



FridaWin



FRIDA

**Exposure Time Calculator
Basic specifications**

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Applicable documents

Nº	Document title	Code	Issue
A.1	FRIDA Exposure Time Calculator	DC	1.A

Reference documents

Nº	Document title	Code	Issue
R.1			

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List of acronyms and abbreviations

GTC	Gran Telescopio Canarias
IA-UNAM	Instituto de Astronomía – Universidad Nacional Autónoma de México
IAC	Instituto de Astrofísica de Canarias
UF	University of Florida

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1. SUMMARY

This document describes the ETC for FRIDA in imaging mode and IFS mode. It follows similar methodology used for equivalent AO- assisted instruments at ESO and Gemini. The calculation will rely on a code developed in PHP or Java, and will be available to the user via a web server.

2. REQUIREMENTS

This section describes the requirements the ETC must fulfil. Requirements are defined according to their priority as basic or additional, which will be followed as an implementation guideline.

The ETC will be made available to the user via a web-page sitting in a web server which location (TBD) may be either the UNAM or/and the IAC, in any case these will be mirrored sites. The web interface will be used to input the relevant parameters defining a FRIDA observation. The calculations will rely on a code to be developed in any language compatible with HTML applications (Java, PHP, or Python).

The ETC will have two independent modes, serving FRIDA imaging mode and IFS mode, respectively.

2.1 Primary Requirements

The ETC should be able to estimate (as accurately as possible) the S/N of a measurement to be obtained using the following FRIDA observing configurations:

- There will be two basic choices for the source morphology: point source and extended source (uniform brightness).
- The brightness of the source will be specified as magnitude of the continuum and optionally the flux of a emission line.
- Transmission and emission of the Earth atmosphere must be included for variety of conditions (humidity and temperature).
- the instrument can operate using two generic observing modes: imaging (broad-band and narrow-band) and Integral Field Spectroscopy.
- there are 3 spatial scales for both imaging and IFS modes.
- The ETC will produce a table showing basic output quantities: achieved SNR ratio, or required exposure time to achieve a given SNR.
- Graphical output showing the variation of SNR vs exposure time (similar to Fig. 1).
- Graphical output showing the variation of SNR vs lambda for IFS observing mode, including sky emission (similar to Fig. 2).

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2.2 Secondary Requirements

- Use as input a set of modelled PSFs as expected for GTCAO, equivalently simulate GTCAO system to provide a matrix of PSFs for different values of seeing, guide star magnitude and distance...
- Include a variety of morphologies for extended objects (Sersic profiles and exponential disks)
- Include different spectral shapes as input for the spectroscopy mode (blackbody, power-law, stellar templates, galaxy templates).
- Provide an output image simulating that expected by FRIDA.
- ...

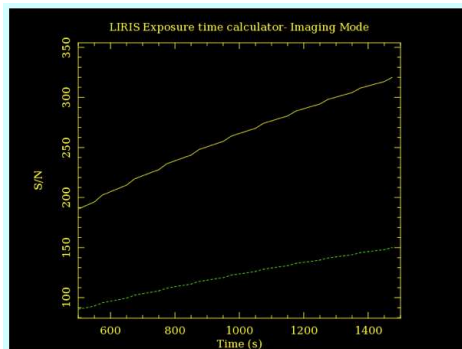


Figure 1: S/N ratio variation with exposure time

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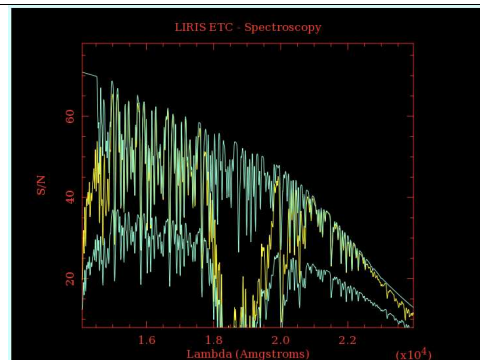


Figure 2: S/N ratio of the observed spectrum, including variations due to sky emission and absorption.

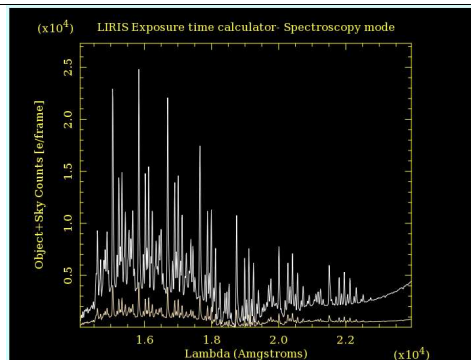


Figure 3: Simulated clean spectrum including sky OH emission lines and telluric absorption.

2.3 Structure of the Web page

The web form will be divided into different sections:

- Target related parameters (point source or extended source, brightness, spectral energy distribution, etc.)
- Observing conditions (seeing, airmass).
- AO reference target (distance to the science target and magnitude).
- Telescope and instrument configuration (GTCAO, minimum integration time)
- Instrument configuration (imaging or IFS, spatial scale, filters or grating)
-

The structure of the WEB page will be similar to what is presented in Fig. 4

Astronomical source definition

Spatial profile and brightness: [\(more info\)](#)
 Choose one of point, extended or user-defined source profile and the brightness in any filter/wavelength

☒ **Point source (nominal PSF)** with spatially integrated brightness (e.g. 19.3 mag or 2e-17 W/m^2/um)
☐ **Extended source** having ... (When this option is selected the image quality selection in section 3 of the ITC is disabled.)

☐ Gaussian profile with full width half maximum (including seeing) of arcsec and spatially integrated brightness of (e.g. 19.3 mag or 2e-17 W/m^2/um)
☒ Uniform surface brightness (e.g. 21.6 mag / sq arcsec)

with the above **brightness normalisation** applied ☒ in filter band at a wavelength micron

[calculate](#)

Spectral distribution: [\(more info\)](#)
 Choose one SED, the redshift and extinction

☐ Library spectrum of a non-stellar object
☒ Library spectrum of a star with spectral type
☐ Single emission line at wavelength micron with line flux W/m^2 and line width km/s on a flat (in wavelength) continuum of flux density W/m^2/um
☐ Model black body spectrum with temperature K
☐ Model power-law spectrum ($S_{\lambda} = \lambda^{\alpha}$)
☐ User-defined spectrum read from file (size < 1MB) no file selected

with the **spectrum mapped** to a redshift ☒ $z =$ or a radial velocity ☐ $v =$ km/s

...and subject to **dust reddening** by a foreground screen (see more info on the extinction law) having a visual extinction of $A_v =$

[calculate](#)

Figure 4: Screen capture of the FRIDA ETC - Astronomical source parameter

Observing conditions and GTCOA configuration

Typical air mass during observation: ☐ <1.2 ☒ 1.5 ☐ 2.0

Image quality (seeing): ☐ <0.6 ☒ 0.6-0.9 ☐ 0.9-1.2 ☐ 1.2-1.5 ☐ >=1.5

GTCOA properties: [\(more info\)](#)

AO guide star separation: arcsec AO guide star brightness (R-band): mag

[calculate](#)

Figure 5: Screen capture of the FRIDA ETC - Telescope and GTCOA related parameters

Comentario [JA1]: Mixing of parameters-New scheme could be

- Spatial Profile
- Point Source
- Extended Source [Uniform, Sersic, Gaussian]
- Spectral Dist.
- Continuum [Star of spectral type, Non-stellar, black-body, Power-law,...]
- Brightness (mag, erg..., but units depend on geometry)
- Single Emission Line (center, flux or EW)

Comentario [JA2]: User could specify Strehl or get estimate from model (include seeing, Guide Star separation and brightness)

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Instrument (FRIDA) configuration

Observing mode:	<input type="radio"/> Direct Imaging	<input checked="" type="radio"/> Integral Field Spectroscopy
Instrument scale:	<input type="radio"/> Fine Scale (10 mas/pix)	<input checked="" type="radio"/> Medium scale (20 mas/pix) <input type="radio"/> Coarse Scale (40 mas/pix)
Filter:	<input type="text" value="Ks Filter"/>	
Grating:	<input type="text" value="J (R-4000)"/>	Spectrum central wavelength: <input type="text" value="2.20"/> um
<input type="button" value="calculate"/>		

Figure 6: Screen capture of the FRIDA ETC - Instrument parameters

Details of observation

Calculation method: more info	
Total S/N ratio resulting from <input type="text" value="30"/> exposures each having an exposure time of <input type="text" value="120"/> secs and with a fraction <input type="text" value="1.0"/> of exposures that observe the source	
Analysis method: more info	
For Integral Field Unit (IFU) spectroscopy only ...	
<input checked="" type="radio"/>	Select multiple IFU elements to be summed : <input type="text" value="2"/> by <input type="text" value="5"/> apertures(each one 0.103x0.042 arcsec)
<input type="radio"/>	Select an individual IFU element offset by <input type="text" value="0.0"/> arcsec from the center
<input type="radio"/>	Select multiple IFU elements along a radius with offsets of <input type="text" value="0.0"/> to <input type="text" value="1.0"/> arcsec
Output:	
For spectroscopy, <input checked="" type="radio"/> autoscale or <input type="radio"/> specify limits for plotted spectra (lower wavelength <input type="text" value="2.10"/> micron and upper wavelength <input type="text" value="2.20"/> micron)	
<input type="button" value="calculate"/>	
<input type="button" value="calculate"/> <input type="button" value="reset to defaults"/>	

Figure 7: Screen capture of the FRIDA ETC - output parameters

3. THE METHOD

This section includes all relevant formulae and auxiliary information (sky emission and absorption). Firstly, the expressions used to estimate the Strehl ratio and the encircled energy are presented. Advanced versions of the ETC will allow the user to do the same computation using a library of model PSFs generated for GTCAO+FRIDA. The derivation of Signal-to-Noise ratio for the direct imaging and IFS modes are also described here.

3.1 STREHL RATIO AND ENCIRCLED ENERGY

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The ability of GTCAO system to correct the wavefront and provide a good correction for the PSF will depend on the brightness and off-axis distance of the wavefront reference target, the so-called AO guide star. The total signal from a point source will be computed as the sum of an AO-corrected core plus an uncorrected (seeing limited) halo. The Strehl ratio dictates the contribution of each of these two components. In order to compute the S/N ratio the flux contained in an user-defined aperture will be used, which is also called “Encircled Energy”. Here we will describe a simple theoretical approximation to compute the Strehl ratio. In future evolved versions of the ETC we will include computation of Strehl ratio and encircled energy from a set of simulated PSF describing GTCAO expected behaviour.

3.1.1 Expected GTCAO performance

The Strehl ratio can be approximated by the following expression:

$$SR_{tot} = SR_{fit} \times SR_{star} \times SR_{anisop}$$

and

$$SR_{fit} = \exp \left[-f_{cor} \times 0.008 \times \left(D_{tel}[m] / r_0(\lambda)[m] \right)^{5/3} \right]$$

$$SR_{star} = \exp \left[-f_{star} \times (\lambda^{norm}[\mu m] / \lambda[\mu m])^2 \times (m_R / m_R^{norm})^{n_{m_R}} \right]$$

$$SR_{anisop} = \exp \left[-f_{anisop} \times (\lambda^{anisop}[\mu m] / \lambda[\mu m])^2 \times (\theta_{GS}[arcsec] / \theta_{anisop}[arcsec])^{5/3} \right]$$

where SR_{fit} is the Strehl due to the system fitting error (limited number of actuators), SR_{star} is the Strehl loss due to the limited number of photons from the guide star (assuming photon noise limited, which is certainly an optimistic case), SR_{anisop} is the expected Strehl loss due to anisoplanatism. The values of λ^{norm} , m_R^{norm} and n_{m_R} will be determined after characterization of GTCAO, for the time being the following values are proposed $\lambda^{norm}=2.2 \mu m$, $m_R^{norm}=14.5$ and $n_{m_R}=16$. The value of θ_{anisop} is also a parameter to be measured during GTCAO characterization, the value $\theta_{anisop} = 1.93''$ at $\lambda_{anisop}=0.5 \mu m$ is proposed as an initial guess. The Fried parameter r_0 at the wavelength of the selected filter/grating can be computed from the value of seeing given at the reference wavelength (λ_{ref}), using the following expression:

$$r_0(\lambda)[m] = 0.20 \times \frac{\lambda[\mu m]}{\theta_{\lambda_{ref}}^{seeing}[arcsec]} \times \left(\frac{\lambda[\mu m]}{\lambda_{ref}[\mu m]} \right)^{1/5}$$

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Usually, the seeing will be specified at $\lambda_{ref}=0.5\mu m$.

The values of f_{cor} , f_{star} and f_{anisop} can be determined from the requirements/specs of GTCAO, although they should be close to unity. As stated in the document "GTCAO system Advanced design Overview", a SR ratio equals to 0.75 is expected at $2.2 \mu m$ for a bright guide star in good seeing conditions ($\theta_{seeing}=0.5''$ at $\lambda=0.5 \mu m$, which implies $r_0[\lambda=0.5 \mu m] = 21 \text{ cm}$). In the case of a fainter star, $mR=14.5$, the SR ratio decreases to 0.1. Using these figures and taking $r_0(2.2\mu m)=1.18m$ it results $f_{cor}\approx 1$, $f_{star}\approx 2$, $f_{anisop}\approx 1$.

Once the Strehl ratio is known the encircled energy within an user defined aperture can be obtained as the ratio between the flux within the aperture and the total flux (or number of photons). The shape of the point spread function (PSF) is required in order to estimate the spatial distribution of photons onto the detector. A simplified model with two components: a core corresponding to the expected diffraction limit (PSF) and a halo associated with the uncorrected part of the seeing disk. Both components will be simulated by Gaussian functions with FWHM, or equivalently σ , which are computed from the following expressions:

$$\sigma_{halo} = \frac{FWHM_{halo}}{2.35} = \frac{\theta_{seeing}[0.5\mu m]}{2.35} \times \left(\frac{0.5}{\lambda[\mu m]} \right)^{1/5}$$

$$\sigma_{core}[arcsec] = \frac{FWHM_{core}}{2.35} = \frac{0.055}{2.35} \times \left(\frac{\lambda[\mu m]}{2.2} \right) \times \left(\frac{10}{D_{tel}[m]} \right)$$

The flux within a circular aperture is computed as the integral up to a radius ρ_{aper}

$$F_{int}(\rho_{aper}) = \pi \left\{ A_{halo} \times \sigma_{halo}^2 \times \left[1 - \exp\left(-\rho_{aper}^2 / 2\sigma_{halo}^2\right) \right] + A_{core} \times \sigma_{core}^2 \times \left[1 - \exp\left(-\rho_{aper}^2 / 2\sigma_{core}^2\right) \right] \right\}$$

$$F_{tot} = F_{int}(\rho_{aper} = \infty) = \pi \left\{ A_{halo} \times \sigma_{halo}^2 + A_{core} \times \sigma_{core}^2 \right\}$$

$$EE(\rho_{aper}) = \frac{F_{int}(\rho_{aper})}{F_{tot}}$$

The values of A_{halo} and A_{core} are related by the Strehl ratio, as the following expression

$$A_{halo} = \frac{(1 - SR)}{SR} \times \left(\frac{FWHM_{core}}{FWHM_{halo}} \right)^2 \times A_{core}$$

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3.1.2 Encircled energy – S/N reference area

The user has to specify the radius of a 'S/N reference area' in mas (Rref). This is the area on the sky over which the photons for the S/N calculation (both object and sky) are collected. For an extended source (and the sky) the number of object (sky) photons is given by multiplying the target's (sky's) surface brightness by: $\Omega = \pi R_{ref}^2$. In the case of an extended source, it should be possible to specify a certain position within the FOV.

The reference area could be:

- The core of a point source – $f \times FWHM(\sim \lambda/D)$ [f is a factor specified by the user]
- the size of a single spaxel – a spatial element- $R_{ref} = \sqrt{\Omega_p / \pi}$
- the size of the object, $R_{ref} = \sqrt{N_{spec} \Omega_p / \pi}$

For a point source the S/N reference area is the size of the PSF at the observing band, which depends on GTCAO performance, i.e. on the spatial resolution achieved. In order to assess this performance in the ETC, per each observing band, seeing, target / NGS (natural guide star) separation, and NGS magnitude, a grid of GTCAO-FRIDA PSFs database will be constructed which will serve as input to the ETC (see below).

$$EE(\rho_{aper}) = \frac{F_{int}(\rho_{aper})}{F_{tot}}$$

The final S/N is calculated per spectral resolution element, i.e. the object's (and the sky's) light is integrated over $\Delta\lambda = \lambda_{ref}/R$, R is the spectral resolution. In FRIDA, $\Delta\lambda = 2$ pixels

Nspec determines the number of detector pixels over which the light collected from the S/N reference area is spread: $N_{pix} = 2N_{spec}$, where the factor 2 comes from the integration over wavelength. Hence, Nspec determines the readout noise and dark current.

A graph of encircled energy and S/N ratio vs. the aperture radius would be offered in order to permit the user to select a proper selection of the aperture.

3.1.3 Using PSF models

The simulated GTCAO+FRIDA PSFs will cover a limited parameter space in seeing, NGS magnitude and target-NGS separation, with a possible 4-D grid as follows:

- filters (3) = [Z_J, H, K]

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- seeings (6) = [0".4, 0".6, 0".8, 1".0, 1".2, 1".4]
- target/NGS sep. (4) = [0", 10", 20", 30"]
- NGS mag. (3) = [13,15,17]

Using this limited set of values will lead to a database of 216 GTCAO+FRIDA PSFs. From these, different quantities required for the ETC, e.g. encircled energy at given radius, shall be derived. For the ETC, the user's input parameters relevant to the AO may be different from the above parameter grid. We shall decide on whether parameters others than the ones quoted are derived from a multidimensional linear interpolation (as done in VLT-SINFONI), or – for sake of simplicity- are selected from a fixed parameter-range drop-down list offered at the ETC GUI page.

3.2 THE ATMOSPHERIC CONTRIBUTION

In the near-IR the sky brightness is dominated by the 'emission line' component (mostly OH airglow) and is quite uncertain. The reason is that the airglow is known to vary systematically by several tenths of a mag, as a function of season and time along the night, as well as randomly on shorter timescales and as a function of position on the sky. The sky continuum component – mainly controlled by the moon phase- is much less important.

The ETC will model the sky background contribution and its dependence on wavelength as the sum of OH-sky emission lines plus thermal emission from the atmosphere, telescope and instrument.

$$F_{\text{back}}(\lambda) = \text{continuum}(\lambda) + \text{em.lines}(\lambda) + \text{atm}(\lambda) + \text{tel}(\lambda)$$

Overall, for the nominal resolutions of FRIDA, $R \sim 4000$, we shall use the sky spectrum measured with LIRIS at La Palma and compared with existing published models. In the case of the FRIDA high resolution mode $R=30,000$, we may use the OH spectrum measured by e.g. ESO/CRIRES.

From the second half of the K-band onwards the background is dominated by the thermal emission from the atmosphere and the telescope. In this case, we will resort to the thermal emission used in Canaricam or EMIR when available.

The atmospheric transmission in the IR, ξ , is caused by molecular absorption which depends on the airmass. This may be derived from an atmospheric model.

For completeness purpose and consistency check we shall use the sky model described in Noll et al. (2012) which is fully implemented at ESO in the code SM-01, and will be available to us:

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<http://www.eso.org/observing/etc/bin/gen/form?INS.MODE=swspectr+INS.NAME=SKYCALC>

3.3 TARGET DEFINITION PARAMETERS

The target's flux is specified by its magnitude in any of the allowed bands, Z, J, H and K, and its flux distribution. The latter is integrated over the chosen band and then normalised to the specified magnitude. The zeropoints of the magnitude scale may be either Vega or AB (cf. Table 1). The input magnitude and the flux distribution determine the object flux, F_{obj} , at the observing wavelength, λ_{ref} .

For a selection of flux distributions, a library of stellar spectra (e.g. the Pickles library which covers up to K-band), non-stellar library (elliptical and spiral galaxies) may be offered in the ETC.

The target's flux at λ_{ref} could also be specified directly in mJy.

The source geometry can be chosen to be a point source or an extended source.

Table 1. Photometric zeropoints

Band	Central wavelength [μm]	ZVega = $-\log F_0$ [W/m ² / μm]	ZAB = $-\log F_0$ [W/m ² / μm]
I	0.79	7.91	7.77
J	1.25	8.51	8.14
H	1.65	8.94	8.39
K	2.16	9.40	8.64

3.4 THE IMAGING CASE

The Signal-to-Noise ratio will be computed using the following expressions:

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$$\frac{S}{N} = \frac{\sqrt{N_{\text{exp}}} \times \Phi_{\text{obj}}}{\sqrt{\Phi_{\text{obj}} + \Phi_{\text{sky}} + n_{\text{pix}}(rn^2 + dk \times DIT)}}$$

$$\Phi_{\text{obj}}(\lambda) = A_{\text{tel}} \times EE \times DIT \times \int \xi(\lambda) \times F_{\text{obj}}(\lambda) / E_{\gamma} \times \varepsilon(\lambda) \times d\lambda$$

$$\Phi_{\text{sky}}(\lambda) = \Omega \times A_{\text{tel}} \times DIT \times \int F_{\text{sky}}(\lambda) / E_{\gamma} \times \varepsilon(\lambda) \times d\lambda$$

3.5 THE INTEGRAL FIELD SPECTROSCOPY CASE

The Signal-to-Noise ratio will be computed using the following expressions:

$$\frac{S}{N} = \frac{\sqrt{N_{\text{exp}}} \times \Phi_{\text{obj}}}{\sqrt{\Phi_{\text{obj}} + \Phi_{\text{sky}} + n_{\text{pix}}(rn^2 + dk \times DIT)}}$$

$$\Phi_{\text{obj}}(\lambda) = \xi(\lambda) \times F_{\text{obj}}(\lambda) / E_{\gamma} \times A_{\text{tel}} \times \Delta\lambda \times \varepsilon \times EE \times DIT$$

$$\Phi_{\text{sky}}(\lambda) = F_{\text{sky}}(\lambda) \times \Omega / E_{\gamma} \times A_{\text{tel}} \times \Delta\lambda \times \varepsilon \times DIT$$

APPENDIX A

A description of the parameters used in the definition of this ETC follows:

- m_{obj} : Object magnitude (for a point source) or object surface brightness (for an extended source) in a specified band (J, H, K) and magnitude system (Vega or AB) [mag or mag/arcsec²]
- $F_0 = 10^{-Z}$: Photometric zeropoint [W/m²/μm]
Z may be either Vega or AB magnitude. The various values for the different bands are listed in Table 1.
- F_{obj} : Object flux (point source) or surface brightness (extended source) at the top of the atmosphere [W/m²/μm or W/m²/μm/arcsec²]

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$$F_{\text{obj}} = F_0 10^{-0.4 m_{\text{obj}}}$$

This formula is only true for the case of a uniform flux distribution. Otherwise m_{obj} is used to normalise the flux distribution so that the distribution's integral over the band is equal to the flux given by m_{obj} .

The user can specify m_{obj} or use directly F_{obj} [mJy or mJy/arcsec²]

- χ : Airmass.

Options: 1, 1.15, 1.5 or 2.

- D: Telescope diameter. [m]

- A: Photon collecting area of the telescope. [m²]

$A = \pi/4 (D^2 - d^2)$, where d is the diameter of the central obstruction.

- Rref : Radius of the circular S/N reference area [mas]

Rref -point-like source = size of the PSF at the observing band

Rref -extended source = size of the spaxel (ie. S/N is calculated in a single spectrum) or size of the object

- Ω : Size of the S/N reference area. Ω_p = Size of the spaxel [mas²]

$$\Omega = \pi R_{\text{ref}}^2$$

- Nspec: Number of individual spectra on the detector covering the S/N reference area. In FRIDA, the separate spatial element (spaxel) is equal to at least 2 Nspec.

- λ_{ref} : Observing wavelength, the S/N is calculated as a function of wavelength centered in λ_{ref} . [μm]

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- R: Spectral resolution
- $\Delta\lambda$: Wavelength range used for the integration over wavelength. [μm]
Set equal to a resolution element: $\Delta\lambda = \lambda_{\text{ref}}/R = 2$ detector pixels in FRIDA
- ξ : Atmospheric transmission
Depends on airmass and λ_{ref}
- $\langle F_{\text{obj}} \rangle$: Object flux (point source) or object surface brightness (extended source) at the telescope entrance [$\text{W}/\text{m}^2/\mu\text{m}$ or $\text{W}/\text{m}^2/\mu\text{m}/\text{arcsec}^2$]
 $\langle F_{\text{obj}} \rangle = \xi F_{\text{obj}}$
- ε : Total efficiency of telescope + FRIDA
- E_{γ} : Photon energy at λ_{ref} [J/γ]
 $E_{\gamma} = 1.985 \times 10^{-19} / \lambda_{\text{ref}}$
- c: Total conversion factor from energy flux incident at the telescope entrance to detected number of photo-electrons.[e^-/s per $\text{W}/\text{m}^2/\mu\text{m}$]
 $c = \varepsilon \Delta\lambda A / E_{\gamma}$
- T: Detector exposure time for one exposure (DIT) [s]
- n_{exp} : Number of exposures (NDIT)

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- e : Encircled energy or fraction of PSF in the S/N reference area.
- N_{obj} : Number of detected electrons from object in the S/N reference area per exposure [e-]
For a point source: $N_{obj} = \langle F_{obj} \rangle e c T$
For an extended source: $N_{obj} = \langle F_{obj} \rangle \Omega c T$
- F_{sky} : Background surface brightness [W/m²/μm/arcsec²]
- N_{sky} : Number of detected electrons from the background in the S/N reference area per exposure [e-]
 $N_{sky} = F_{sky} \Omega c T$
- N_{pix} : Number of detector pixel over which the light from the S/N reference area is spread.
 $N_{pix} = 2 N_{spec}$, where the factor 2 comes from the integration over wavelength.
- d : Detector dark current [e-/s/pixel]
- r : Detector read-out noise [e-/pixel]
- S/N: Signal-to-noise ratio per resolution element
$$S/N = \text{SQR}(n_{exp}) N_{obj} / \text{SQR} (N_{obj} + N_{sky} + N_{pix} r^2 + N_{pix} d T)$$

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