

Calculating expectation

$$\begin{split} E[T(n)] &= E\bigg[\sum_{k=0}^{n-1} X_k \big(T(k) + T(n-k-1) + \Theta(n) \big) \bigg] \\ &= \sum_{k=0}^{n-1} E\big[X_k \big(T(k) + T(n-k-1) + \Theta(n) \big) \big] \\ &= \sum_{k=0}^{n-1} E\big[X_k \big] \cdot E\big[T(k) + T(n-k-1) + \Theta(n) \big] \end{split}$$

Independence of X_k from other random choices.