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## Aufgabe 4.19

```
dbtype myCholesky.m

A = [4,-2,0;-2,5,-2;0,-2,3];
R = myCholesky(A);
R2 = chol(A);

disp('A = ');
disp(A);

disp('Linke untere Dreiecksmatrix der eigenen Cholesky-Zerlegung:');
disp(R);

disp('chol Funktion von Matlab:');
disp(R2);
```

```
1    function C = myCholesky(A)
2    n = size(A,2);
3    C = zeros(n,n);
4
5    for j=1:n
6
7        for k=1:j-1
8            tmp = 0;
9            for l=1:k-1
10               tmp = tmp + C(j,l) * conj(C(k,l));
11            end
12            C(j,k) = (A(j,k) - tmp) / C(k,k);
13        end
14
15        cj = abs( C(j,:) );
16        cj = cj.^2;
17        cj_sum = sum(cj(1:j-1));
18        C(j,j) = sqrt(A(j,j) - cj_sum );
19
20    end
21 end
A =
```

```
    4    -2     0
   -2     5    -2
    0    -2     3
```

Linke untere Dreiecksmatrix der eigenen Cholesky-Zerlegung:

```
    2.0000     0     0
   -1.0000    2.0000     0
         0   -1.0000    1.4142
```

chol Funktion von Matlab:

```
    2.0000   -1.0000     0
         0    2.0000   -1.0000
```

## Aufgabe 4.21

a)  $A \cdot x = b$

dbtype `JacobiVerfahren.m`

```
n = 10;
alpha = 0.5;
kmax = 100;

A = diag(ones(n-1,1)*alpha,1) + diag(ones(n-1,1)*alpha,-1) +
    diag(ones(n,1));
b = linspace(1,n,n)';
x0 = zeros(n,1);

rel_errors = [];
real_x = inv(A)*b;

for k=1:kmax
    x = JacobiVerfahren(A, b, x0, k);
    x_error = norm(real_x - x)/norm(real_x);
    rel_errors = [rel_errors; x_error];
end

plot(linspace(1,kmax,kmax), rel_errors);
title('alpha = 0.5')
xlabel('Iterationen')
ylabel('Relativer Fehler')

% b)
% neues alpha sonst das gleiche
alpha = 0.25;
A = diag(ones(n-1,1)*alpha,1) + diag(ones(n-1,1)*alpha,-1) +
    diag(ones(n,1));

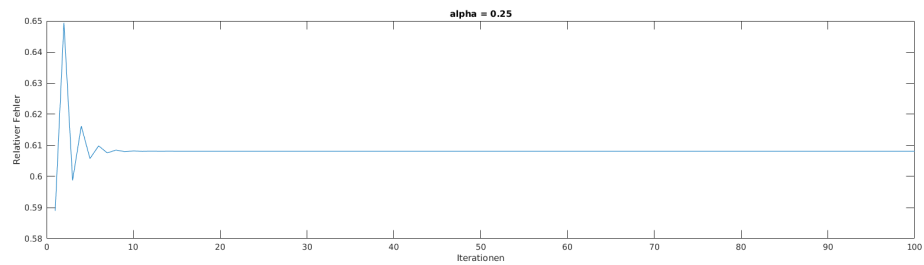
rel_errors = [];

for k=1:kmax
    x = JacobiVerfahren(A, b, x0, k);
    x_error = norm(real_x - x)/norm(real_x);
    rel_errors = [rel_errors; x_error];
end

plot(linspace(1,kmax,kmax), rel_errors);
title('alpha = 0.25')
xlabel('Iterationen')
ylabel('Relativer Fehler')
```

---

```
1  function x = JacobiVerfahren(A,b,xs,kmax)
2      n = size(A,1);
3
4      xs_tmp = xs;
5
6      for k=[0:kmax]
7          for i=1:n
8              tmp=0;
9              for j=[1:i-1,i+1:n]
10                 tmp = tmp + A(i,j) * xs(j);
11             end
12             xs_tmp(i) = (b(i) - tmp)/(A(i,i));
13         end
14
15         xs = xs_tmp;
16     end
17     x = xs_tmp;
18 end
```



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