

Lab 3 Tutorial

Janette Avelar & Anwesha Guha

1/25/2022

Intro

This week we will go over calculating probability from a standard normal distribution.

Note: All material is taken from Dr. Zopluoglu's 2021 EDUC 614 materials and adapted for this year's course.

We have adapted it to slide format using R.

Want to learn how we created R slide presentations? [This tutorial](#) is helpful.

Calculating Probability from a Standard Normal Distribution

Density for z-score

To compute density for a z-score, you can compute `dnorm()` from the base package. Below is the code to reproduce density calculations from Lecture 3a.

```
dnorm(x = -1)
```

```
## [1] 0.2419707
```

```
dnorm(x = 0)
```

```
## [1] 0.3989423
```

```
dnorm(x = 1)
```

```
## [1] 0.2419707
```

```
dnorm(x = 2)
```

```
## [1] 0.05399097
```

Lower-tail Probability

Lower-tail probability refers the probability of a random variable X taking the value x or less. In other words, it refers to the area under the normal curve on the left side of normal distribution.

Cumulative probability is also another term being used for lower-tail probability.

You can compute this by using the `pnorm()` function from the base package.

Examples

Suppose, you want to compute the probability of z scores being 0 or less than 0.

$$P(z < 0) = ?$$

```
pnorm(0, lower.tail = TRUE)
```

```
## [1] 0.5
```

What about probability of z score being -1 or less than -1?

$P(z < -1) = ?$

```
pnorm(-1, lower.tail = TRUE)
```

```
## [1] 0.1586553
```

Or probability of z score being 2 or less than 2?

$P(z < 2) = ?$

```
pnorm(2, lower.tail = TRUE)
```

```
## [1] 0.9772499
```


Upper-tail Probability

Upper-tail probability refers the probability of a random variable X taking the value x or more. In other words, it refers to the area under the normal curve on the right side of normal distribution.

You can compute this by using `pnorm()` from the base package, and setting `lower.tail = FALSE`.

Examples

Suppose you want to calculate the probability of z score being -1 or more than -1.

$$P(z > -1) = ?$$

```
pnorm(-1, lower.tail = FALSE)
```

```
## [1] 0.8413447
```

What about the probability of z score being 2 or more than 2?

$P(z > 2) = ?$

```
pnorm(2, lower.tail = FALSE)
```

```
## [1] 0.02275013
```

Probability between scores

If you want to compute the probability between two z-scores, then you need to get creative.

Suppose you want to compute the probability of z score being between -1 and 2.

You can do this by subtracting $P(z < -1)$ from $P(z < 2)$.

```
pnorm(2, lower.tail = TRUE) - pnorm(-1, lower.tail = TRUE)
```

```
## [1] 0.8185946
```

qnorm()

Another useful function is `qnorm()`. Consider this function as an inverse of `pnorm()`.

- `pnorm()` returns the cumulative probability given a z-score in a normal distribution
- `qnorm()` returns the z-score given the cumulative probability.

Example

Suppose you want to know that which z-score has a cumulative probability of 0.6.

```
qnorm(0.6, lower.tail=TRUE)
```

```
## [1] 0.2533471
```

Q-Q Plots

Import the data

Like in our previous tutorial where we learned how to create histograms and boxplots, in order to create a q-q plot our first step is to import the dataset we'd like to use.

```
Add <- read.csv(file = "/Users/janetteavelar/Desktop/Add.csv",  
                 header = TRUE)
```

Remember your working directory goes in the first line of code. You can set it manually, or use `getwd()` to find your file path.

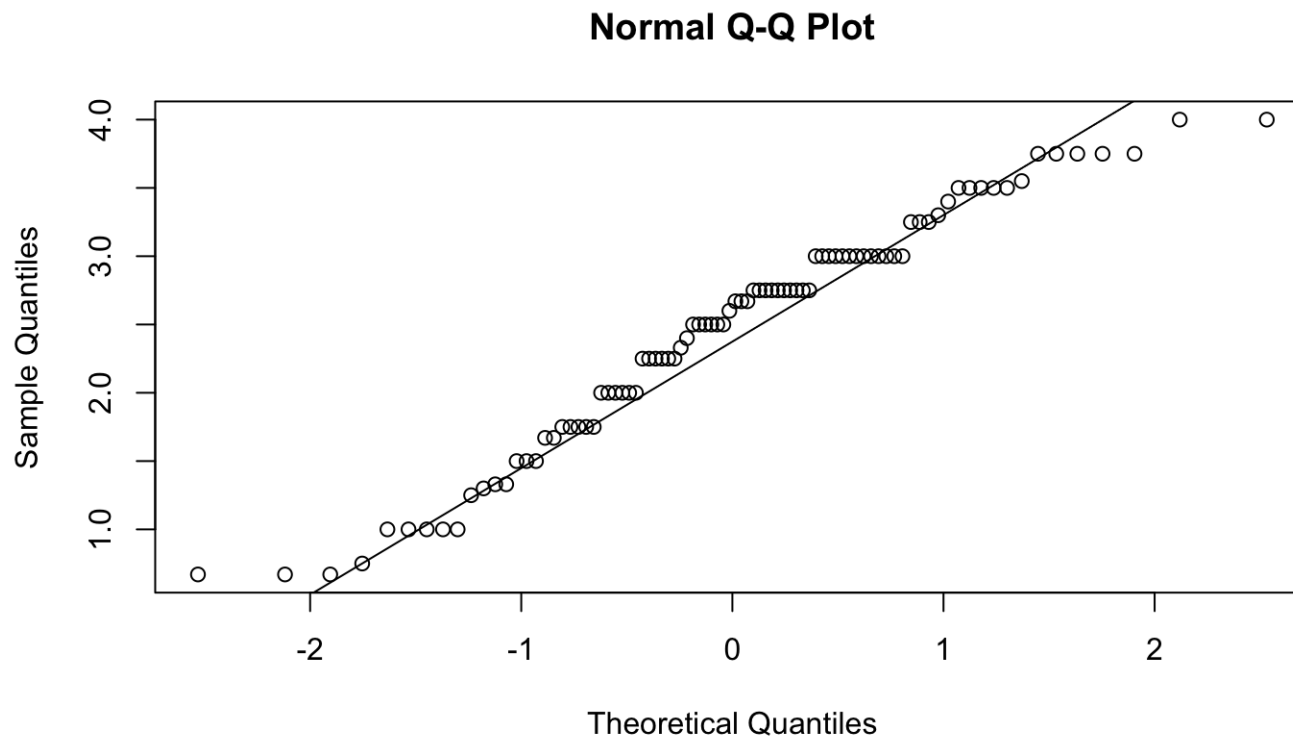
Note: If you choose to import your dataset using the point-and-click interface, be sure to mark **Yes** for Header to ensure your data loads in properly.

Create the plot

We'll now use the `qqline()` function from the base package to draw a QQ plot for any variable of choice.

Let's look at GPA first.

```
qqnorm(Add$GPA)
qqline(Add$GPA) # This adds a diagonal line
```



Another example

Now let's try another variable.

```
qqnorm(Add$ADDSC)  
qqline(Add$ADDSC)  # Add the diagonal line
```

