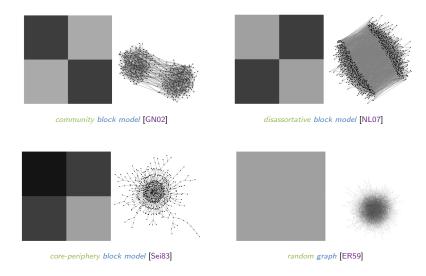
core-periphery structure

introduction to network analysis in Python (NetPy)

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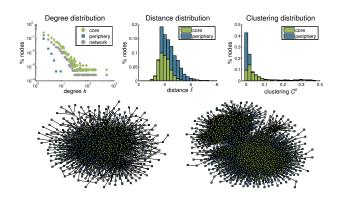
core-periphery block model



^{*}origin of core-periphery structure in international relations

core-periphery structure

- core/periphery nodes have higher/lower degrees k
- core/periphery nodes are on shorter/longer distances ℓ
- core/periphery nodes have higher/lower clustering C



core-periphery *stochastic*

- $G(\{C_1, C_2\}, \{p_{11}, p_{12}, p_{22}\})$ stochastic block model [HLL83] — n_i is size of cluster C_i & p_{ij} is link density between C_i and C_j
- density-based core-periphery structure for $p_{11} \gg p_{12} \gg p_{22}$
- lookalike core-periphery for $n_1p_{11}\gg 1$, $n_1p_{12}\ll 1$, $n_2p_{22}\approx 1$



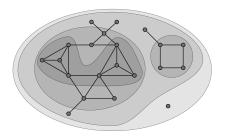
non-corrected block model $p_{11} > p_{12} > p_{22}$



degree-corrected block model $p_{11} \approx p_{22} > p_{12}$

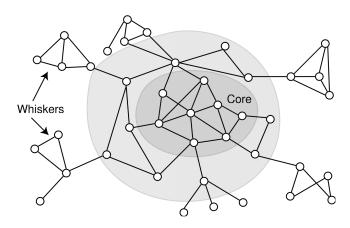
core-periphery *k-cores*

- k-cores are subgraphs of nodes with $\geq k$ neighbors [Sei83] remove nodes with degree < k until no such node remains [BZ11]
- k-shells are nodes of k-cores that are not in k+1-cores
- k-cores are nested while k-shells form decomposition



0-cores are connected components & k-cores can be disconnected

core-periphery *nestedness*



nested cores & whiskers communities [LLDM09, YL13]

core-periphery references



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