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① Given two parameters  $n$  and  $m$ .

Given function =  $g(n, m)$

② Definition for  $\Omega(g(n, m))$

$\Omega(g(n, m)) = \{ f(n, m) : \text{there exist positive constants } c, n_0, \text{ and } m_0 \text{ such that}$

$0 \leq c g(n, m) \leq f(n, m) \text{ for all } n \geq n_0 \text{ or } m \geq m_0 \}$

Ex:  $f(n, m) = (2n * m) + 3$

$(2n * m + 3) \geq m * n$  here  $g(n, m) = m * n$   $c = 1$

hence  $f(m, n) = \Omega(m * n)$

③ Definition for  $\Theta(g(n, m))$

$\Theta(g(n, m)) = \{ f(n, m) : \text{there exist positive constants } c_1, c_2, n_0, \text{ and } m_0 \text{ such that}$

$0 \leq c_1 g(n, m) \leq f(n, m) \leq c_2 g(n, m) \text{ for all } n \geq n_0 \text{ or } m \geq m_0 \}$

Ex:  $f(n, m) = (n + 2m) + 5$

$1 * (n + 2m) \leq n + 2m + 5 \leq 12 * (n + 2m)$

here  $c_1 = 1$   $c_2 = 12$   $g(n) = n + 2m$

$f(n, m) = \Theta(n + 2m)$



② Given  $T(n) = 3T(n/2) + n \lg n$

According to the master theorem

$$T(n) = aT(n/b) + f(n)$$

Here we have  $a=3$   $b=2$   $f(n) = n \lg n$

Here  $\log_b^a = \log_2^3 = n^{1.58}$

$f(n)$  is less than the  $n^{1.58}$

Since  $f(n) = n \lg n = O(n^{\log a - \epsilon})$

$$= O(n^{\log 3 - \epsilon})$$

for any constant  $\epsilon > 0$ . based on this

case ① of the master theorem applies

and  $T(n) = \Theta(n^{\log_b^a})$

$$= \Theta(n^{\log_2^3})$$

$$= \Theta(n^{\log_2^3})$$

$$= \Theta(n^{1.58})$$