

HW07_Sampathirao_A

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R Markdown

#1.

```
data("mtcars")
head(mtcars)
```

```
##           mpg cyl disp  hp drat   wt  qsec vs am gear carb
## Mazda RX4      21.0   6  160 110 3.90 2.620 16.46  0  1    4    4
## Mazda RX4 Wag  21.0   6  160 110 3.90 2.875 17.02  0  1    4    4
## Datsun 710      22.8   4  108  93 3.85 2.320 18.61  1  1    4    1
## Hornet 4 Drive  21.4   6  258 110 3.08 3.215 19.44  1  0    3    1
## Hornet Sportabout 18.7   8  360 175 3.15 3.440 17.02  0  0    3    2
## Valiant         18.1   6  225 105 2.76 3.460 20.22  1  0    3    1
```

```
df<- data.frame(mtcars$mpg,mtcars$hp,
                row.names = row.names(mtcars))
colnames(df)<- c("mpg","hp")
head(df)
```

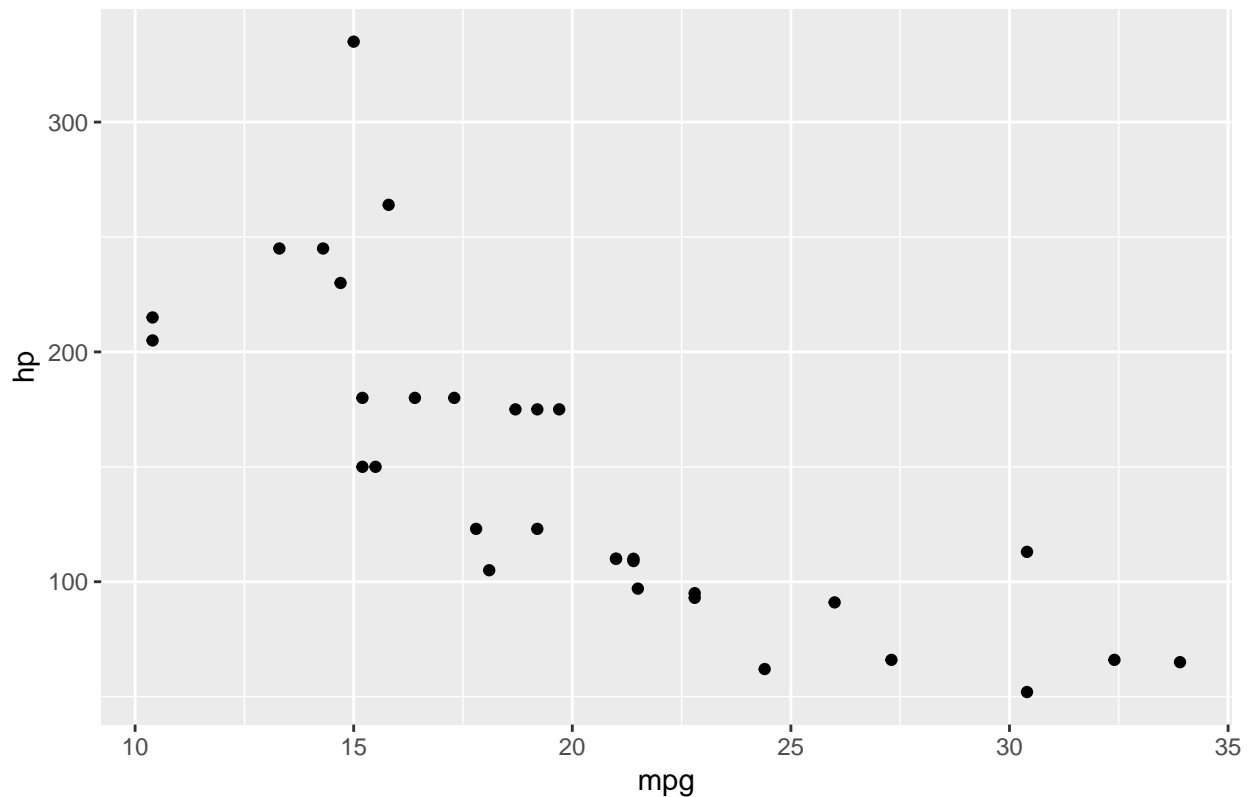
```
##           mpg  hp
## Mazda RX4      21.0 110
## Mazda RX4 Wag  21.0 110
## Datsun 710      22.8  93
## Hornet 4 Drive  21.4 110
## Hornet Sportabout 18.7 175
## Valiant         18.1 105
```

```
library(ggplot2)
```

```
## Registered S3 methods overwritten by 'ggplot2':
##   method      from
##   [.quosures  rlang
##   c.quosures  rlang
##   print.quosures rlang
```

```
ggplot(df, aes(x= mpg, y= hp)) + geom_point() + ggtitle("Scatterplot of mpg and hp")
```

Scatterplot of mpg and hp



From the plot, it looks like hp and mpg are negatively related. There is no reason to believe that relation is non linear. A relation can be said as non linear if the points are scattered all over and do not coincide which doesn't seem like in our case.

#2.

```
a<- cov(df$mpg,df$hp)
a
```

```
## [1] -320.7321
```

- There is a statistical association between mpg and hp because the variation of mpg coincides with the variation in hp on an average.
- The sign of the relation is negative, indicating that there is a negative association between mpg and hp
- The magnitude is relatively high, thus it is a strong association. However, covariance is not an apt measure to determine the strength of the relationship

#3.

```
b<- cor(df$mpg,df$hp)
b
```

```
## [1] -0.7761684
```

- There is a statistical relation between mpg and hp because the variation of mpg coincides with the variation in hp on an average

- b) The sign of the relation is negative, indicating that there is a negative association between mpg and hp
- c) The strength is considerably strong as the magnitude of the correlation coefficient is closer to the bound of -1.

#4. No we cannot conclude that hp causes mpg. From 2., we can infer that there is a negative relation between hp and mpg. And From 3., we can observe that the correlation coefficient is closer to the -1 bound. Hence, there is a negative correlation between hp and mpg. However, we cannot deduce from this that hp causes mpg. "Correlation does not imply causation."

#5.

$$\beta_1 = \frac{\sigma_{(x,y)}}{sd_x^2}$$

$$\beta_0 = \bar{y} - \beta_1 * \bar{x}$$

```
b1<- a/(sd(mtcars$mpg)^2)
b1
```

```
## [1] -8.829731
```

```
b0<- mean(mtcars$hp)- (b1*mean(mtcars$mpg))
b0
```

```
## [1] 324.0823
```

Beta_0 is the y intercept of the fitted line in our linear model. It is the average value of hp when mpg is 0.

Beta_1 is the slope of the fitted line in our linear model. It means, hp will change Beta_1 times with an incremental change in mpg, i.e., hp drops by 8.83 units when there is a unit increase in mpg.

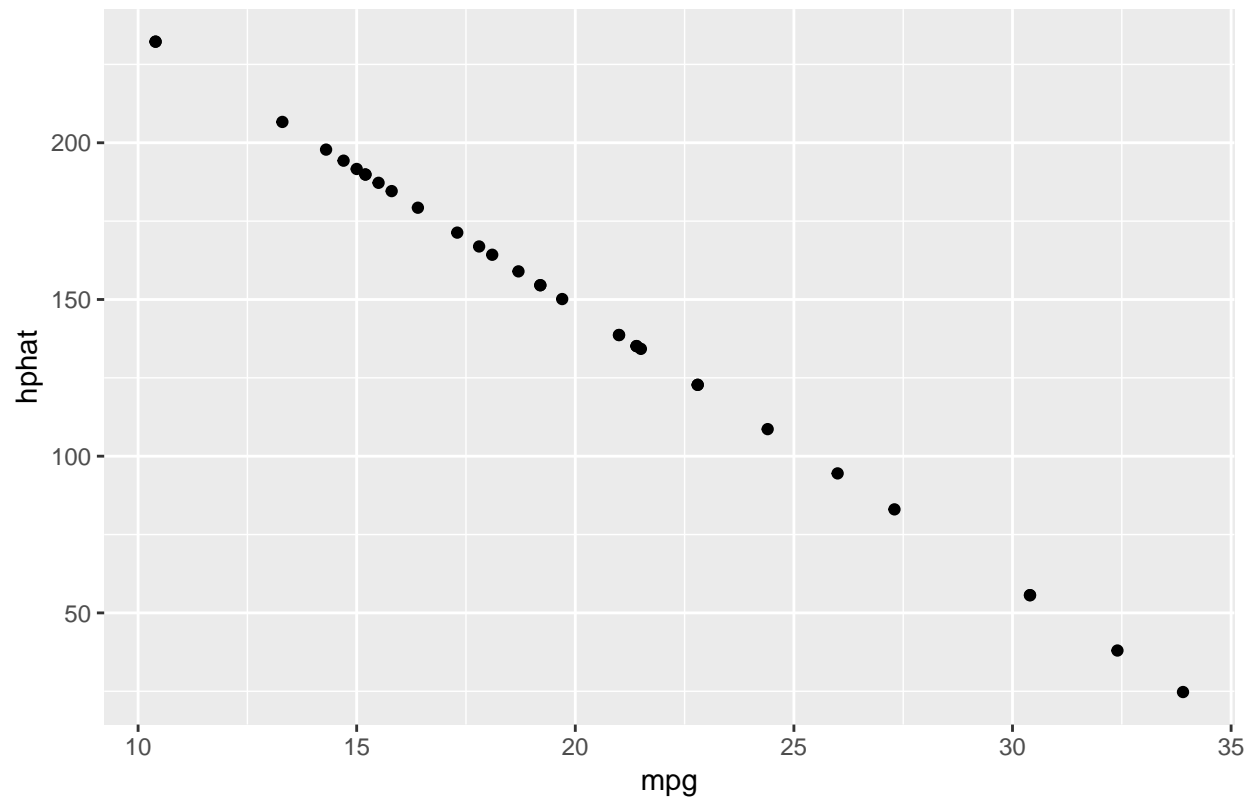
#6.

```
yhatfun<- function(x){
  yhat<- b0 + (b1*x)
  return(yhat)
}
hpfit<- yhatfun(df$mpg)
df1<- data.frame(df$mpg, df$hp, hpfit, row.names = row.names(df))
colnames(df1)<- c("mpg", "hp", "hphat")
head(df1)
```

```
##           mpg  hp   hphat
## Mazda RX4   21.0 110 138.6580
## Mazda RX4 Wag 21.0 110 138.6580
## Datsun 710    22.8  93 122.7644
## Hornet 4 Drive 21.4 110 135.1261
## Hornet Sportabout 18.7 175 158.9663
## Valiant      18.1 105 164.2642
```

```
ggplot(df1, aes(x= mpg, y= hphat)) + geom_point() +
  ggtitle("Scatterplot of mpg and fitted hp")
```

Scatterplot of mpg and fitted hp



#7.

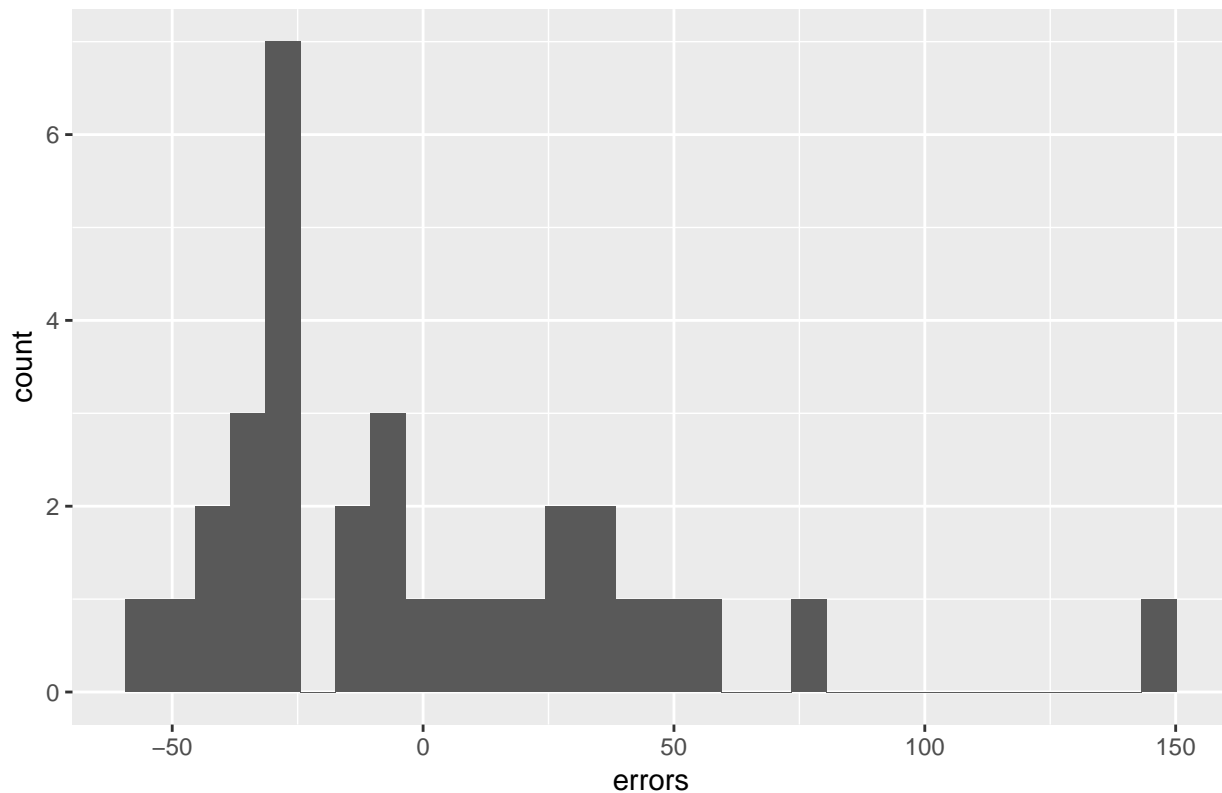
```
err<- df1$hp - df1$hphat
df2<- data.frame(df1$mpg, df1$hp, df1$hphat, err,
                 row.names = row.names(df1))
colnames(df2)<- c("mpg","hp","hphat","errors")
head(df2)
```

```
##           mpg  hp   hphat  errors
## Mazda RX4    21.0 110 138.6580 -28.65796
## Mazda RX4 Wag 21.0 110 138.6580 -28.65796
## Datsun 710    22.8  93 122.7644 -29.76445
## Hornet 4 Drive 21.4 110 135.1261 -25.12607
## Hornet Sportabout 18.7 175 158.9663 16.03366
## Valiant      18.1 105 164.2642 -59.26418
```

```
ggplot(df2, aes(x= errors)) + geom_histogram() + ggtitle("Histogram of errors")
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

Histogram of errors



Yes, they look normally distributed but the distribution looks skewed to the right.

```
SSE<- sum((df2$hp-df2$hphat)^2)
SSE #Sum of Standard Errors
```

```
## [1] 57935.56
```

#8.

$$se_{\beta_1} = se_{\hat{y}} \frac{1}{\sqrt{\sum (x_i - \bar{x})^2}}$$

where,

$$se_{\hat{y}} = \sqrt{\frac{\sum (y_i - \hat{y})^2}{n - 2}}$$

$$H_0 : \beta_1 = 0$$

$$H_a : \beta_1 \neq 0$$

```
n<-length(df2$hp)
k<-1 #1 variable in linear model
dof<- n-k-1 #Degree of freedom
stderr_y <- sqrt(sum((df2$hp-df2$hphat)^2)/dof)
stderr_b1 <- stderr_y* 1/(sqrt(sum((df2$mpg - mean(df2$mpg))^2)))
stderr_b1 #Standard Error of Beta1
```

```
## [1] 1.309585
```

```
t_val<- (b1-0)/stderr_b1  
t_val
```

```
## [1] -6.742389
```

```
t_crit<-qt(c(0.975,0.025),dof)  
t_crit
```

```
## [1] 2.042272 -2.042272
```

```
CI<- b1+(t_crit*stderr_b1)  
CI #95% Confidence Interval
```

```
## [1] -6.155202 -11.504260
```

```
2*pt(t_val,dof)
```

```
## [1] 1.787835e-07
```

We can see that `t_value` lies outside of our acceptance region of `t` distribution, therefore we reject the null hypothesis. Also, we note that `p` value is less than 0.05, it confirms that we can reject the null hypothesis, i.e., `Beta1` is not equal to 0 and this implies there exists a linear relationship between `mpg` and `hp`.

#9.

$$R^2 = \frac{TSS - SSE}{TSS}$$

```
TSS <- sum((df2$hp - mean(df2$hp))^2)  
Rsq <- (TSS -SSE)/TSS  
Rsq
```

```
## [1] 0.6024373
```

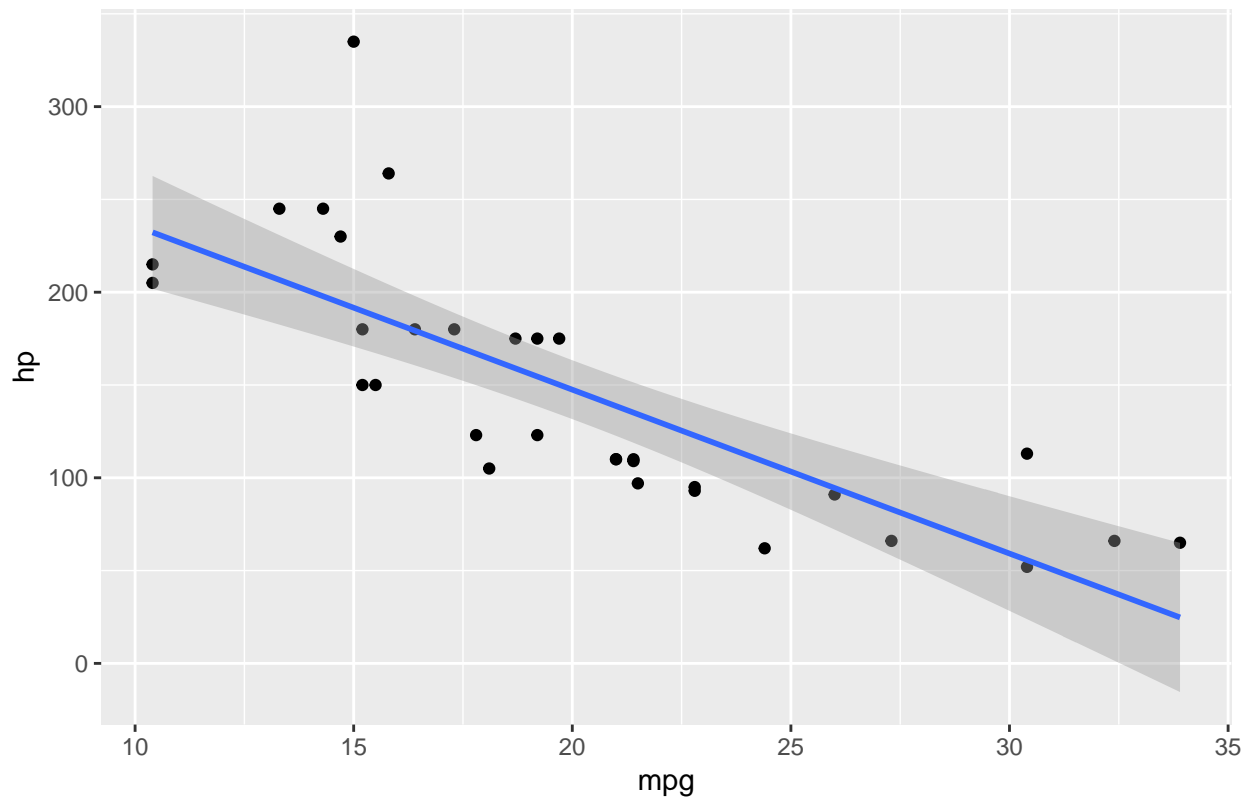
$R^2 = 0.6024$ implies that 60.24% of the variation in `hp` is defined by our linear model, i.e.,

$$hp = -8.83 * mpg + 324.08$$

#10.

```
ggplot(df2, aes(x=mpg, y=hp)) + geom_point() + geom_smooth(method=lm) + ggtitle("Regression Line & 95% CI")
```

Regression Line & 95% Confidence Interval for fitted hp



#11.

```
summary(lm(hp ~ mpg, data = df2))
```

```
##
## Call:
## lm(formula = hp ~ mpg, data = df2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -59.26  -28.93  -13.45   25.65  143.36
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    324.08     27.43   11.813 8.25e-13 ***
## mpg             -8.83       1.31   -6.742 1.79e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 43.95 on 30 degrees of freedom
## Multiple R-squared:  0.6024, Adjusted R-squared:  0.5892
## F-statistic: 45.46 on 1 and 30 DF,  p-value: 1.788e-07
```

Thus, we see that $\text{Beta}_0 = 324.08$ $\text{Beta}_1 = -8.83$ Standard Error of Beta 1 = 1.31 t-test for Beta 1 (t-value) = -6.742 and p-value = 1.79e-07 match our values in 5. and 8. Hence, proved!