# Age Distribution Inference of Blood cells

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## 1 Recent Progress - April 2

#### 1.1 Redefine the problem

From my point of view, the original formula ?? does not give a direct computation of HbA1c, but involves the related factors, i.e., G(t) and  $f_{RBC_{age}}(t)$ , and how they affect the measurement HbA1c together.

Based on the formula ?? and further assumptions, we try to define a direct computation formula of HbA1c.

First define a new factor v(t) = f(G(t)), the glycation rate – the added percentage of glycation per day. Specifically, one of its valid units can be %/d.

Thus the new formula that can directly compute HbA1c is

$$HbA1c(t) = \int_0^\infty v(t-a) \left[ 1 - \int_0^a f_{RBC_{age}}(\tau) d\tau \right] da.$$
 (1)

#### 1.2 Specify the glycation rate

Assumptions:

- 1. Suppose the glucose concentration G contributes linearly to the glycation rate v.
- 2. Suppose the oldest cells' life is 120 days.
- 3. Suppose the oldest cells reach a 20% level of glycation in 250 mg/dL glucose concentration, which is the inner environment of a person with type 1 diabetes.

The glycation rate can be specified as

$$v(t) = \frac{G(t)20\%}{250 \text{mg/dL} \times 120 \text{d}}.$$
 (2)

So the final formula of HbA1c is

$$HbA1c(t) = \int_0^\infty \frac{G(t-a)20\%}{250 \text{mg/dL} \times 120 \text{d}} \left[ 1 - \int_0^a f_{RBC_{age}}(\tau) d\tau \right] da.$$
 (3)

#### 1.3 Simulations

Suppose the G(t) is circulant, i.e., we extend the measurement sequence periodically due to the practical limitation. The simulation sequence is collected from PhysioNet<sup>1</sup>.

Here we use G[n] = [135, 140, 169, 215, 224, 201, 265, 252, 332, 325, 296,240, 285, 294, 276, 273, 296, 286, 349], where the last entry is the latest measurement. And suppose the measurement interval is 1 day. The HbA1cis computed as  $10.5\%^2$  by prediction from the mean of glucose concentration  $\mathbb{E}[G] \approx 255.42 \text{mg/dL}.$ 

#### Uniform distribution

Suppose  $f_{RBC_{age}}(t)$  follows from uniform distribution with mean  $M_{RBC}$ ,

$$f_{RBC_{age}}(t) = \frac{1}{2M_{RBC}} \qquad 0 \le t \le 2M_{RBC}.$$

For approximation, through binning the domain of  $f_{RBC_{age}}(t)$ , we have

$$\sum_{n=0}^{M_{RBC}-1} \tilde{v}(n) \times 1 \times \frac{2M_{RBC} - n}{2M_{RBC}} = HbA1c \tag{4}$$

where  $\tilde{v}(n) = \frac{\tilde{G}(n)20\%}{250 \text{mg/dL} \times 120 \text{d}}$  and  $\tilde{G}(n) = G(-n)$ . This results in  $M_{RBC} \approx 58$  days, thus showing

$$f_{RBC_{age}}(t) = \frac{1}{116}$$
  $0 \le t \le 116$ .

Because we have the similar assumed value with G, the result is no wonder related to the oldest age of cells.

<sup>&</sup>lt;sup>1</sup>https://physionet.org/physiobank/database/mimic2cdb-ps/s20794/#234

<sup>&</sup>lt;sup>2</sup>https://www.uptodate.com/contents/calculator-glycemic-assessment-usingconventional-or-si-units-for-hemoglobin-a1c

## 2 Questions - March 30

1. Should the G term in the formula be G(t-a) instead of G(-a) in the original word text?

$$HbA1c(t) = \int_0^\infty G(t-a) \left[ 1 - \int_0^a f_{RBC_{age}}(\tau) d\tau \right] da$$
 (5)

- 2. Is this formula equal to the practical measurement up to a constant? If yes, so how do we deal with this constant? (Suppose G is a constant, and M is the mean of a uniform distribution, then H = GM where the true mean  $M_{age} = \frac{M}{\alpha}$ . Ideally set the maximum of the support to be 120 days and then do a scale).
- 3. Can we use monte carlo integration to solve this problem? Is there any relationship between monte carlo integration with sampling theorem?
- 4. How do we define the measurement at t=0, i.e., HbA1c(0)?
- 5. Is this formula equal to the practical measurement up to a constant?
- 6. When we mention to "measure multiple HbA1c", are we referring to multiple measurements on the same blood sample or multiple measurements on different blood samples?
- 7. At this time, if we take G(t) as a constant and assume the shape of f, it seems solvable for uniform assumption and finite exponential assumption. But in practice, because both G and f are changing, and every time there are new signals entering, I can not see the process of taking deconvolution method, can you give me some more hints on this method? Or do we need to take other assumptions?