

Three common cases

Compare f(n) with $n^{\log_b a}$:

- 1. $f(n) = O(n^{\log_b a \varepsilon})$ for some constant $\varepsilon > 0$.
 - f(n) grows polynomially slower than $n^{\log_b a}$ (by an n^{ϵ} factor).

Solution:
$$T(n) = \Theta(n^{\log_b a})$$
.

- 2. $f(n) = \Theta(n^{\log_b a} \lg^k n)$ for some constant $k \ge 0$.
 - f(n) and $n^{\log_b a}$ grow at similar rates.

Solution:
$$T(n) = \Theta(n^{\log_b a} \lg^{k+1} n)$$
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