

Analysis of Strassen

$$T(n) = 7 T(n/2) + \Theta(n^2)$$

$$n^{\log_b a} = n^{\log_2 7} \approx n^{2.81} \implies \text{CASE } 1 \implies T(n) = \Theta(n^{\log_2 7}).$$

The number 2.81 may not seem much smaller than 3, but because the difference is in the exponent, the impact on running time is significant. In fact, Strassen's algorithm beats the ordinary algorithm on today's machines for $n \ge 32$ or so.

Best to date (of theoretical interest only): $\Theta(n^{2.376\cdots})$.