

sequences  $X = \langle A, B, C, B, D, A, B \rangle$  and  $Y = \langle B, D, C, A, B, A \rangle$ . The running time of the procedure is  $\Theta(mn)$ , since each table entry takes  $\Theta(1)$  time to compute.

**LCS-LENGTH**( $X, Y, m, n$ )

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1  let  $b[1:m, 1:n]$  and  $c[0:m, 0:n]$  be new tables
2  for  $i = 1$  to  $m$ 
3       $c[i, 0] = 0$ 
4  for  $j = 0$  to  $n$ 
5       $c[0, j] = 0$ 
6  for  $i = 1$  to  $m$            // compute table entries in row-major order
7      for  $j = 1$  to  $n$ 
8          if  $x_i == y_j$ 
9               $c[i, j] = c[i - 1, j - 1] + 1$ 
10              $b[i, j] = "\nwarrow"$ 
11         elseif  $c[i - 1, j] \geq c[i, j - 1]$ 
12              $c[i, j] = c[i - 1, j]$ 
13              $b[i, j] = "\uparrow"$ 
14         else  $c[i, j] = c[i, j - 1]$ 
15              $b[i, j] = "\leftarrow"$ 
16  return  $c$  and  $b$ 
```

**PRINT-LCS**( $b, X, i, j$ )

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1  if  $i == 0$  or  $j == 0$ 
2      return           // the LCS has length 0
3  if  $b[i, j] == "\nwarrow"$ 
4      PRINT-LCS( $b, X, i - 1, j - 1$ )
5      print  $x_i$        // same as  $y_j$ 
6  elseif  $b[i, j] == "\uparrow"$ 
7      PRINT-LCS( $b, X, i - 1, j$ )
8  else PRINT-LCS( $b, X, i, j - 1$ )
```

#### Step 4: Constructing an LCS

With the  $b$  table returned by **LCS-LENGTH**, you can quickly construct an LCS of  $X = \langle x_1, x_2, \dots, x_m \rangle$  and  $Y = \langle y_1, y_2, \dots, y_n \rangle$ . Begin at  $b[m, n]$  and trace through the table by following the arrows. Each “ $\nwarrow$ ” encountered in an entry  $b[i, j]$  implies that  $x_i = y_j$  is an element of the LCS that **LCS-LENGTH** found. This method gives you the elements of this LCS in reverse order. The recursive procedure **PRINT-LCS** prints out an LCS of  $X$  and  $Y$  in the proper, forward order.