

Logic Tutorial 2 Solutions

1) a.

- i) False *A sees B* is false, and *B sees C* is true. $False \leftrightarrow True$ is False.
- ii) True *B next-to D* is True. $True \vee anything$ is True.
- iii) True *F above A* is False. $anything \wedge False$ is False, and $\neg (False)$ is True.
- iv) True *A sees E* is False. So $\neg[A \text{ sees } E]$ is True, and $anything \rightarrow True$ is True.
- v) True Consider $\neg([B \text{ above } E] \leftrightarrow [B \text{ next-to } C])$. This is $\neg(True \leftrightarrow False)$ which is $\neg(False)$ which is True.

b. The following is an example:

A	B	D
F	C	
		E

2.

a. Contingency

P	Q	$P \vee Q$	$P \wedge (P \vee Q)$
T	T	T	T
T	F	T	T
F	T	T	F
F	F	F	F

b. Contingency

P	Q	$P \vee Q$	$P \rightarrow Q$	$(P \vee Q) \wedge (P \rightarrow Q)$
T	T	T	T	T
T	F	T	F	F
F	T	T	T	T
F	F	F	T	F

c. Inconsistency

P	Q	$\neg P$	$Q \rightarrow P$	$P \vee (Q \rightarrow P)$	$Q \wedge \neg P$	Given wff c.
T	T	F	T	T	F	F
T	F	F	T	T	F	F
F	T	T	F	F	T	F
F	F	T	T	T	F	F

d. Tautology

P	Q	$Q \vee P$	$P \wedge (Q \vee P)$	$P \wedge (Q \vee P) \leftrightarrow P$
T	T	T	T	T
T	F	T	T	T
F	T	T	F	T
F	F	F	F	T

e. Tautology

P	Q	$P \rightarrow Q$	$\neg P$	$\neg P \vee Q$	Given wff in e.
T	T	T	F	T	T
T	F	F	F	F	T
F	T	T	T	T	T
F	F	T	T	T	T

f. Tautology – I leave the details to you!