

CMSC 330

Midterm Review

Administrative

Administrative

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Midterm is Thursday

Project 3 is due Friday

Quiz 3 on July 6th

Context Free Grammars

Basics

Basics

A way of describing sets of strings

CFGs subsume REs, DFAs, and NFAs

CFGs are often used as the basis of parsers

Generating Strings

A grammar “generates” strings via rewriting

Example

$$S \rightarrow 0S \mid 01 \mid \varepsilon$$

Generate the string 011

$$S \rightarrow$$

Generating Strings

A grammar “generates” strings via rewriting

Example

$$S \rightarrow 0S \mid 1S \mid \varepsilon$$

Generate the string 011

$$S \rightarrow 0S \rightarrow 01S \rightarrow 011S \rightarrow 011$$

Accepting Strings

Algorithm - is s in the language?

Find a rewriting of s starting from G 's start symbol

A sequence of rewrites is a derivation (or parse)

Discovering the derivation is called parsing

Creating Grammars

Write a grammar for $a^n b^n$

— — —

$S \rightarrow$

Write a grammar for $a^n b^n$

— — —

$S \rightarrow aSb \mid \varepsilon$

Write a grammar for $a^i b^j a^k$ where $k = i + j$ and $i, j, k \geq 0$

— — —

$S \rightarrow$

Wire a grammar for $a^i b^j a^k$ where $k = i + j$ and $i, j, k \geq 0$

$S \rightarrow aSa \mid T$

$T \rightarrow bTa \mid \varepsilon$

Ambiguity

Ambiguity

A grammar is ambiguous if there are multiple leftmost derivations of the same string

Give a leftmost derivation for $((()))$

$$S \rightarrow SS \mid (S) \mid \varepsilon$$
$$S \rightarrow (S) \rightarrow (SS) \rightarrow ((S)S) \rightarrow ((())S) \rightarrow ((()(S))) \rightarrow (((())))$$

Prove that the grammar is ambiguous

Prove that the grammar is ambiguous by giving 2 different leftmost derivations of the same string

$S \rightarrow aS \mid Sb \mid SS \mid ab$

Prove that the grammar is ambiguous

Prove that the grammar is ambiguous by giving 2 different leftmost derivations of the same string

$S \rightarrow aS \mid Sb \mid SS \mid ab$

$S \rightarrow aS \rightarrow aSb \rightarrow aabb$

$S \rightarrow Sb \rightarrow aSb \rightarrow aabb$

Parsing

Provide a leftmost derivation for $a * a + b$

$S \rightarrow S + E \mid E$

$E \rightarrow E * L \mid L$

$L \rightarrow a \mid b$

$S \rightarrow$

Provide a leftmost derivation for $a * a + b$

$S \rightarrow S + E \mid E$

$E \rightarrow E * L \mid L$

$L \rightarrow a \mid b$

$S \rightarrow S + E \rightarrow E + E \rightarrow E * L + E \rightarrow L * L + E \rightarrow a * L + E$
 $\rightarrow a * a + E \rightarrow a * a + L \rightarrow a * a + b$

Provide the Parse Tree for the derivation

$S \rightarrow S + E \rightarrow E + E$

$\rightarrow E * L + E \rightarrow L * L + E$

$\rightarrow a * L + E \rightarrow a * a + E$

$\rightarrow a * a + L \rightarrow a * a + b$

Provide the Parse Tree for the derivation

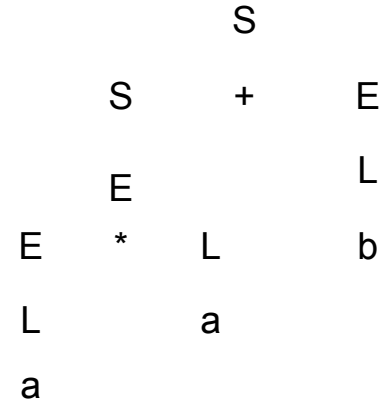
— — —

$S \rightarrow S + E \rightarrow E + E$

$\rightarrow E * L + E \rightarrow L * L + E$

$\rightarrow a * L + E \rightarrow a * a + E$

$\rightarrow a * a + L \rightarrow a * a + b$



Provide the AST

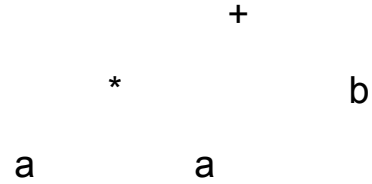
— — —

$S \rightarrow S + E \rightarrow E + E$

$\rightarrow E * L + E \rightarrow L * L + E$

$\rightarrow a * L + E \rightarrow a * a + E$

$\rightarrow a * a + L \rightarrow a * a + b$



Associativity

Associativity

Left-recursive = Left-associative

Right-recursive = right-associative

Make the Grammar Right Associative

— — —

$S \rightarrow S + E \mid E$

$S \rightarrow$

$E \rightarrow E * L \mid L$

$L \rightarrow a \mid b$

Make the Grammar Right Associative

— — —

$S \rightarrow S + E \mid E$

$E \rightarrow E * L \mid L$

$L \rightarrow a \mid b$

$S \rightarrow E + S \mid E$

$E \rightarrow L * E \mid L$

$L \rightarrow a \mid b$

Precedence

Precedence

Close to start symbol = lower precedence

Further from start symbol = higher precedence

Give + Higher Precedence Than *

— — —

$S \rightarrow S + E \mid E$

$E \rightarrow E * L \mid L$

$L \rightarrow a \mid b$

$S \rightarrow S * E \mid E$

$E \rightarrow E + L \mid L$

$L \rightarrow a \mid b$

First Sets

Provide The First Set For Each Production Rule

— — —

$S \rightarrow aAB \mid Bc$

$\text{FIRST}(S) =$

$A \rightarrow dB \mid Ac$

$\text{FIRST}(A) =$

$B \rightarrow Cg$

$\text{FIRST}(B) =$

$C \rightarrow f \mid d \mid \varepsilon$

$\text{FIRST}(C) =$

Provide The First Set For Each Production Rule

— — —

$S \rightarrow aAB \mid Bc$

$\text{FIRST}(S) = \{a, f, d, g\}$

$A \rightarrow dB \mid Ac$

$\text{FIRST}(A) = \{d\}$

$B \rightarrow Cg$

$\text{FIRST}(B) = \{f, d, g\}$

$C \rightarrow f \mid d \mid \varepsilon$

$\text{FIRST}(C) = \{f, d, \varepsilon\}$

Ruby Scan Method

Ruby Scan Method

Scan returns everything that the regex matches

Scan returns as a 2D array with each match as an array of all the capture groups

What is the output?

— — —

```
a = "CMSC 330 CMSC 351"
```

```
b = a.scan(/[A-Z]+/)
```

b

What is the output?

— — —

```
a = "CMSC 330 CMSC 351"
```

```
b = a.scan(/[A-Z]+/)
```

```
b
```

Output

```
b = ["CMSC", "CMSC"]
```

What is the output

— — —

```
a = "CMSC 330 CMSC 351"
```

```
b = a.scan(/[0-9]+ [A-Z]+/)
```

```
b
```

What is the output

— — —

```
a = "CMSC 330 CMSC 351"
```

```
b = a.scan(/[0-9]+ [A-Z]+)/)
```

```
b
```

Output

```
b = ["330 CMSC"]
```


What is the Output?

— — —

```
s = "To be, or not to be!"
```

```
a = s.scan(/(\S+) (\S+)/)
```

```
a.inspect
```

What is the Output?

```
s = "To be, or not to be!"
```

```
a = s.scan(/(\S+) (\S+)/)
```

```
a.inspect
```

Output

```
a = [["To", "be,"], ["or", "not"], ["to", "be!"]]
```

Closures

Closures

In OCaml, when you create a function, you create a “closure”

Function code associated with binding for variables

Closures

```
let f x y = x + y;;
```

When first created, this is the code with no bindings

Arguments can be applied one at a time

```
let g = f 6;;
```

This assigns g to be closure defined by f, with x=6

What would g 7 be? What would f 7 be?

Scoping

Scoping

Defined variables can be associated with a closure

Static Scoping

```
let x = 5;;
```

```
let f y = x + y;; (* f is a closure where x is bound to 5 *)
```

```
let x = 2;;
```

```
f 5;; (* What is the output? *)
```


Static Scoping

```
let x = 5;;
```

```
let f y = x + y;; (* f is a closure where x is bound to 5 *)
```

```
let x = 2;;
```

```
f 5;; (* What is the output? *)
```

10 is the output. This is static scoping.

Dynamic Scoping

```
let x = 5;;
```

```
let f y = x + y;; (* f is a closure where x is bound to 5 *)
```

```
let x = 2;;
```

```
f 5;; (* What is the output? *)
```

Dynamic Scoping

```
let x = 5;;
```

```
let f y = x + y;; (* f is a closure where x is bound to 5 *)
```

```
let x = 2;;
```

```
f 5;; (* What is the output? *)
```

7 is the output. Variables use the most recent declaration.

Midterm

Topics

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PL Concepts

Ruby

OCaml

NFA/DFA