



Lecture 12

Syntax Analysis

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Take aways from the last class

- Applying symbols to state

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- Goto Operations

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- Limitations of SLR Parser
- Closure operation on LR(1)

Example

- Consider the following grammar

$$S' \rightarrow S$$

$$S \rightarrow CC$$

$$C \rightarrow cC \mid d$$

- Compute closure(I) where $I = [S' \rightarrow .S, \$]$

$$S \rightarrow .S, \$$$

$$S \rightarrow .CC, \$$$

$$C \rightarrow .cC, c$$

$$C \rightarrow .cC, d$$

$$C \rightarrow .d, c$$

$$C \rightarrow .d, d$$

Example

Construct sets of LR(1) items for the grammar on previous slide

- $I_0 : S \rightarrow .S, \$$
 $S \rightarrow .CC, \$$
 $C \rightarrow .cC, c/d$
 $C \rightarrow .d, c/d$
- $I_1 : \text{goto}(I_0, S)$
 $S' \rightarrow S., \$$
- $I_2 : \text{goto}(I_0, C)$
 $S \rightarrow C.C, \$$
 $C \rightarrow .cC, \$$
 $C \rightarrow .d, \$$
- $I_3 : \text{goto}(I_0, c)$
 $C \rightarrow c.C, c/d$
 $C \rightarrow .cC, c/d$
 $C \rightarrow .d, c/d$
- $I_4 : \text{goto}(I_0, d)$
 $C \rightarrow d., c/d$
- $I_5 : \text{goto}(I_2, C)$
 $S \rightarrow CC., \$$
- $I_6 : \text{goto}(I_2, c)$
 $C \rightarrow c.C, \$$
 $C \rightarrow .cC, \$$
 $C \rightarrow .d, \$$
- $I_7 : \text{goto}(I_2, d)$
 $C \rightarrow d., \$$
- $I_8 : \text{goto}(I_3, C)$
 $C \rightarrow cC., c/d$
- $I_9 : \text{goto}(I_6, C)$
 $C \rightarrow cC., \$$

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- If $[A \rightarrow \alpha., a]$ is in I_i then $action[i, a]$ reduce $A \rightarrow \alpha$

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- If $[S' \rightarrow S., \$]$ is in I_i then $action[i, \$] = \text{accept}$
- If $goto(I_i, A) = I_j$ then $goto[i, A] = j$ for all non terminals A

Parse table

| State | c | d | \$ | S | C |
|-------|----|----|-----|---|---|
| 0 | s3 | s4 | | 1 | 2 |
| 1 | | | acc | | |
| 2 | s6 | s7 | | | 5 |
| 3 | s3 | s4 | | | 8 |
| 4 | r3 | r3 | | | |
| 5 | | | r1 | | |
| 6 | s6 | s7 | | | 9 |
| 7 | | | r3 | | |
| 8 | r2 | r2 | | | |
| 9 | | | r2 | | |

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- Merge LR(1) items having the same core

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- Construct action table as was done earlier
- Let $J = I_1 \cup I_2 \dots \cup I_k$
since I_1, I_2, \dots, I_k have same core, $goto(J, X)$ will have the same core
Let $K = goto(I_1, X) \cup goto(I_2, X) \dots goto(I_k, X)$ the $goto(J, X) = K$

LALR parse table ...

| State | c | d | \$ | S | C |
|-------|-----|-----|-----|---|----|
| 0 | s36 | s47 | | 1 | 2 |
| 1 | | | acc | | |
| 2 | s36 | s47 | | | 5 |
| 36 | s36 | s47 | | | 89 |
| 47 | r3 | r3 | r3 | | |
| 5 | | | r1 | | |
| 89 | r2 | r2 | r2 | | |

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 - ▶ Assume states $[X \rightarrow \alpha., a], [Y \rightarrow \alpha., b]$ and $[X \rightarrow \alpha., b], [Y \rightarrow \alpha., a]$
 - ▶ Merging the two states produces $[X \rightarrow \alpha., a/b], [Y \rightarrow \alpha., a/b]$

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 - ▶ $SLR(k) \leq LALR(k) \leq LR(k)$
 - ▶ $LL(k) \leq LR(k)$

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- Choice of A : Normally these are non terminals representing major program pieces such as an expression, statement or a block. For example if A is the nonterminal `stmt`, a might be semicolon or end

Parser Generator

- Some common LR parser generators
 - ▶ YACC: Yet Another Compiler Compiler
 - ▶ Bison: GNU Software
- Yacc/Bison source program specification (accept LALR grammars)

declaration

%%

translation rules

%%

supporting C routines

Yacc and Lex schema

