

# Online Advertising



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## Times Reporter Will Not Be Called to Testify in Leak Case

By MATT APUZZO 9:00 PM ET

The decision ends a seven-year legal fight over whether James Risen could be forced to name the sources of his reports on a botched C.I.A. operation.

39 Comments

France Orders



The Jiaozhou Bay Bridge, which cost \$2.3 billion, is the world's longest sea-crossing bridge.

Van Runbo/Xinhua via Associated Press

1 of 7 ◀ ▶

## The Opinion Pages

### Choke First, Ask Questions Later

By THE EDITORIAL BOARD

A new report suggests that this disavowed tactic has never gone away and sometimes officers use it as a first, not last, resort.

- Editorial: United in Outrage
- Sheryl Sandberg and Adam Grant: Speaking While Female
- Taking Note: The Sony Hack and the Gender Pay Gap
- The Stone: Why Life Is Absurd

### MENAGERIE

#### A Swarm in 'Dead City'

By GABRIELLE SELZ



At 14, I tried to run away. But millions of molting cicadas came between me and my freedom.

- Blow: Tamir Rice and the Value of Life
- Krugman: For the Love of Carbon
- Room for Debate: When Satire Cuts Both Ways
- Bruni, Douthat: Movies and Our Still-Wrenching History

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# OSU IN CONTROL

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# Online Advertising is Big Business

Multiple billion dollar industry

\$43B in 2013 in USA, 17% increase over 2012

[PWC, Internet Advertising Bureau, April 2013]

Higher revenue in USA than cable TV and nearly  
the same as broadcast TV

[PWC, Internet Advertising Bureau, Oct 2013]

Large source of revenue for Google and other  
search engines



# Canonical Scalable ML Problem

Problem is hard; we need all the data we can get!

- Success varies by type of online ad (banner, sponsor search, email, etc.) and by ad campaign, but can be less than 1% [Andrew Stern, iMedia Connection, 2010]

Lots of Data

- Lots of people use the internet
- Easy to gather labeled data



**A great success story for scalable ML**

# The Players

**Publishers:** NYTimes, Google, ESPN

- Make money displaying ads on their sites

**Advertisers:** Marc Jacobs, Fossil, Macy's, Dr. Pepper

- Pay for their ads to be displayed on publisher sites
- They want to attract business

**Matchmakers:** Google, Microsoft, Yahoo

- Match publishers with advertisers
- In real-time (i.e., as a specific user visits a website)

# Why Advertisers Pay?

## Impressions

- Get message to target audience
- e.g., brand awareness campaign

## Performance

- Get users to do something
- e.g., click on ad (pay-per-click) ← **Most common**
- e.g., buy something or join a mailing list

# Efficient Matchmaking

**Idea:** Predict probability that user will click each ad and choose ads to maximize probability

- Estimate  $P(\text{click} \mid \text{predictive features})$
- Conditional probability: probability **given** predictive features

## Predictive features

- Ad's historical performance
- Advertiser and ad content info
- Publisher info
- User info (e.g., search / click history)



# Publishers Get Billions of Impressions Per Day

But, data is **high-dimensional, sparse, and skewed**

- Hundreds of millions of online users
- Millions of unique publisher pages to display ads
- Millions of unique ads to display
- Very few ads get clicked by users

Massive datasets are crucial to tease out signal

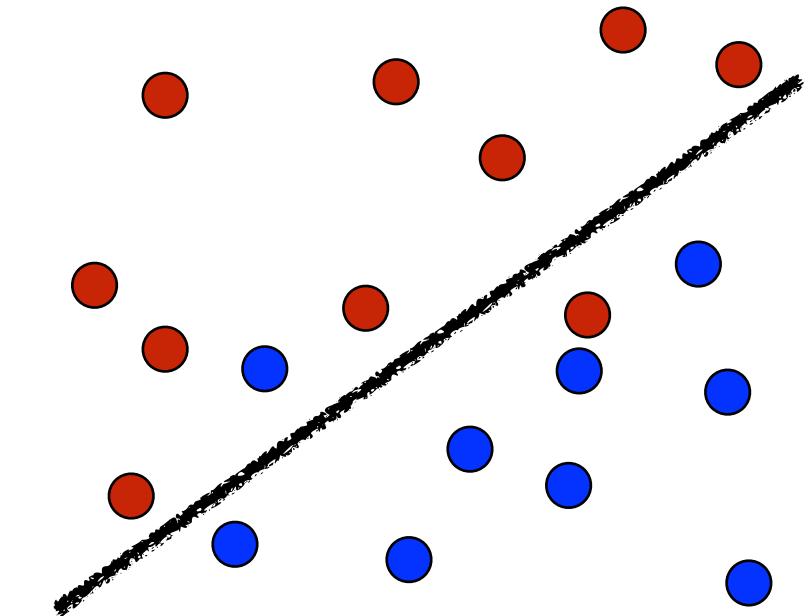
**Goal:** Estimate  $\mathbb{P}(\text{click} \mid \text{user, ad, publisher info})$

**Given:** Massive amounts of labeled data

# Linear Classification and Logistic Regression



# Classification

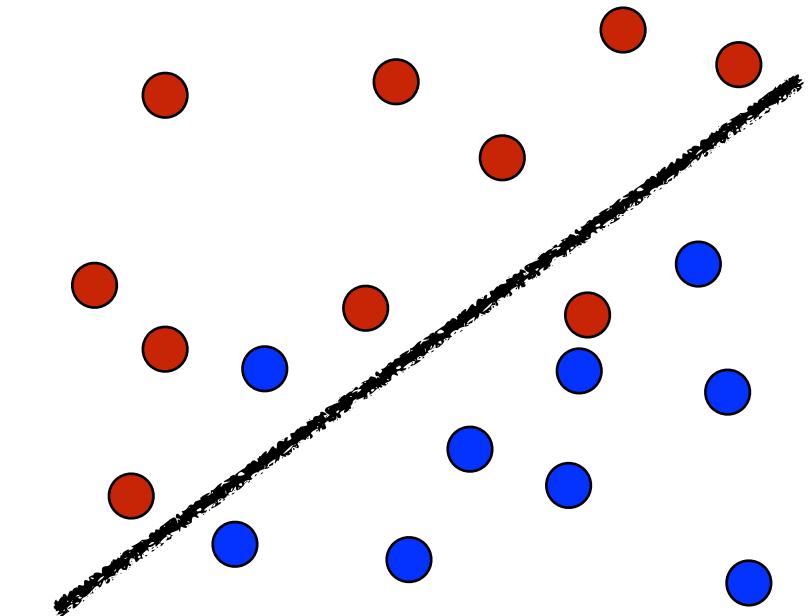


**Goal:** Learn a mapping from observations to discrete labels given a set of training examples (supervised learning)

**Example:** Spam Classification

- Observations are emails
- Labels are {spam, not-spam} (Binary Classification)
- Given a set of labeled emails, we want to predict whether a new email is spam or not-spam

# Classification

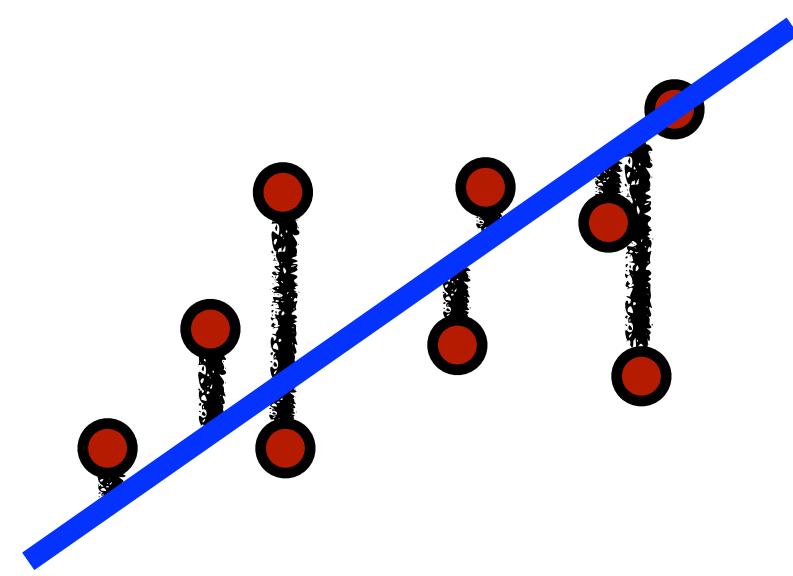


**Goal:** Learn a mapping from observations to discrete labels given a set of training examples (supervised learning)

**Example:** Click-through Rate Prediction

- Observations are user-ad-publisher triples
- Labels are {not-click, click} (Binary Classification)
- Given a set of labeled observations, we want to predict whether a new user-ad-publisher triple will result in a click

# Reminder: Linear Regression



**Example:** Predicting shoe size from height, gender, and weight

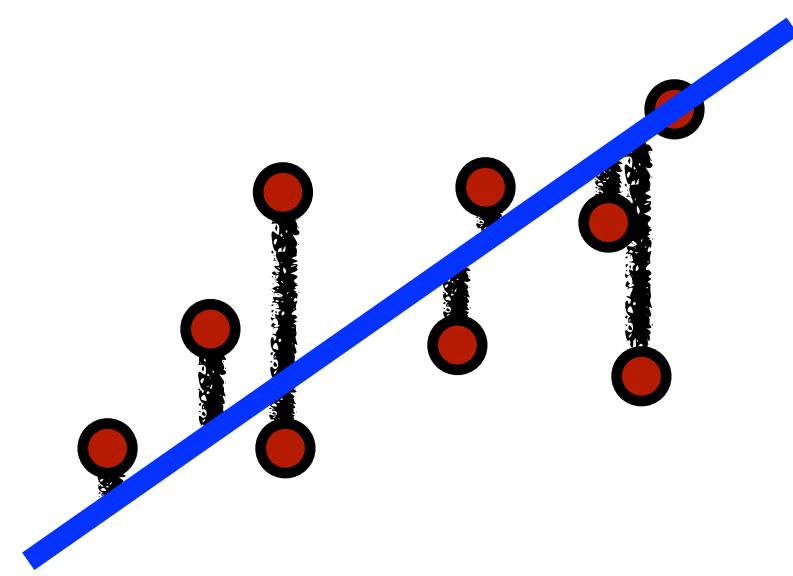
For each observation we have a feature vector,  $\mathbf{x}$ , and label,  $y$

$$\mathbf{x}^\top = [x_1 \quad x_2 \quad x_3]$$

We assume a *linear* mapping between features and label:

$$y \approx w_0 + w_1 x_1 + w_2 x_2 + w_3 x_3$$

# Reminder: Linear Regression



**Example:** Predicting shoe size from height, gender, and weight

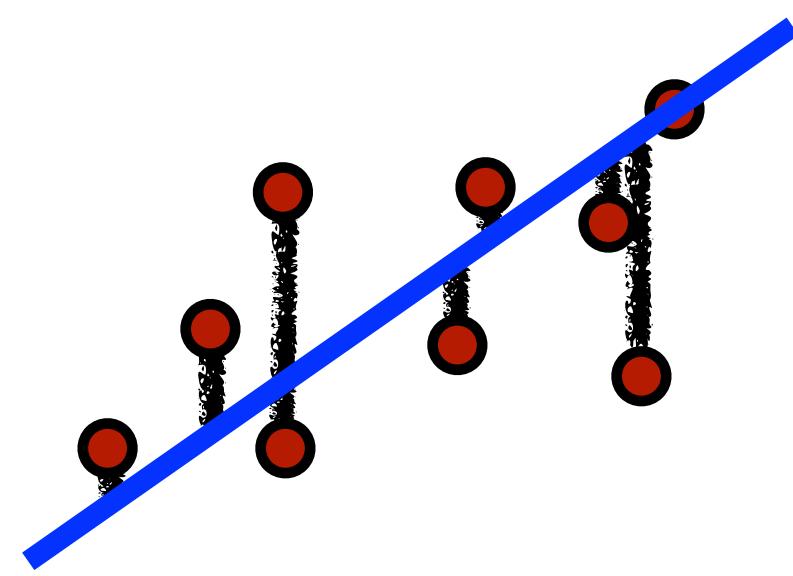
We can augment the feature vector to incorporate offset:

$$\mathbf{x}^\top = [1 \quad x_1 \quad x_2 \quad x_3]$$

We can then rewrite this linear mapping as scalar product:

$$y \approx \hat{y} = \sum_{i=0}^3 w_i x_i = \mathbf{w}^\top \mathbf{x}$$

# Why a Linear Mapping?



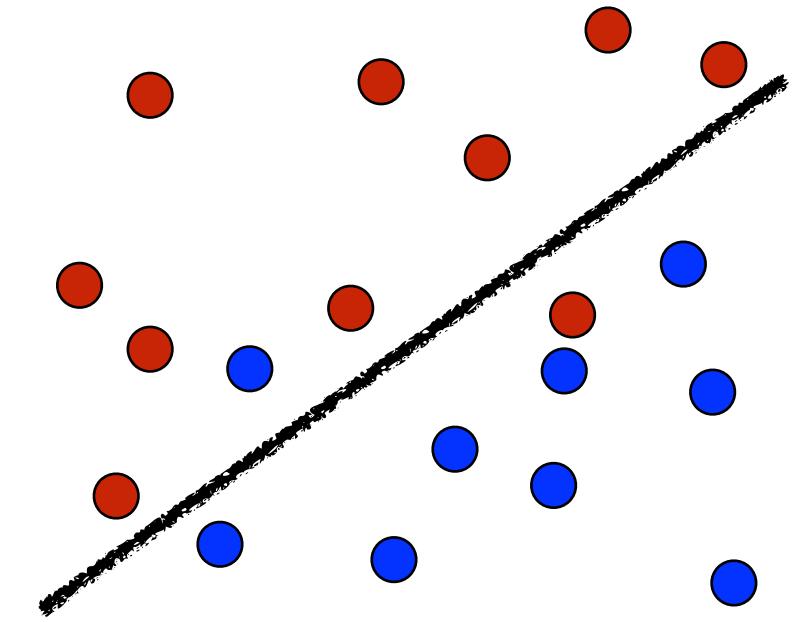
**Simple**

**Often works well in practice**

**Can introduce complexity via feature extraction**

Can we do something similar for classification?

# Linear Regression $\Rightarrow$ Linear Classifier



**Example:** Predicting rain from temperature, cloudiness, and humidity

Use the same feature representation:  $\mathbf{x}^\top = [1 \quad x_1 \quad x_2 \quad x_3]$

How can we make class predictions?

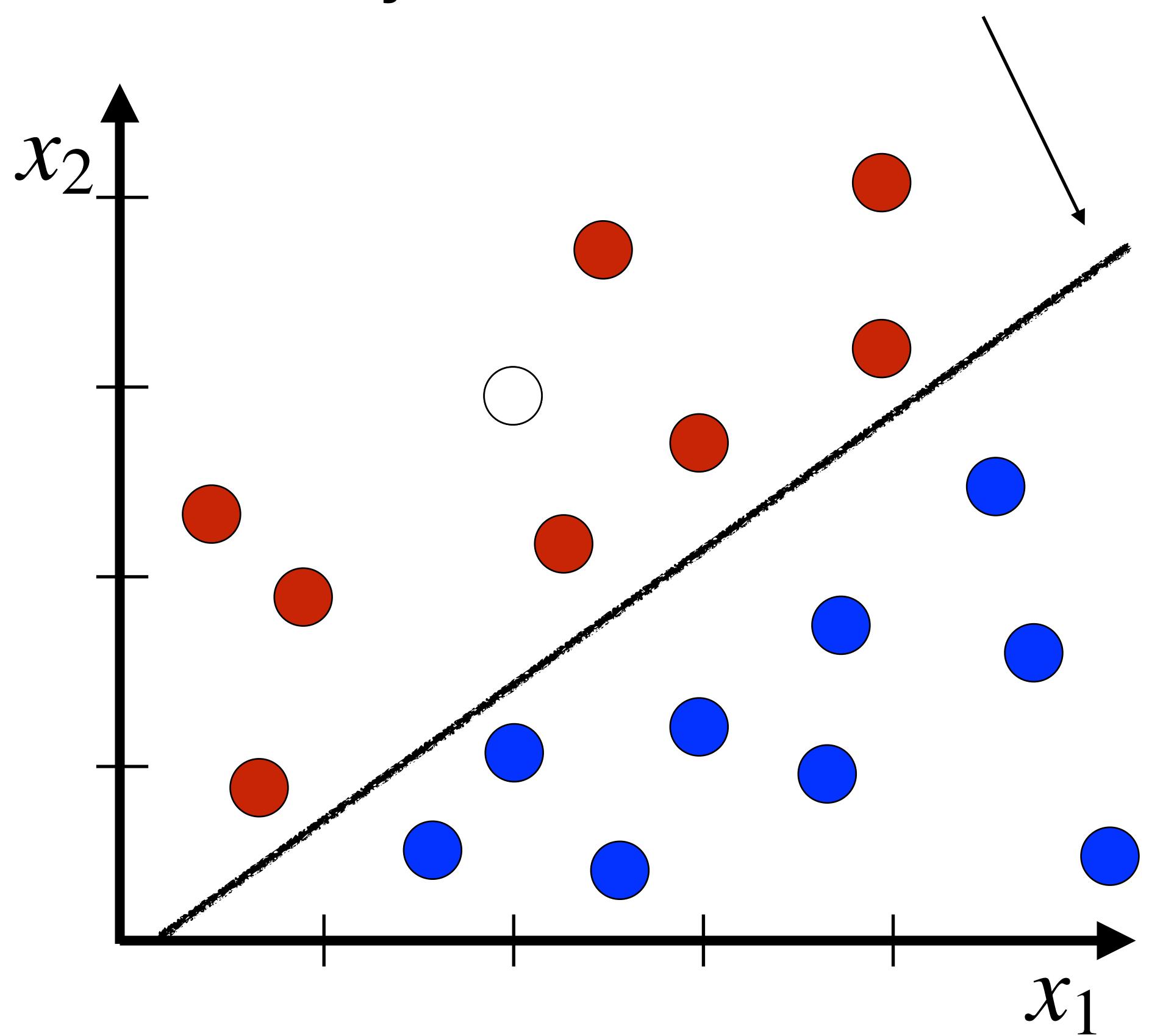
- {not-rain, rain}, {not-spam, spam}, {not-click, click}
- We can threshold by sign

$$\hat{y} = \sum_{i=0}^3 w_i x_i = \mathbf{w}^\top \mathbf{x} \implies \hat{y} = \text{sign}(\mathbf{w}^\top \mathbf{x})$$

# Linear Classifier Decision Boundary

Decision  
Boundary

$$3x_1 - 4x_2 - 1 = 0$$



Imagine  $\mathbf{w}^\top = [-1 \quad 3 \quad -4]$

$$\mathbf{x}^\top = [1 \quad 2 \quad 3]$$

$$\mathbf{x}^\top = [1 \quad 2 \quad 1] : \mathbf{w}^\top \mathbf{x} = 1$$

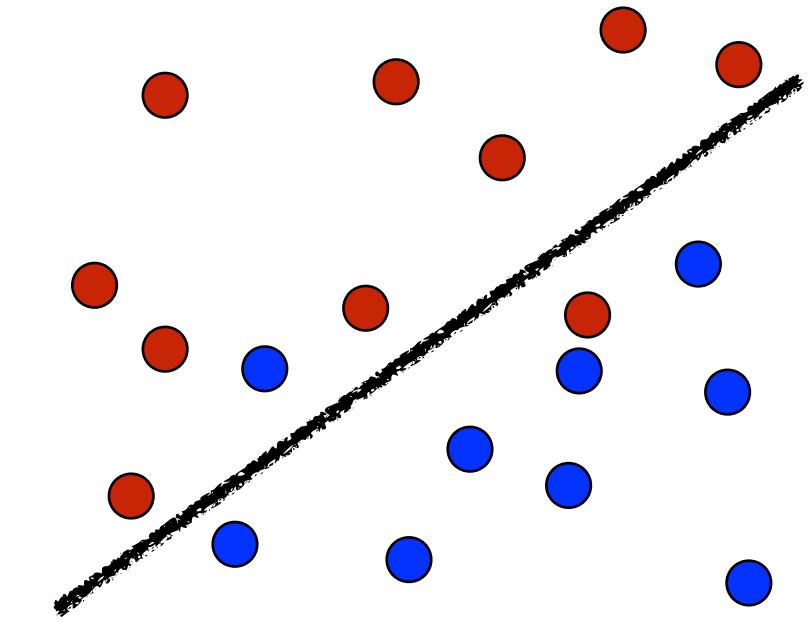
$$\mathbf{x}^\top = [1 \quad 5 \quad .5] : \mathbf{w}^\top \mathbf{x} = 12$$

$$\mathbf{x}^\top = [1 \quad 3 \quad 2.5] : \mathbf{w}^\top \mathbf{x} = -2$$

Let's interpret this rule:  $\hat{y} = \text{sign}(\mathbf{w}^\top \mathbf{x})$

- $\hat{y} = 1 : \mathbf{w}^\top \mathbf{x} > 0$
- $\hat{y} = -1 : \mathbf{w}^\top \mathbf{x} < 0$
- Decision boundary:  $\mathbf{w}^\top \mathbf{x} = 0$

# Evaluating Predictions



**Regression:** can measure ‘closeness’ between label and prediction

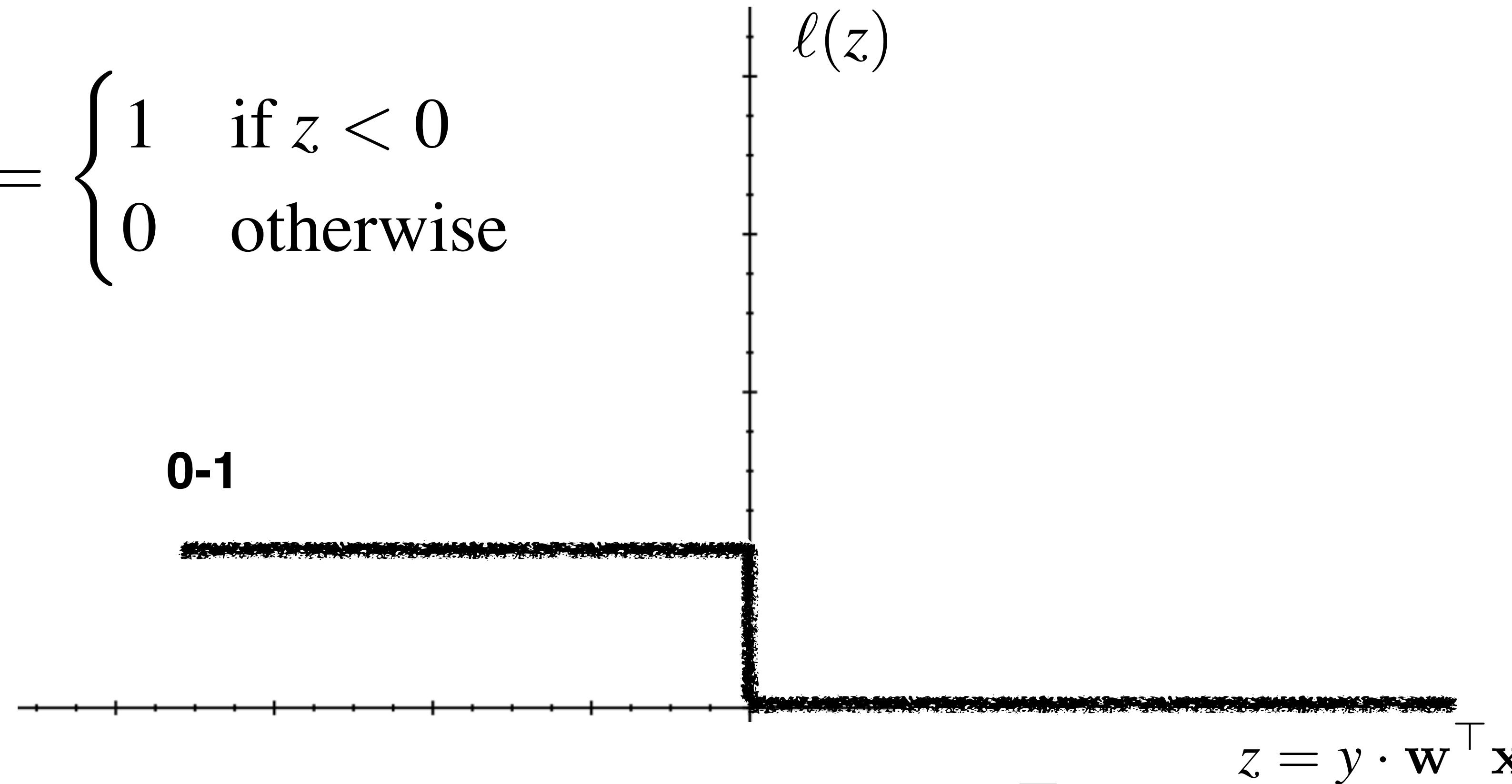
- Song year prediction: better to be off by a year than by 20 years
- Squared loss:  $(y - \hat{y})^2$

**Classification:** Class predictions are discrete

- 0-1 loss: Penalty is 0 for correct prediction, and 1 otherwise

# 0/1 Loss Minimization

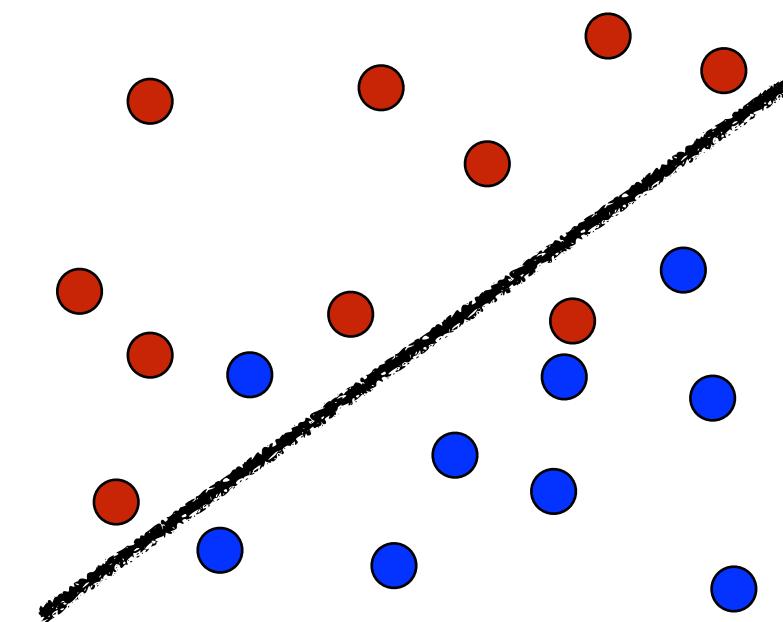
$$\ell_{0/1}(z) = \begin{cases} 1 & \text{if } z < 0 \\ 0 & \text{otherwise} \end{cases}$$



Let  $y \in \{-1, 1\}$  and define  $z = y \cdot \mathbf{w}^\top \mathbf{x}$

$z$  is positive if  $y$  and  $\mathbf{w}^\top \mathbf{x}$  have same sign, negative otherwise

# How Can We Learn Model ( $\mathbf{w}$ )?



Assume we have  $n$  training points, where  $\mathbf{x}^{(i)}$  denotes the  $i$ th point

Recall two earlier points:

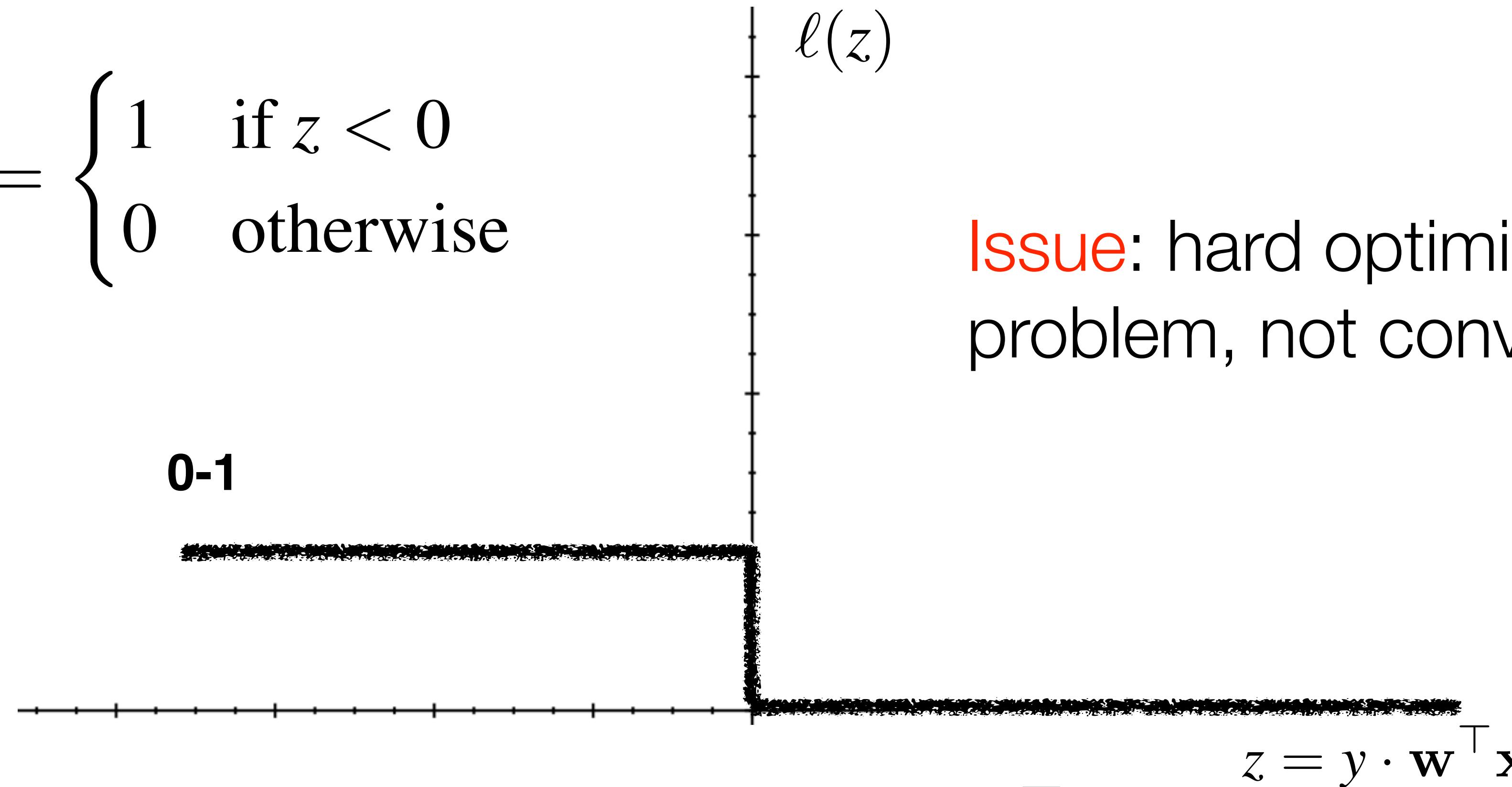
- *Linear assumption:*  $\hat{y} = \text{sign}(\mathbf{w}^\top \mathbf{x})$
- We use 0-1 loss:  $\ell_{0/1}(z)$

Idea: Find  $\mathbf{w}$  that minimizes average 0-1 loss over training points:

$$\min_{\mathbf{w}} \sum_{i=1}^n \ell_{0/1}\left(y^{(i)} \cdot \mathbf{w}^\top \mathbf{x}^{(i)}\right)$$

# 0/1 Loss Minimization

$$\ell_{0/1}(z) = \begin{cases} 1 & \text{if } z < 0 \\ 0 & \text{otherwise} \end{cases}$$

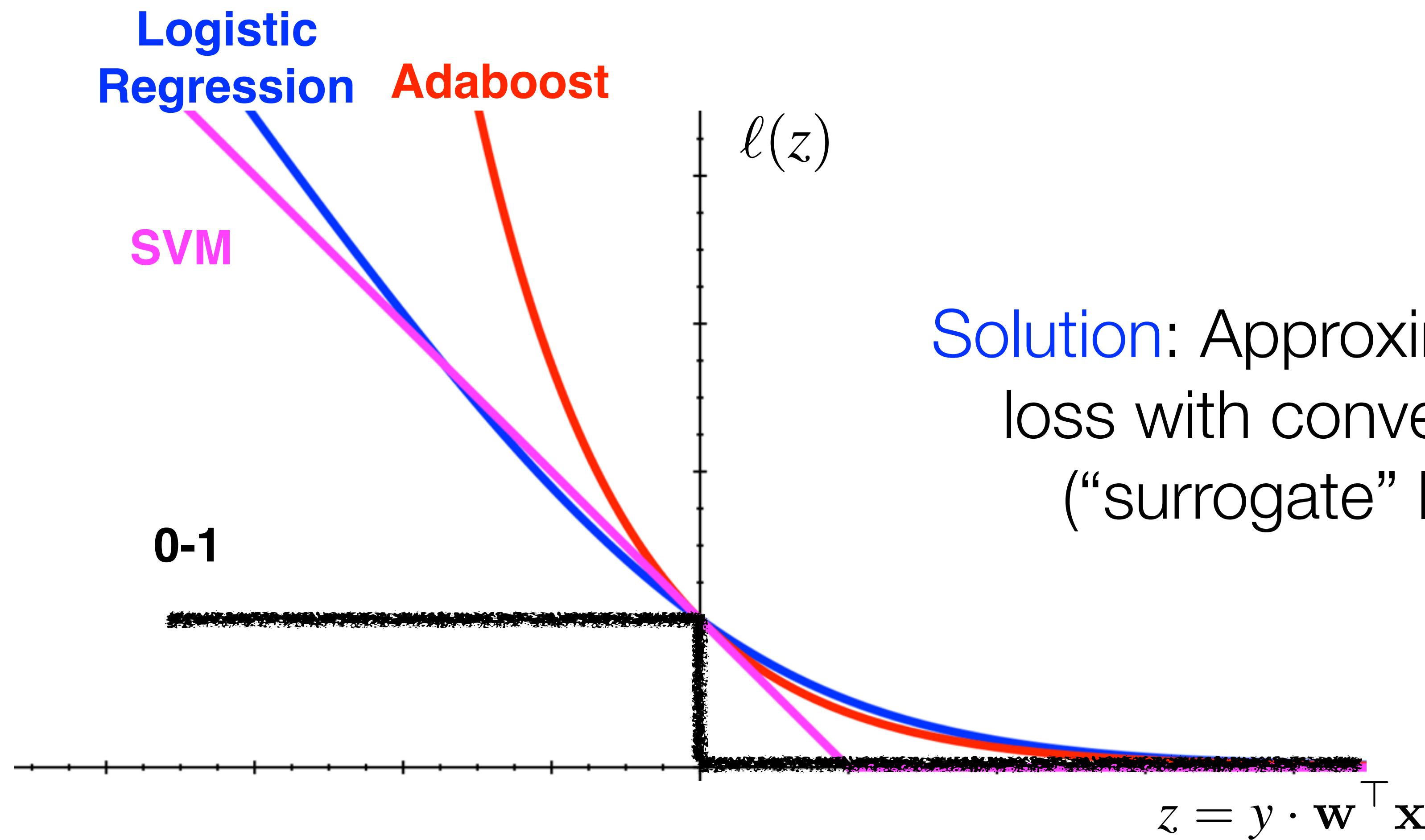


**Issue:** hard optimization problem, not convex!

Let  $y \in \{-1, 1\}$  and define  $z = y \cdot \mathbf{w}^\top \mathbf{x}$

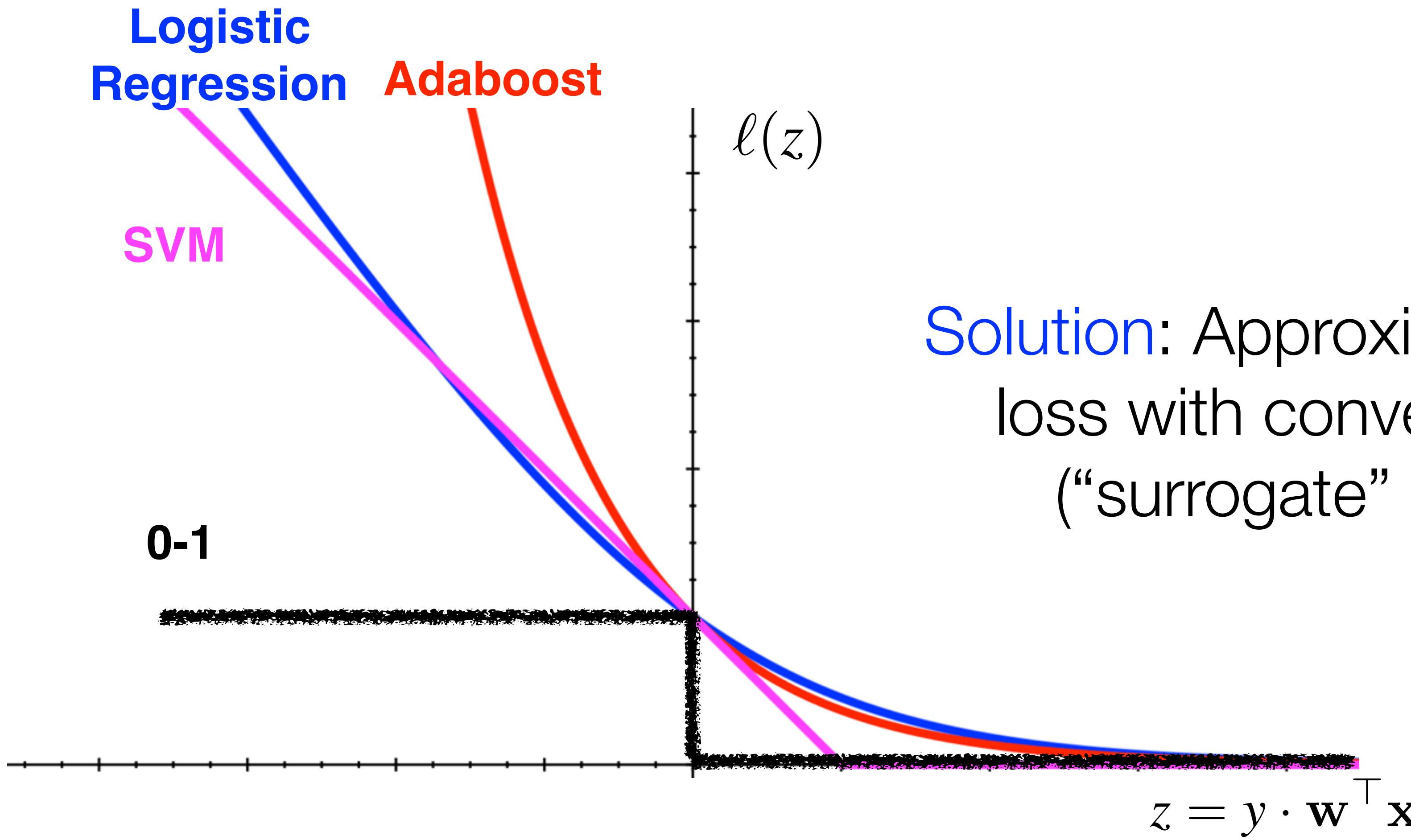
$z$  is positive if  $y$  and  $\mathbf{w}^\top \mathbf{x}$  have same sign, negative otherwise

# Approximate 0/1 Loss



SVM (hinge), Logistic regression (logistic), Adaboost (exponential)

# Approximate 0/1 Loss



Logistic loss (logloss):  $\ell_{log}(z) = \log(1 + e^{-z})$

# Logistic Regression Optimization

***Logistic Regression:*** Learn mapping ( $\mathbf{w}$ ) that minimizes logistic loss on training data

$$\min_{\mathbf{w}} \sum_{i=1}^n \ell_{log}\left(y^{(i)} \cdot \mathbf{w}^\top \mathbf{x}^{(i)}\right)$$

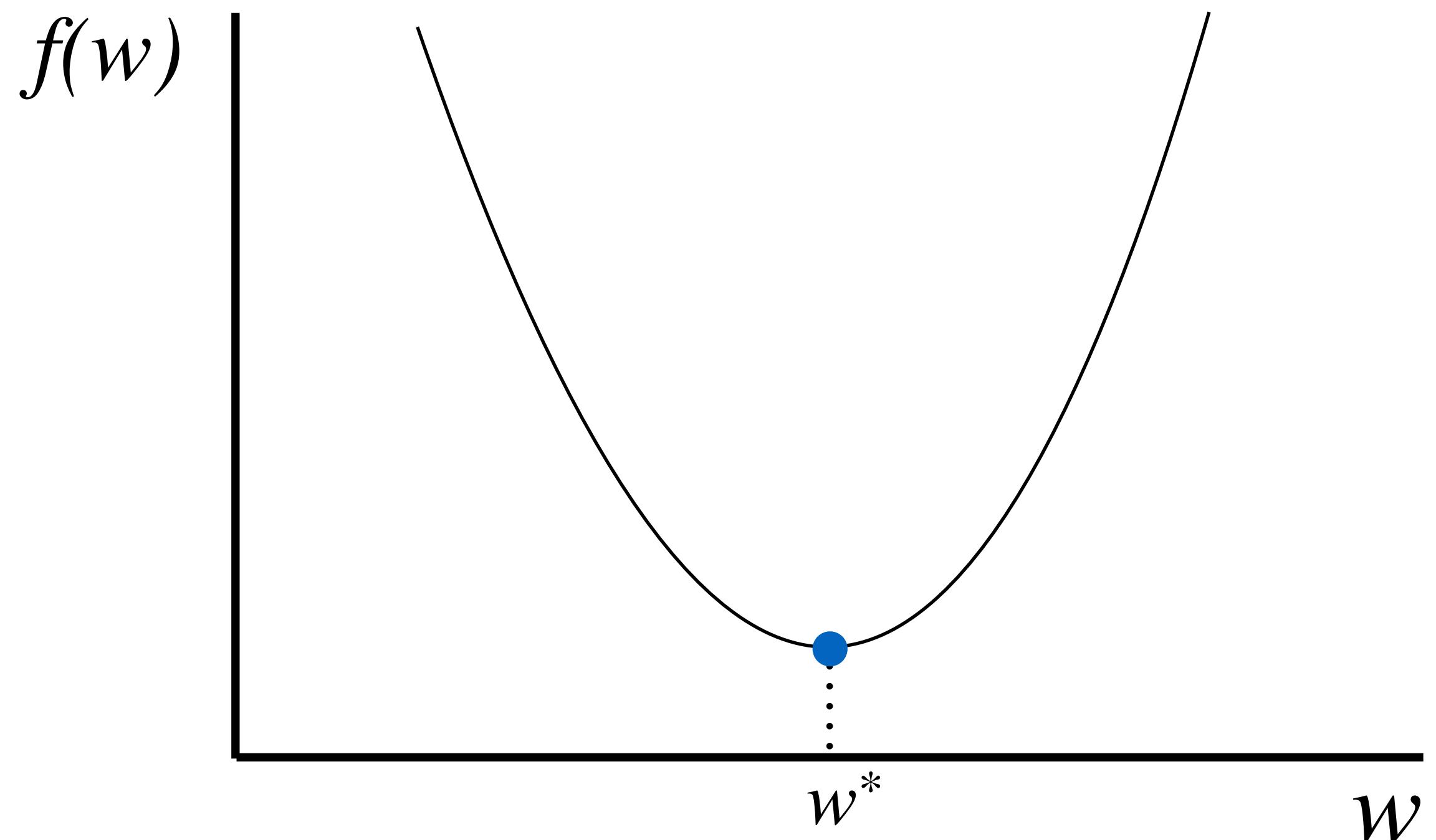
- Convex
- Closed form solution doesn't exist

# Logistic Regression Optimization

**Goal:** Find  $\mathbf{w}^*$  that minimizes

$$f(\mathbf{w}) = \sum_{i=1}^n \ell_{log}\left(y^{(i)} \cdot \mathbf{w}^\top \mathbf{x}^{(i)}\right)$$

- Can solve via Gradient Descent



**Update Rule:**  $\mathbf{w}_{i+1} = \mathbf{w}_i - \alpha \nabla f(\mathbf{w})$

Step Size

Gradient

$$\sum_{j=1}^n \left[ 1 - \frac{1}{1 + \exp(-y^{(j)} \mathbf{w}_i^\top \mathbf{x}^{(j)})} \right] (-y^{(j)} \mathbf{x}^{(j)})$$

# Logistic Regression Optimization

## Regularized

✓ **Logistic Regression:** Learn mapping ( $\mathbf{w}$ ) that minimizes logistic loss on training data

$$\min_{\mathbf{w}} \sum_{i=1}^n \ell_{log}\left(y^{(i)} \cdot \mathbf{w}^\top \mathbf{x}^{(i)}\right)$$

- Convex
- Closed form solution doesn't exist
- Can add regularization term (as in ridge regression)