



Overview



Learning objectives for lecture series:

- basic models of accelerator physics
- suitable methods for their implementation

Topics covered:

- 1. reduced models: steering, focusing, acceleration
- 2. maps of linear periodic systems + stability analysis
- beam transport models: particles, beam distributions (self-consistent modelling)
- 4. control-room applications and diagnostics:
 - tune reconstruction
 - → tomographic reconstruction of phase space
 - closed-orbit control

Examination



- 30 min oral exam
- format = conceptual discussion on models of accelerator physics and numerical implementations
- \blacksquare exam material = \sum summary slides

you do <u>not</u> need to know how to write python code −
 focus on the ideas and concepts we discussed!



- I. basic concepts: lectures 1-3
- II. longitudinal dynamics: lectures 4-6
- III. transverse dynamics: lectures 7-8
- IV. applications: lectures 9-14



- basic concepts: lectures 1-3
 - → using the simple pendulum as example
 - time scales in a synchrotron (transverse / longitudinal motion period, storage times)
 - → phase space (system state), Hamiltonian (equations of motion)
 - → discrete integrators: Euler, Euler-Cromer, leapfrog
 - → statistical moments, emittance
 - mon-linearities, Liouville theorem vs. filamentation (emittance growth)
 - → discrete frequency analysis, NAFF algorithm (vs. FFT)
 - control of simulation error sources:
 - 1. discretisation error (symplecticity!)
 - 2. modelling error
 - 3. numerical artefacts
 - 4. (input error)
 - deterministic chaos,
 early indicators: (max.) Lyapunov exponent, frequency map analysis



- I. basic concepts: lectures 1-3
- II. longitudinal dynamics: lectures 4-6
 - \rightarrow Lorentz force, electric longitudinal field E_z to accelerate
 - → beam rigidity, paraxial approximation
 - → momentum compaction, phase slippage, transition energy
 - phase focusing and stability (classical vs. relativistic regime)
 - → longitudinal tracking equations (discrete one-turn map)
 - → synchrotron Hamiltonian, rf bucket
 - → Monte-Carlo sampling (random number generation)
 - equilibrium distributions (thermal PDF),
 - small-amplitude approximation vs. nonlinear matching
 - → emittance growth mechanisms (filamentation ↔ bucket non-linearity) from dipole and quadrupole moment oscillations



- basic concepts: lectures 1-3
- II. longitudinal dynamics: lectures 4-6
- III. transverse dynamics: lectures 7-8
 - magnetic fields for bending (steering) and focusing
 - → multipole representation, dipole / quadrupole / sextupole magnets
 - → Hill differential equation, quasi-harmonic oscillation
 - → betatron transport matrices
 - → FODO cell, alternate-gradient focusing
 - \longrightarrow optics / Twiss functions, β -function as beam envelope, dispersion function
 - → stability of periodic transport maps
 - betatron tune, chromaticity



- L basic concepts: lectures 1-3
- II. longitudinal dynamics: lectures 4-6
- III. transverse dynamics: lectures 7-8
- IV. applications:
 - → longitudinal phase-space tomography (lecture 9)
 - Radon transform, sinogram, Fourier Slice Theorem
 - filtered back projection vs. algebraic reconstruction technique
 - → closed orbit distortion (lecture 10)
 - local orbit correction (bumps)
 - global orbit correction (orbit response matrix, SVD)
 - → machine learning (lectures 11-12)
 - → Bayesian optimisation (Gaussian processes, uncertainty modelling)
 - reinforcement learning (discrete vs. continuous state/action spaces, Q-learning & actor-critic methods)
 - → self-consistent modelling / collective effects (lecture 13)
 - categories of beam interactions (space charge, ...)
 - longitudinal space charge, line density derivative λ' model
 - microwave instability

You have gained solid fundamental knowledge on numerical modelling of periodic physics + have seen in action some dynamical examples from accelerator physics!

... and perhaps became a happy python user.

Well done! :))