



Lecture 12

Syntax Analysis

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February 14, 2025

Take aways from the last class

- Applying symbols to state

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- Goto Operations

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- Sets of Item

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- Limitations of SLR Parser
- Closure operation on LR(1)

Example

- Consider the following grammar

$$S' \rightarrow S$$

$$S \rightarrow CC$$

$$C \rightarrow cC \mid d$$

- Compute closure(I) where $I = [S' \rightarrow .S, \$]$

$$S \rightarrow .S, \$$$

$$S \rightarrow .CC, \$$$

$$C \rightarrow .cC, c$$

$$C \rightarrow .cC, d$$

$$C \rightarrow .d, c$$

$$C \rightarrow .d, d$$

Example

Construct sets of LR(1) items for the grammar on previous slide

- $I_0 : S \rightarrow .S, \$$
 $S \rightarrow .CC, \$$
 $C \rightarrow .cC, c/d$
 $C \rightarrow .d, c/d$
- $I_1 : \text{goto}(I_0, S)$
 $S' \rightarrow S., \$$
- $I_2 : \text{goto}(I_0, C)$
 $S \rightarrow C.C, \$$
 $C \rightarrow .cC, \$$
 $C \rightarrow .d, \$$
- $I_3 : \text{goto}(I_0, c)$
 $C \rightarrow c.C, c/d$
 $C \rightarrow .cC, c/d$
 $C \rightarrow .d, c/d$
- $I_4 : \text{goto}(I_0, d)$
 $C \rightarrow d., c/d$
- $I_5 : \text{goto}(I_2, C)$
 $S \rightarrow CC., \$$
- $I_6 : \text{goto}(I_2, c)$
 $C \rightarrow c.C, \$$
 $C \rightarrow .cC, \$$
 $C \rightarrow .d, \$$
- $I_7 : \text{goto}(I_2, d)$
 $C \rightarrow d., \$$
- $I_8 : \text{goto}(I_3, C)$
 $C \rightarrow cC., c/d$
- $I_9 : \text{goto}(I_6, C)$
 $C \rightarrow cC., \$$

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- If $[A \rightarrow \alpha., a]$ is in I_i then $action[i, a]$ reduce $A \rightarrow \alpha$

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- If $[S' \rightarrow S., \$]$ is in I_i then $\text{action}[i, \$] = \text{accept}$
- If $\text{goto}(I_i, A) = I_j$ then $\text{goto}[i, A] = j$ for all non terminals A

Parse table

State	c	d	\$	S	C
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

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due to more number of states in CLR, it is memory inefficient.
Decrease number of states in LALR

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- Merge LR(1) items having the same core

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- Construct action table as was done earlier
- Let $J = I_1 \cup I_2 \dots \cup I_k$

since I_1, I_2, \dots, I_k have same core, $goto(J, X)$ will have the same core
Let $K = goto(I_1, X) \cup goto(I_2, X) \dots goto(I_k, X)$ the $goto(J, X) = K$

LALR parse table ...

State	c	d	\$	S	C
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

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and CLR have more number of states than LALR | SLR...

states (CLR) \geq states (LALR) = states (SLR)

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- LALR parser can have new reduce-reduce conflicts
 - ▶ Assume states $[X \rightarrow \alpha., a], [Y \rightarrow \alpha., b]$ and $[X \rightarrow \alpha., b], [Y \rightarrow \alpha., a]$
 - ▶ Merging the two states produces $[X \rightarrow \alpha., a/b], [Y \rightarrow \alpha., a/b]$

LR means CLR by default.

there are two reduce possibilities when a/b comes in input when this state is at top of stack,

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 - ▶ $SLR(k) \leq LALR(k) \leq LR(k)$
 - ▶ $LL(k) \leq LR(k)$

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errors will not arise from goto table



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- Choice of A : Normally these are non terminals representing major program pieces such as an expression, statement or a block. For example if A is the nonterminal `stmt`, `a` might be semicolon or end

Parser Generator

- Some common LR parser generators
 - ▶ YACC: Yet Another Compiler Compiler
 - ▶ Bison: GNU Software
 - Yacc/Bison source program specification (accept LALR grammars)
- by default, they generate LALR parsers.

declaration

%%

translation rules

%%

supporting C routines

Yacc and Lex schema

