles and apply these to one's own work, as a member and leader in a team, to manage projects and in varied environments.

**PO12.** Life-long learning: Recognize the need for and have the preparation and ability to engage in independent and life-long learning in the broadest context of technological change.

## **Program Specific Outcomes (PSOs)**

At the end of the B. Tech. CSE program, the student:

- **PSO1.** Imbibe the basic concepts and applications of computer-based Communication or networking, information sharing, signal processing, web-based systems, smart devices, and communication technology.
- **PSO2.** Investigate prominent areas in the field of Computer and Communication Engineering to provide feasible solutions.
- **PSO3.** Apply the contextual knowledge in the field of Computing and Communication to assess social, health, safety, and security issues relevant to the professional engineering practice.

### D. Assessment Plan:

| Criteria             | Description  | Maximum Marks          |  |  |  |  |  |  |  |  |
|----------------------|--|------------------------|--|--|--|--|--|--|--|--|
| Internal Assessment  | Sessional Exam   | 30                     |  |  |  |  |  |  |  |  |
| (Summative)          | CWS Marks based on Quizzes and                                   | 30                     |  |  |  |  |  |  |  |  |
|                      | Assignments.   |                        |  |  |  |  |  |  |  |  |
| End Term Exam        | End Term Exam  | 40                     |  |  |  |  |  |  |  |  |
| (Summative)          |  |                        |  |  |  |  |  |  |  |  |
|                      | Total  | 100                    |  |  |  |  |  |  |  |  |
| Attendance           | A minimum of 75% Attendance required                             | to be maintained by a  |  |  |  |  |  |  |  |  |
| (Formative)          | student to be qualified for taking up the End                    | Semester examination.  |  |  |  |  |  |  |  |  |
|                      | The allowance of 25% includes all type                           | es of leaves including |  |  |  |  |  |  |  |  |
|                      | medical leaves.  |                        |  |  |  |  |  |  |  |  |
| Homework/ Home       | Although these works are not graded with marks. However, a       |                        |  |  |  |  |  |  |  |  |
| Assignment/ Activity | student is expected to participate and perform these assignments |                        |  |  |  |  |  |  |  |  |
| Assignment           | with full zeal.  |                        |  |  |  |  |  |  |  |  |
| (Formative)          |  |                        |  |  |  |  |  |  |  |  |

#### E. SYLLABUS

Basic Set theory, Axioms of probability, Sample space, conditional probability, total probability theorem, Baye's theorem. One dimensional and two dimensional random variables, mean and variance, properties, Chebyschev's inequality, correlation coefficient, Distributions, Binomial, Poisson, Normal and Chisquare. Functions of random variables: One dimensional and Two dimensional, F & T distributions, Moment generating functions, Sampling theory, Central limit theorem, Point estimation, MLE, Interval estimation, Test of Hypothesis: significance level, certain best tests; Chi square test.

#### **References:**

- 1. P. L. Meyer, Introduction to probability and Statistical Applications, (2e), Oxford and IBH publishing, 1980.
- 2. Miller, Freund and Johnson, Probability and Statistics for Engineers, (8e), Prentice Hall of India, 2011.
- 3. Hogg and Craig, Introduction to mathematical statistics, (6e), Pearson Education, 2012.
- 4. Sheldon M Ross, Introduction to Probability and Statistics for Engineers and Scientists, Elsevier, 2010

## F. LECTURE PLAN

| Lecture | Topic                       | Session Outcome       | Mode of      | Corresponding | Mode of         |  |  |  |  |
|---------|-----------------------------|-----------------------|--------------|---------------|-----------------|--|--|--|--|
| Number  |                             |                       | Delivery     | CO            | Assessing CO    |  |  |  |  |
| 1       | Introduction of the Course  | Develop the           | Lecture,     | NA            | NA              |  |  |  |  |
|         |                             | understanding about   | Discussion & |               |                 |  |  |  |  |
|         |                             | the course            | Examples     |               |                 |  |  |  |  |
| 2       | Basic Set Theory            | Students will get the | Lecture,     | 2201.1        | Quiz, Sessional |  |  |  |  |
|         |                             | acquaintance with     | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | the basic concept of  | Examples     |               | Exam            |  |  |  |  |
| 2       |                             | Set Theory            | <b>.</b>     | 2201.1        | 0               |  |  |  |  |
| 3       | Axioms of Probability       | Learn about the basic | Lecture,     | 2201.1        | Quiz, Sessional |  |  |  |  |
|         |                             | concept of            | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | Probability           | Examples     |               | Exam            |  |  |  |  |
| 4       | Conditional Probability     | Understand the        | Lecture,     | 2201.1        | Quiz, Sessional |  |  |  |  |
|         |                             | Conditional           | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | Probability           | Examples     |               | Exam            |  |  |  |  |
| 5       | Total Probability Theorem   | Learn about Total     | Lecture,     | 2201.1        | Quiz, Sessional |  |  |  |  |
|         |                             | Probability Theorem   | Discussion & |               | & End Term      |  |  |  |  |
|         |                             |                       | Examples     |               | Exam            |  |  |  |  |
| 6       | Baye's Theorem              | Learn about Baye's    | Lecture,     | 2201.1        | Quiz, Sessional |  |  |  |  |
|         |                             | Theorem               | Discussion & |               | & End Term      |  |  |  |  |
|         |                             |                       | Examples     |               | Exam            |  |  |  |  |
| 7       | Tutorial-Problem Solving    | Apply the concepts    | Discussion & | 2201.1        | Quiz, Sessional |  |  |  |  |
|         | Session                     | in real world         | Examples     |               | & End Term      |  |  |  |  |
|         |                             | problems              | •            |               | Exam            |  |  |  |  |
| 8       | Random Variable: One        | Learn about Random    | Lecture,     | 2201.2        | Quiz, Sessional |  |  |  |  |
|         | Dimensional                 | Variable              | Discussion & |               | & End Term      |  |  |  |  |
|         |                             |                       | Examples     |               | Exam            |  |  |  |  |
| 9       | Classification: Discrete &  | Understand the        | Lecture,     | 2201.2        | Quiz, Sessional |  |  |  |  |
|         | Continuous Random           | classification of     | Discussion & |               | & End Term      |  |  |  |  |
|         | Variable                    | Random Variables      | Examples     |               | Exam            |  |  |  |  |
| 10      | Random variable: Two        | Elaborate the concept | Lecture,     | 2201.3        | Quiz, Sessional |  |  |  |  |
|         | Dimensional                 | of Random Variable    | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | in two dimensions     | Examples     |               | Exam            |  |  |  |  |
| 11      | Joint Distribution Function | Get the knowledge of  | Lecture,     | 2201.3        | Quiz, Sessional |  |  |  |  |
|         |                             | Joint Distribution    | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | Function              | Examples     |               | Exam            |  |  |  |  |
| 12      | Marginal Distribution &     | Get the knowledge of  | Lecture,     | 2201.3        | Quiz, Sessional |  |  |  |  |
|         | Conditional Distribution    | Marginal &            | Discussion & |               | & End Term      |  |  |  |  |
|         |                             | Conditional           | Examples     |               | Exam            |  |  |  |  |
|         |                             | Distributions         | 1            |               |                 |  |  |  |  |
| 13      | Mathematical Expectation    | Develop the notion    | Lecture,     | 2201.2        | Quiz, Sessional |  |  |  |  |
|         | and Variance                | of Mean & variance    | Discussion & |               | & End Term      |  |  |  |  |
|         |                             |                       | Examples     |               | Exam            |  |  |  |  |
| 14      | Moments & Moment            | Elaborate the concept | Lecture,     | 2201.2        | Quiz, Sessional |  |  |  |  |
|         | Generating Function         | of Mgf                | Discussion & |               | & End Term      |  |  |  |  |
|         | _                           | -                     | Examples     |               | Exam            |  |  |  |  |
| L       | l .                         | <u> </u>              | P.0          | J             |                 |  |  |  |  |

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|-------|---|---|--------------------------|--------|---------------------------------------|
| 15    | Tutorial-Problem Solving<br>Session                   | Apply the concepts in real world problems | Discussion & Examples    | 2201.2 | Quiz, Sessional<br>& End Term<br>Exam |
| 16    | Functions of Random<br>Variables                      | Develop the notion of Functions of        | Lecture,<br>Discussion & | 2201.3 | Quiz, Sessional<br>& End Term         |
|       |   | Random Variables                          | Examples                 |        | Exam                                  |
| 17    | Covariance  | Understand the                            | Lecture,                 | 2201.3 | Quiz, Sessional                       |
|       |   | concept of                                | Discussion &             |        | & End Term                            |
|       |   | Covariance                                | Examples                 |        | Exam                                  |
| 18    | Conditional Expectation                               | Elaborate the notion                      | Lecture,                 | 2201.3 | Quiz, Sessional                       |
|       | 1   | of Expectation                            | Discussion &             |        | & End Term                            |
|       |   | _   | Examples                 |        | Exam                                  |
| 19    | Correlation Coefficient                               | Calculate the                             | Lecture,                 | 2201.3 | Quiz, Sessional                       |
|       |   | Correlation                               | Discussion &             |        | & End Term                            |
|       |   | Coefficient                               | Examples                 |        | Exam                                  |
| 20    | Chebyschev's Inequality                               | Understand the                            | Lecture,                 | 2201.2 | Quiz, Sessional                       |
|       | energisene ( s mequanty                               | concept of                                | Discussion &             |        | & End Term                            |
|       |   | Chebyschev's                              | Examples                 |        | Exam                                  |
|       |   | Inequality                                | Examples                 |        |                                       |
| 21    | Tutorial-Problem Solving                              | Apply the concepts                        | Discussion &             | 2201.3 | Quiz, Sessional                       |
| 21    | Session   | in real world                             | Examples                 | 2201.5 | & End Term                            |
|       |   | problems                                  | Examples                 |        | Exam                                  |
| 22    | Probability Distributions:                            | Get the knowledge of                      | Lecture,                 | 2201.2 | Quiz, Sessional                       |
|       | Binomial Distribution                                 | Binomial                                  | Discussion &             | 2201.2 | & End Term                            |
|       |   | Distribution                              | Examples                 |        | Exam                                  |
| 23    | Poisson Distribution                                  | Get the knowledge of                      | Lecture,                 | 2201.2 | Quiz, Sessional                       |
| 23    | Tolsson Distribution                                  | Poisson Distribution                      | Discussion &             | 2201.2 | & End Term                            |
|       |   | Tologon Distribution                      | Examples                 |        | Exam                                  |
| 24    | Normal Distribution                                   | Get the knowledge of                      | Lecture,                 | 2201.2 | Quiz, Sessional                       |
|       | Troinia Bistiroation                                  | Normal Distribution                       | Discussion &             | 2201.2 | & End Term                            |
|       |   |   | Examples                 |        | Exam                                  |
| 25-27 | Brief overview about                                  | Develop the concept                       | Lecture,                 | 2201.4 | Quiz, Sessional                       |
| 20 27 | Sampling Theory                                       | of Sampling Theory                        | Discussion &             |        | & End Term                            |
|       |   |   | Examples                 |        | Exam                                  |
| 28    | Point Estimation                                      | Understand the                            | Lecture,                 | 2201.4 | Quiz, Sessional                       |
|       |   | concept of estimators                     | Discussion &             |        | & End Term                            |
|       |   | 1   | Examples                 |        | Exam                                  |
| 29    | MLE (Maximum  | Understand the                            | Lecture,                 | 2201.4 | Quiz, Sessional                       |
|       | Likelihood Estimate)                                  | concept of estimators                     | Discussion &             |        | & End Term                            |
|       |   |   | Examples                 |        | Exam                                  |
| 30    | Central Limit Theorem                                 | Understand the                            | Discussion &             | 2201.4 | Quiz, Sessional                       |
|       |   | concept of Central                        | Examples                 |        | & End Term                            |
|       |   | Limit Theorem                             | 1                        |        | Exam                                  |
| 31    | Interval Estimation                                   | Understand the                            | Lecture,                 | 2201.4 | Quiz, Sessional                       |
|       |   | concept of estimators                     | Discussion &             |        | & End Term                            |
|       |   |   | Examples                 |        | Exam                                  |
| 32    | Tutorial-Problem Solving                              | Apply the concepts                        | Discussion &             | 2201.4 | Quiz & End                            |
|       | Session   | in real world                             | Examples                 |        | Term Exam                             |
| 22    | TD. A. CIT. 4   | problems                                  | Τ                        | 2201.7 | 0: 0 5:                               |
| 33    | Testing of Hypothesis:                                | Analyze the                               | Lecture,                 | 2201.5 | Quiz & End                            |
|       | Statistical Hypothesis,<br>Null Hypothesis, Alternate | Hypothesis                                | Discussion &             |        | Term Exam                             |
|       | Hypothesis & Types of                                 |   | Examples                 |        |                                       |
|       | Error   |   |                          |        |                                       |
| 34    | Level of Significance &                               | Analyze the                               | Lecture,                 | 2201.5 | Quiz & End                            |
|       | Critical Region                                       | Hypothesis                                | Discussion &             |        | Term Exam                             |
|       |   | , i                                       | Examples                 |        |                                       |
| 35    | Procedure for Testing of                              | Analyze the                               | Lecture,                 | 2201.5 | Quiz & End                            |
|       | Hypothesis  | Hypothesis                                | Discussion &             |        | Term Exam                             |
|       |   |   | Examples                 |        |                                       |
|       | 1   | 1   |                          | 1      | ı                                     |

| 36 | t-Distribution                               | Understand t-<br>Distribution                   | Lecture, Discussion &          | 2201.2                  | Quiz & End<br>Term Exam |  |  |  |  |  |
|----|--|---|--------------------------------|-------------------------|-------------------------|--|--|--|--|--|
|    |  |   | Examples                       |                         | Term Exam               |  |  |  |  |  |
| 37 | Test of Significance based on t-Distribution | Apply the tests of Hypothesis                   | Lecture,<br>Discussion &       | 2201.5                  | Quiz & End<br>Term Exam |  |  |  |  |  |
|    |  |   | Examples                       |                         |                         |  |  |  |  |  |
| 38 | F- Distribution                              | Understand F-<br>Distribution                   | Lecture, Discussion & Examples | Discussion &            |                         |  |  |  |  |  |
| 39 | Test of Significance based on F-Distribution | Apply the tests of<br>Hypothesis                | Lecture, Discussion & Examples | Quiz & End<br>Term Exam |                         |  |  |  |  |  |
| 40 | Chi-square Distribution                      | Understand Chi-<br>square Distribution          | Lecture, Discussion & Examples | 2201.2                  | Quiz & End<br>Term Exam |  |  |  |  |  |
| 41 | Chi square Test                              | Apply the tests of<br>Hypothesis                | Lecture, Discussion & Examples | 2201.5                  | Quiz & End<br>Term Exam |  |  |  |  |  |
| 42 | Tutorial-Problem Solving                     | Apply the concepts<br>in real world<br>problems | Discussion &<br>Examples       | 2201.5                  | Quiz & End<br>Term Exam |  |  |  |  |  |

# G. COURSE ARTICULATION MATRIX (MAPPING OF COs WITH POs)

| СО       | STATEMENT   |         | CORRELATION WITH PROGRAM OUTCOMES |         |         |         |         |         |         |         |          |          | CORRELATION WITH PROGRAM SPECIFIC OUTCOMES |       |       |       |
|----------|---|---------|-----------------------------------|---------|---------|---------|---------|---------|---------|---------|----------|----------|--|-------|-------|-------|
|          |   | PO<br>1 | PO<br>2                           | PO<br>3 | PO<br>4 | PO<br>5 | PO<br>6 | PO<br>7 | PO<br>8 | PO<br>9 | PO<br>10 | PO<br>11 | PO<br>12                                   | PSO 1 | PSO 2 | PSO 3 |
| MA2201.1 | Apply the concept of probability and related theorems in solving various real-world problems.   |         | 2                                 | 1       | 2       | 1       | 2       | 3       | 3       | 2       | 1        | 2        | 1  | 3     | 2     | 1     |
| MA2201.2 | Understand the key concept of random variable, its probability distributions including mean, expectation, variance and moments.         | 3       | 2                                 | 1       | 2       | 1       | 1       | 3       | 3       | 2       | 1        | 2        | 1  | 3     | 1     | 2     |
| MA2201.3 | Implement the variation and the relation between two random variables by using the concept of correlation.                              | 3       | 2                                 | 1       | 2       | 1       | 1       | 3       | 3       | 2       | 1        | 2        | 1  | 3     | 1     | 1     |
| MA2201.4 | Comprehend the concept of random sample and its sampling distribution which will enhance the logical & analytical skills.               |         | 2                                 | 1       | 2       | 1       | 2       | 3       | 3       | 2       | 1        | 2        | 1  | 2     | 2     | 2     |
| MA2201.5 | Apply the statistics for testing the significance of the given large and small sample data by using t-test, F-test and Chi-square test. | 3       | 2                                 | 1       | 2       | 1       | 2       | 3       | 3       | 2       | 1        | 2        | 1  | 3     | 3     | 2     |

<sup>1-</sup> Low Correlation; 2- Moderate Correlation; 3- Substantial Correlation

# **H.** Course Outcome Attainment Level Matrix:

| СО     | STATEMENT   |      | ATTAINMENT OF PROGRAM OUTCOMES THRESHOLD VALUE: 40% |      |      |      |      |      |      |      |       |       |       |       | ATTAINMENT OF<br>PROGRAM SPECIFIC<br>OUTCOMES |       |  |  |
|--------|---|------|---|------|------|------|------|------|------|------|-------|-------|-------|-------|---|-------|--|--|
| 2201.1 | Apply the concept of probability and related theorems in solving various real-world problems.   | PO 1 | PO 2  | PO 3 | PO 4 | PO 5 | PO 6 | PO 7 | PO 8 | PO 9 | PO 10 | PO 11 | PO 12 | PSO 1 | PSO 2   | PSO 3 |  |  |
| 2201.2 | Understand the key concept of random variable, its probability distributions including mean, expectation, variance and moments.         |      |   |      |      |      |      |      |      |      |       |       |       |       |   |       |  |  |
| 2201.3 | Implement the variation and the relation between two random variables by using the concept of correlation.                              |      |   |      |      |      |      |      |      |      |       |       |       |       |   |       |  |  |
| 2201.4 | Comprehend the concept of random sample and its sampling distribution which will enhance the logical & analytical skills.               |      |   |      |      |      |      |      |      |      |       |       |       |       |   |       |  |  |
| 2201.5 | Apply the statistics for testing the significance of the given large and small sample data by using t-test, F-test and Chi-square test. |      |   |      |      |      |      |      |      |      |       |       |       |       |   |       |  |  |

0-No Attainment; 1- Low Attainment; 2- Moderate Attainment; 3- Substantial Attainment