

**DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING**  
**INDIAN INSTITUTE OF TECHNOLOGY ROORKEE**  
**SPRING SEMESTER 2021-2022 Mid-Term Examination    Online mode**

**CSN312 PRINCIPLES OF PROGRAMMING LANGUAGES      Full Marks: 25**  
**Duration: 1 hour      4.3.2022**

Write your name and enrolment no. on the top of all pages. Each page should include your signature at the bottom. All the answers **MUST** be hand written in **BLUE** pen; otherwise zero mark will be given. Calculators are not allowed.

Answer all the questions. Answer for each question should begin on a new page.

Note:

Zero mark would be given for correct answers with no steps/unjustified steps/ incorrect justifications.

For each question, the final answer should be explicitly stated as: **Final Answer : ...**

1. For the term given below, construct an equivalent term (without any shortcut notation) with as few parentheses as possible. All the steps should be clearly justified. [6]

$(( (w (\lambda x. (\lambda y. (\lambda z. ((x z) (y z))))) ) u) v)$

2. Find the set of free variables, using the rules, for each of the following terms. [6]

(a)  $(\lambda x. x y) \lambda z. w \lambda w. w z y x$

(b)  $x \lambda z. x \lambda w. w z y$

All the steps should be clearly justified.

3. Find the normal form of the term

$(( (\lambda f. ((\lambda g. ((f f) g)) (\lambda h. (k h)))) (\lambda x. (\lambda y. y)))$

[6]

All the steps should be clearly justified.

4. Find the Principal Type (PT) of  $(\lambda x. \lambda y. \lambda z. x y z z)$  using the PT algorithm, if any. All the steps should be clearly justified in any case. [7]

**END**