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1. Calculate the Kronecker product of the matrices C and D:

$$C = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \\ 2 & 3 & 1 \end{bmatrix} \quad \text{and} \quad D = \begin{bmatrix} 5 & 0 & 4 \\ 4 & 5 & 0 \\ 0 & 4 & 5 \end{bmatrix}$$

```
import numpy as np
from scipy.linalg import kron

C = np.array([[1, 2, 3], [3, 1, 2], [2, 3, 1]])
D = np.array([[5, 0, 4], [4, 5, 0], [0, 4, 5]])

kron_product_C_D = kron(C, D)
print("Kronecker Product of C and D:\n", kron_product_C_D)
```

```
Kronecker Product of C and D:

[[ 5  0  4 10  0  8 15  0 12]

[ 4  5  0  8 10  0 12 15  0]

[ 0  4  5  0  8 10  0 12 15]

[15  0 12  5  0  4 10  0  8]

[12  15  0  4  5  0  8 10  0]

[ 0  12  15  0  4  5  0  8 10]

[ 10  0  8  15  0  12  5  0  4]

[ 8  10  0  12  15  0  4  5  0]

[ 0  8  10  0  12  15  0  4  5]
```

2. Calculate the Kronecker Product of the matrices U and W:

$$U = \begin{bmatrix} 5 & 2 \\ 3 & 9 \end{bmatrix} \quad \text{and} \quad W = \begin{bmatrix} 5 & 0 & 4 & 9 \\ 4 & 5 & 0 & 9 \\ 0 & 4 & 5 & 0 \\ 1 & 2 & 3 & 4 \end{bmatrix}$$

```
U = np.array([[5, 2], [3, 9]])
W = np.array([[5, 0, 4, 9], [4, 5, 0, 9], [0, 4, 5, 0], [1, 2, 3, 4]])
kron_product_U_W = kron(U, W)
print("\nKronecker Product of U and W:\n", kron_product_U_W)
```

```
Kronecker Product of U and W:

[[25  0  20  45  10  0  8  18]

[20  25  0  45  8  10  0  18]

[ 0  20  25  0  0  8  10  0]

[ 5  10  15  20  2  4  6  8]

[15  0  12  27  45  0  36  81]

[12  15  0  27  36  45  0  81]

[ 0  12  15  0  0  36  45  0]

[ 3  6  9  12  9  18  27  36]]
```

3. Write a Python function kron\_add (A, B) that takes as input two 2-D NumPy array, A and B, and calculates their Kronecker sum. Use this function to calculate the Kronecker sum of the matrices C and D from question 1.

```
def kron_add(A, B):
    A_size = A.shape[0]
    B_size = B.shape[0]
    A_kron_I = np.kron(A, np.eye(B_size))
    I_kron_B = np.kron(np.eye(A_size), B)
    return A_kron_I + I_kron_B

kron_sum_C_D = kron_add(C, D)
print("\nKronecker Sum of C and D:\n", kron_sum_C_D)
```

```
Kronecker Sum of C and D:

[[6. 0. 4. 2. 0. 0. 3. 0. 0.]

[4. 6. 0. 0. 2. 0. 0. 3. 0.]

[0. 4. 6. 0. 0. 2. 0. 0. 3.]

[3. 0. 0. 6. 0. 4. 2. 0. 0.]

[0. 3. 0. 4. 6. 0. 0. 2. 0.]

[0. 0. 3. 0. 4. 6. 0. 0. 2.]

[2. 0. 0. 3. 0. 4. 6. 0. 0. 4.]

[0. 2. 0. 0. 3. 0. 4. 6. 0.]

[0. 0. 2. 0. 0. 3. 0. 4. 6.]
```

4. Find the distance matrix for the 3 points in the datamatrix

$$X = \begin{bmatrix} 0 & 0 \\ 1 & 1 \\ 2 & 2 \end{bmatrix}$$

```
X = np.array([[0, 0], [1, 1], [2, 2]])
dist_matrix = np.linalg.norm(X[:, np.newaxis] - X, axis=2)
print("\nDistance Matrix for X:\n", dist_matrix)
```

```
Distance Matrix for X:

[[0. 1.41421356 2.82842712]

[1.41421356 0. 1.41421356]

[2.82842712 1.41421356 0. ]]
```

Λ= [[-8.

[ 0.

[ 0.

0.

[ 0.2141865 -0.95302061 0.2141865 ]

Q.T= [[ 0.70710678 0.

-0.89897949 0.

0. 8.89897949]]

5. Use spectral decomposition to find one datamatrix X that is compatible with the distance matrix

$$D = \begin{bmatrix} 0 & 2 & 8 \\ 2 & 0 & 2 \\ 8 & 2 & 0 \end{bmatrix}$$

1

-0.70710678]

```
[-0.67388734 -0.30290545 -0.67388734]]

Data Matrix D (from spectral decomposition):
[[-0. 2. 8.]
[ 2. 0. 2.]
[ 8. 2. -0.]]
```

Start coding or generate with AI.