

(i) Necessary conditions for grammar to be LL(1) are:

(a) Left recursion absent

(b) unambiguous grammar

(c) Left-factored grammar.

Failing any of the above will lead to not LL(1).

(ii) Parse table for LL(1) must not contain any multiple entries.

(O/R)

A grammar will be LL(1) iff:

For a non-terminal  $X$ ,

$$X \rightarrow \alpha_1 | \alpha_2 | \dots | \alpha_n | \epsilon$$

$\text{First}(\alpha_1), \text{First}(\alpha_2), \dots, \text{First}(\alpha_n), \text{Follow}(X)$

are all mutually exclusive.

(doesn't contain any same element)

# [this will be corresponding to " $\epsilon$ " production]

Example:-

$$(a) S \rightarrow aSbS | bSaS | \epsilon$$

$$\Rightarrow \text{First}(aSbS) = \{a\}$$

$$\text{First}(bSaS) = \{b\}$$

$$\text{Follow}(S) = \{\$, a, b\}$$

$$\Rightarrow \text{Follow}(S) \cap \text{First}(aSbS) \neq \emptyset$$

$$\text{First}(bSaS) \neq \emptyset$$

∴

Hence, grammar is not LL(1).

Parse table will surely have multiple entry.



$$\begin{aligned}
 (b) \quad S &\rightarrow iCtSS_1 | a & \Rightarrow \{i\} \cap \{a\} = \emptyset \\
 S_1 &\rightarrow eS | e & \Rightarrow \{e\}, \{e, t\} \neq \emptyset \\
 C &\rightarrow b
 \end{aligned}$$

$\Downarrow$   
 Hence grammar is  
 not LL(1)

$$(c) \quad S \rightarrow aS_1 | bS | c$$

$$\begin{aligned}
 \Rightarrow \text{First}(aS_1) &= \{a\} \\
 \text{First}(bS) &= \{b\} \\
 \text{First}(c) &= \{c\}
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} \text{First}(aS_1) &= \{a\} \\ \text{First}(bS) &= \{b\} \\ \text{First}(c) &= \{c\} \end{aligned}} \right\} \begin{array}{l} \text{No element repeating} \\ \text{or no two will} \\ \text{have } \neq \emptyset \text{ intersection} \\ \text{and hence, } \underline{\underline{LL(1)}}. \end{array}$$