

w/ gaussian errors ML model is the one that minimizes

$$\chi^2 \Rightarrow \sum \left[ \frac{(d_i - A_i m)^2}{\sigma_i^2} \right]$$

for linear models

$$d = Am$$

$$(A^T N^T A) m = A^T N^T d$$

$$\langle (m - m_e)(m - m_e)^T \rangle = (A^T N^T A)^{-1} \mathbb{I}$$

$$\langle (Am - d_e)(Am - d_e)^T \rangle = A (A^T N^T A)^{-1} A^T \mathbb{I}$$

$$\chi^2 = (d - Am)^T N^T (d - Am)$$

$$\chi^2 = (d - A_m)^T N^{-1} (d - A_m) \quad r \equiv d - A_m \quad \langle \tilde{N}_{ij} \rangle = \langle \tilde{r}_i \tilde{r}_j \rangle$$

$$\chi^2 = r^T N^{-1} r$$

(residual)

$$V^T V = I$$

$$V^{-1} = V^T$$

$$\Rightarrow r^T V^T V N^{-1} V^T V r$$

$$\Rightarrow (Vr)^T \underbrace{(V N V^T)^{-1}}_{\Rightarrow N^{-1} V^T} (Vr)$$

$$\tilde{r} \Rightarrow Vr$$

$$\tilde{N} = V N V^T$$

$$\Rightarrow \chi^2 = \tilde{r}^T \tilde{N}^{-1} \tilde{r}$$

$$\Rightarrow \tilde{d} = V d = V A_m + V b$$

$$\Rightarrow V A = \tilde{A}$$

$$V b = \tilde{b}$$

I can calculate  $\tilde{N}$  directly

if I can calculate  $\langle \tilde{r}_i \tilde{r}_j \rangle$

$$\chi^2 = (d - A_m)^T N^{-1} (d - A_m)$$

Just like we had if  $N_{ij} = \langle r_i r_j \rangle$