

Set definition of O-notation

$$O(g(n)) = \{ f(n) : \text{there exist constants}$$

 $c > 0, n_0 > 0 \text{ such}$
 $\text{that } 0 \le f(n) \le cg(n)$
 $\text{for all } n \ge n_0 \}$

EXAMPLE: $2n^2 \in O(n^3)$

(Logicians: $\lambda n.2n^2 \in O(\lambda n.n^3)$, but it's convenient to be sloppy, as long as we understand what's really going on.)