



Example of substitution

$$\begin{aligned}T(n) &= 4T(n/2) + n \\&\leq 4c(n/2)^3 + n \\&= (c/2)n^3 + n \\&= cn^3 - ((c/2)n^3 - n) \leftarrow \textit{desired} - \textit{residual} \\&\leq cn^3 \leftarrow \textit{desired}\end{aligned}$$

whenever $(c/2)n^3 - n \geq 0$, for example,
if $c \geq 2$ and $n \geq 1$.
 \nwarrow
residual